Color Rendering Index: the NEMA Lighting Commission A Industry Position

OCKETED Industry Position on the Color Rendering
14-BSTD-01 Index.

Introduction

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The color rendering index (CRI is a JAN 27 2015 performance metric for lighting products that has generated much discussion in recent years. This discussion is moving into lighting efficiency policy discussions. The Lighting Systems Division of the National Electrical Manufacturers Association (NEMA) believes it would be incorrect and unfortunate for consumers, producers, and public policy to give too much weight to CRI in energy efficiency policy. This position paper explains why.

Background

At a technical level the Illuminating Engineering Society (IES), defines the CRI value of a light source as a "measure of the degree of color shift objects undergo when illuminated by the light source as compared with the color of those same objects when illuminated by a reference source of comparable color temperature." In practical terms, CRI is a measure of how closely a light source reproduces the colors of a standardized set of 8 to 14 test color samples in comparison with an incandescent reference light source, or one which emulates a phase of daylight. In this sense, the Index is a comparator, indicating the fidelity with which a light source reproduces colors, again, in comparison to a reference light source. Importantly: it does not indicate the preference that people have for any light source in question.

The comments below are the views of Dr. Lorne Whitehead, a Professor of Physics at the University of British Columbia, who serves on the Board International Commission on Illumination and its Technical Committee TC1-90, which is responsible for updating the CIE Color Rendering Index. He is also a member of the Color Committee of the Illuminating Engineering Society. In addition to his university work, Dr. Whitehead is an accredited Professional Engineer with considerable business experience in Illuminating Engineering. His efforts center on assessing and improving the quality and efficiency of illumination in buildings and the displays in computers and televisions.

Color rendering is a complex scientific topic that is often misunderstood even by highly educated people. Those wishing to participate in the debate should first understand the topic. To help with this, there is a recently published color rendering tutorial in LEUKOS, freely available online:

Tutorial: Color Rendering and Its Applications in Lighting DOI: 10.1080/15502724.2014.989802

Below, Dr. Whitehead points out statements in the NEMA position which, in there current form, could mislead readers. Each bulleted point below is made in reference to the corresponding highlighted section of the NEMA text to its left.

• This sentence implies that the aim of the CRI has been to assess "preference" of light sources, but this has never been the case. The CRI has always had a single clear important purpose – to measure the accuracy with which a light source renders the colors of surfaces. This is an objective idea that can be accurately quantified. In contrast, the idea of "preference" concerns aesthetic choices which are personal and context-dependent. It is an important, but completely different topic.

CRI has entered energy efficiency policy discussions of late, in part because of a misconception that the closer a light source's CRI value is to the CRI value of an incandescent lamp, the greater the expected level of consumer satisfaction with the light source. NEMA believes this perception is mistakenly arrived at, because incandescent light has its drawbacks too, and it is at times not selected as the preferred light source in direct comparison tests with light sources having more saturated light. Put another way, strictly copying or mimicking incandescent lighting performance requirements could lead to copying its deficiencies as well. It is worth mentioning that CRI was originally developed to evaluate fluorescent lighting and there are known deficiencies in applying the Index to solid-state lighting.

Numerous organizations, with members who are the scientific and engineering experts on the science of light, are speaking out against using high CRI requirements as a correlate of consumer satisfaction . Recently, Lighting Europe issued a paper cautioning against high CRI requirements and affirming existing EU regulations which set the minimum at 80. Earlier this year, the IES issued a Position Statement cautioning against using CRI as a strict metric for lighting regulations until the Society's Task Group has completed their work on new approaches to color metrics. A recent presentation by Yoshi Ohno of NIST indicates that optimally saturated CRI 75 light is equally preferred to CRI 93 light. The NEMA Lighting Systems Division adds its voice to the call for temperance in over-reliance on CRI as a guarantor of satisfaction.

- The numerous credible proponents of high CRI absolutely understand there are several important measures of lamp quality. CRI is an important one, but not the only one. To satisfy consumers, a lamp must satisfy them all.
- With high CRI light, colors are stable and therefore have reliable meaning. This allows people to judge the freshness of food, the healthiness of complexion, and to create color designs that will reliably harmonize. Daylight, incandescent light and others can enable this.
- The CRI was always intended to assess all kinds of light sources. Like most measures, the CRI isn't perfect and is being improved. It certainly will be used effectively with solid state lighting.
- True, some organizations with some scientific members have recently spoken against the CRI, but that doesn't mean their scientific members were consulted sufficiently. For example, the IES Position Statement on CRI was passed by its Board without review by its Color Committee. The IES has since received strong criticism from universities and lamp manufacturers for their position statement.
- Even if one particular CRI 75 lamp might look good to certain people in a specific isolated setting, a different manufacturer's CRI 75 lamp could cause the same objects to take on disturbingly different shade of color.
- No credible group has ever claimed the CRI is a "guarantor of satisfaction". But it does appropriately assess one very important way in which a light source may fail to meet human needs.

Discussion

There is no evidence today to suggest that consumers demand or prefer a CRI value higher than 80 in general indoor illumination applications. It is worth pointing out that it is difficult for the human eye to distinguish the difference between CRI values that differ 5 points or less. A CRI value of 80 is common among high volume (i.e. well liked) highefficiency lamps in the market today and is the current minimum threshold for numerous country- and regional-level regulations and incentive programs. The Alliance for Solid-State Illumination Systems and Technologies (ASSIST) as established in 2002 by the Lighting Research Center (LRC) recommends a minimum of CRI 80 (together with gamut area index, a measure of how saturated the light is, between 80 and 100) for its "Class A" rating of LED lamps. A 2014 study by Consumer Reports magazine indicates that CRI 80 is satisfactory for most indoor applications. Lastly, in June 2014 the U.S. Environmental Protection Agency announced that they had met their 12-month challenge to sell 20 million ENERGY STAR certified LED bulbs. Such a feat seems unlikely if consumers were not pleased with the products, and a review of the ENERGY STAR Lamps qualified products list reveals less than 3% of these lamps feature a CRI value of 90 or greater. This percentage is even lower if high-efficacy products are selected.

- There is plenty of evidence that when people have the chance to observe the color differences between different CRI 80 lamps, most strongly prefer the consistency of high CRI.
- One reason that CRI 80 is common today is that manufacturers originally found it expensive to go higher, and most consumers didn't know any better. That doesn't show that CRI 80 is best for consumers; as with many quality factors consumers can't judge this very well at the time of purchase.
- Just because a few groups have been talked into a misconception doesn't make it right. Interestingly, they all seem to agree the CRI is important and should be regulated. Now perception experts should determine the best CRI value, overall, for consumers. This question is addressed in the appended manuscript, which has been accepted for publication and will soon appear freely online in LEUKOS.
- In the past, consumers have often been convinced to adopt inadequate products because the problems weren't obvious.
 That is why consumers need experts to look out for them, and why CRI is already regulated. The key question is what is the optimum CRI value for people. The best answer for consumers may not be the most profitable short term outcome for some manufacturers, but they will readily adapt.

With respect to consumer preference, industry and consumer advocates have been working together for several years to educate consumers and increase awareness of the wider variety of choices now presented. The LUMEN Coalition is one good example of these efforts. Rather than limit flexibility and choice, we suggest that the issue of color is better addressed with consumer education than assuming high CRI is a guarantee of satisfaction or essential to all lighting applications. Supply and demand will achieve the right result for meeting consumer satisfaction; questionable regulatory requirements unrelated to energy efficiency will not.

Conclusion

NEMA joins with those cautioning against requirements of CRI above 80 for the purpose of regulatory or other minimum performance requirements. NEMA supports the importance of good color quality and encourages the ongoing work to develop new approaches to color metrics. A minimum threshold of CRI 80 provides flexibility and allows further innovation and price tradeoffs which will promote the continued evolution and adoption of LED lighting worldwide.

- Recognizing that high CRI is practical and desirable is in no way inconsistent with consumer education and does not imply that other attributes are unimportant.
- It is well known that often supply and demand alone fail to yield needed improvement. (Consider seat belts and air bags.) Consumer rely on regulations to ensure their interests.
- Others, such as NRDC, have stated that higher CRI will require more power, but this is an incorrect view arising from a common scientific misunderstanding, as explained in the appended paper.
- The typical current minimum of CRI 80 has had a major *inhibitory* effect on innovation as evidenced by the fact that the vast majority of lamps sold today have a CRI around 80, presumably because they cost less to manufacture at current volumes. Regulations that encourage higher CRI will reduce the barrier, boosting innovation.

The following manuscript has been accepted for publication in the respected peer-reviewed scientific journal LEUKOS. It will be freely available for online download in early 2015.

High Color Rendering Can Enable Better Vision Without Requiring More Power

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Abstract

For many people, the correct perception of the colors of objects is an important part of life, and today it is being threatened by misinformed policy-making and associated business decisions.

Some conservationists and lamp manufacturers have concluded that the accurate color rendering provided by ordinary incandescent lamps is an unaffordable luxury that good citizens should forgo as we employ more energy efficient alternatives. While this is not as extreme as suggesting we should live in cold darkness, it is in the same general direction of deprivation.

Yet research has shown that color rendering is important to people and high efficiency lamps can now also provide high color rendering, so there is no longer any need to have lighting that distorts color appearance. This paper focuses on the tradeoff between color rendering accuracy and lamp efficiency to show that high color rendering accuracy is appropriate and, contrary to a common misconception, does not intrinsically require greater electrical energy consumption.

1 Introduction

Several programs promoting the use of energy efficient lighting products have failed to yield widespread market acceptance because they focus on reducing energy and cost at the expense of quality factors that are important to people; a case in point is the introduction of compact fluorescent lamps into the market [Sandahl et al. 2006]. These quality factors include lamp color appearance (Correlated Color Temperature [CCT]), color rendering (e.g., CIE Color Rendering Index $[R_a]$), color consistency among identical products, smoothness and range of dimming response, and absence of flicker and buzzing. This paper is focused on color rendering, and will use the term " R_a " to refer specifically to the CIE General Color Rendering Index^{iv}. We focus on inadequate

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^{iv} Very often the term CRI is used to mean Ra but that slightly confusing practice will not be followed here, where only Ra will be used to represent the CIE General Color Rendering Index numerical measure for color rendering.

color rendering, not because it is the only barrier to adoption, but because it is an important barrier that, once recognized, can be readily overcome. In terms of lighting application areas, we will be discussing the provision of light for the purpose of general use, recognizing that in certain specialized situations color rendering might be much less important, or much more important, than is typically the case.

Generally, energy efficiency programs will be more successful if they address users' expectations as they promote energy efficient products [Cowan and Daim 2011]. Although energy and environmental benefits and the promise of reduced energy bills are important, they are not the sole drivers in technology adoption decisions. Cowan and Daim [2011] categorized lighting expectations in three behavioral categories that influence these decisions: performance expectations (outcome expectations; fitness for purpose), effort expectations (ease of use), and social influences (norms and image). The likelihood of adopting a new technology increases in the presence of facilitating conditions, such as high energy prices and product compatibility with relevant standards. Experience has shown that programs that focus only on outcome expectations (e.g., lower energy costs or lower maintenance costs) are likely to be unsuccessful in the long run if they ignore other performance expectations. That is a key insight gained from the low adoption rates of compact fluorescent lamps (CFLs).

The importance of reducing energy use for both environmental and economic reasons is clear to all, and with the advent of solid-state lighting (SSL) there are new ways to achieve this. This promising alternative to the low adoption rates of CFLs has motivated many SSL programs aimed at accelerating development, demonstrating technologies and formulating performance standards. There is widespread recognition that only high quality products will deliver the good experiences that are required for broad adoption of these innovative energy-efficient light sources. However we contend, and this paper aims to show, that color rendering has received much less attention in the development of new SSL products than it deserves, in part because of common misconceptions that this paper seeks to dispel. At risk is a valuable, affordable, and traditional human experience – the natural color appearances of objects^v enabled by high color rendering light as produced by incandescent lamps.

It is widely expected that efficient lamps using conventional and/or organic light-emitting diodes (LEDs and OLEDs) will replace the incandescent light bulb. These new light sources are revolutionary and have required substantial research and development on the part of industry and governments. Especially given the very long life of these new lamps, it would be understandable for manufacturers to seek the largest possible share of the first wave of lamp replacement, so there is a business incentive to promote these lamps to consumers and to recoup some of the associated investment costs quickly.

v Throughout this paper, when discussing color appearance, the word "natural" will be used to describe color appearances of known objects which match the expectation of most observers. More precisely, the CIE employs the concept of color rendering, as quantified by the CIE Color Rendering Index, to compare the color appearances of objects under a test illuminant to those under a reference illuminant that is deemed to be the standard for color appearance. The reference illuminant is either a blackbody radiator (similar to incandescent lamps) or a phase of daylight, depending on the source spectral characteristics. Since people are very familiar with the color appearance of objects under these common (and natural) standard illuminants, they often describe these color appearances under these illuminants as "natural".

Unfortunately, most of the currently available high efficiency replacement lamps in the market produce significantly poorer color rendering than incandescent lamps, because, for reasons explained here, improving luminous efficacy of radiation (LER) and color rendering are, to a degree, conflicting goals. LER, measured in lumens per watt, represents the effectiveness with which a given spectral power distribution stimulates the human retina during typical daytime light levels, and this is indeed an important energy consideration. It would be understandable, but also incorrect, to assume that increasing a lamp's LER is the only way to reduce energy use. Possibly this has led manufacturers to prioritize LER over color rendering. As an example, numerous manufacturers are selling LED lamps that are described as "incandescent replacement" lamps even though they do not provide the high color rendering of incandescent lamps. Energy agencies have supported this trend by setting minimum color quality requirements that allow lamps to produce readily apparent color rendering error (e.g., R_a =80 as opposed to R_a =100 for incandescent lamps) [Energy Star 2014]. Lamps with an R_a value of 80 often cause unnatural color appearance of skin, some foods, and other common objects. Some people find the distortion disturbing and it probably bothers many to some extent. We argue that by undervaluing this important aspect of the performance expectation for SSL, this approach, if continued, might not even save energy. Indeed, by impeding the adoption of the most suitable technology, it could cause needless energy wastevi.

Of course, if necessary, people *could* tolerate such inferior lighting, just as they *could* tolerate, for example, having their homes heated to only 10°C (50°F) in winter. But would that be the best plan? We note that instead of being encouraged to shiver in the winter, consumers are encouraged to insulate their homes to save fuel while also *improving* comfort. Similarly, it seems reasonable to expect that modern lamps should save energy while also *improving* the lighting experience. From that perspective, it seems appropriate to critically assess the widespread view that we should now forgo the high color rendering lighting that we have long enjoyed with incandescent lamps.

It might at first seem unreasonable to suggest that respected regulators and manufacturers should reconsider their views on this matter, but this is actually a surprisingly complex topic. It involves three interconnected performance variables – radiant power density (irradiance), luminous efficacy of radiation (LER), and color rendering (R_a), and each of these has a non-linear effect on lighting benefits. Proper optimization in the face of such complexity can be challenging, so understandably people have tried to simplify the issue, accepting illuminance as a given (in the form of illuminance recommendations) and valuing luminous efficacy (as the means to deliver the target illuminance with least energy) while assigning no benefit to having R_a exceed a minimum value of, typically, 80. Sometimes such simplifications can be helpful, giving reasonable answers. But other times (and this is one of them) a reasonable-sounding simplification of the design process yields a problematic outcome. In this

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 $^{^{}vi}$ To be clear, setting a minimum R_a value of 80 does not directly require that such a low value be provided. However it may often indirectly have that effect, because consumers often may not understand the difference, and lighting designers who are trying to minimize energy use while attaining fixed illuminance requirements, may feel obligated to use the most efficient lamps which have lower R_a . Of course there are some settings where, for special effects, low R_a values may be preferred, but the topic for this paper is general lighting. Requiring a somewhat higher R_a value for general lighting need not prevent the use of lower values for special purposes.

paper we correct that understandable error and show an encouraging result: As the title of this paper suggests, it may now be possible to have high color rendering and thus better vision, without using more power.

This paper is intended to accurately cover an important scientific topic using language that is accessible to a wide audience. As such, critics might worry that the treatment is insufficiently technical and does not offer indisputable scientific proof. Indeed it does not – rather, the aim is to offer a strong *plausibility argument* for a *testable hypothesis*. We argue that in an important and meaningful way, color rendering is more valuable to people than illuminance, provided that illuminance is greater than the minimum truly required for the task at hand. We further argue that present-day lighting standards are indirectly leading to inadequate color rendering, and that this problem can be readily solved without increased energy use. We hope this article will motivate further research and deliberation on this important topic.

2 How Light Affects Vision

To state the obvious, there is no vision without light. Indeed, the definition of light is visual: "radiation that is considered from the point of view of its ability to excite the human visual system" [CIE 2011]. Our system of physical photometry is based on the biological functions of spectral luminous efficacy; this is the only physical quantity in the international system of weights and measures that is derived from human capabilities. In calculating how much light one has, one takes the radiometric intensity (irradiance) measured across the wavelength range of the visible radiation spectrum (typically from 380 to 780 nm) and applies a weighting function (usually V_{λ}), summing over the spectrum to determine the quantity available to excite a visual sensation [CIE 2004]. This is well known in lighting circles, but less well known among the general public. This photometric quantity predicts brightness judgments of white light because it is an average over the relevant photoreceptors, but is not as accurate in predicting brightness judgments of colored light, which require specific information about stimulation of individual photoreceptors [CIE 2004].

The photopic weighting function, V_{λ} , used to calculate the quantity of light at levels typical for interiors is shown in Figure 1. In principle, one could obtain a maximum luminous efficacy of 683 lm/W by delivering all of the energy at a wavelength of 555 nm. However, it is well known that such monochromatic (single wavelength) light (similar to that from low pressure sodium lamps) yields no color information. A more reasonable approach might seem to be to make a lamp's spectral power distribution proportional to V_{λ} . One author calculated that a light source with such an output would have a spectral luminous efficacy of 488 lm/W, but an R_a value of only 24 [Murphy 2012]. Neither of these theoretical illuminants would have any market uptake for general lighting because no one wants to live under a green light all of the time. In order for us to perceive the natural color appearance of the objects around us, the light sources we use must deliver radiant power fairly broadly across the visible spectrum. Only those wavelengths emitted by the source and reflected from the surfaces we look at trigger visual responses - although predicting the perceptual response to those wavelengths is more complex than this paper can begin to describe [Boyce 2003; Gregory 1998] and is unnecessary in understanding the arguments presented.

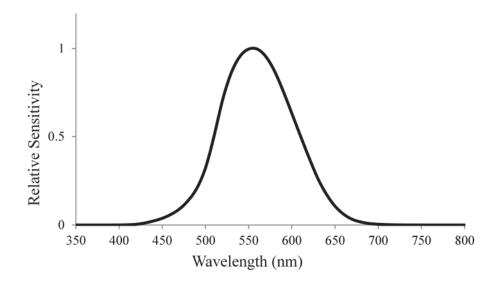


Figure 1. The relative photopic weighting function, V_{λ} .

As mentioned in the introduction, the purpose of this paper is to present a plausibility argument for the hypothesis that people would be significantly more satisfied by illumination having higher color rendering than the minimum presently required, even with the slight reduction in illuminance required to ensure there is no increase in power consumption. The argument requires an *approximate*, but nevertheless *quantitative*, discussion - this is about numbers and the numbers matter. The paper does not present new quantitative scientific information, nor does it summarize the cited previous quantitative research in scientific detail. Rather, it introduces the general quantitative relationship between illuminance and visual perception on the one hand, and color rendering and lamp efficacy on the other.

2.1 The Effect of Light Quantity On Visual Performance

Thanks to a century of investigation, we have excellent models of the effect of the quantity of light on achromatic visual performance. That is, we know quantitatively how our ability to see details will improve if we increase the amount of light available to the eye; the size and contrast of the target also are important parameters [Rea and Ouellette 1991; Boyce and Rea 1987]. These models put numbers to our everyday experience, showing that we can better see objects when they are larger, have greater contrast, and/or have a greater quantity of light falling on them. Importantly, over the range of illuminance levels commonly experienced in interiors, small changes in the quantity of light have very little effect on relative visual performance. The relationship depends somewhat on the target size and contrast and will differ slightly from one normal observer to another, but overall these results provide reliable guidance in setting illuminance recommendations that are high enough to support our visual needs without being wasteful. [DiLaura et al. 2011b].

Figure 2 shows, very approximately, how human angular resolution for a high-contrast target varies with the intensity of illumination for the average person. The primary reference [Shlaer 1937] used to create Figure 2 is an early experiment in which subjects viewed screens with black and white bars having varying visual angular spacing. The size of the finest visible spacing was determined for a wide range of light levels. Although this particular experiment used only a small number of

subjects, it has the advantage of spanning the full relevant range of light levels for this paper, and it uses a very general vision task. Similar information is available in more recent studies [Van Ness and Bouman 1966]. The y-axis of Figure 2 represents the angular size, from the position of the subject, of the finest visible spacing.

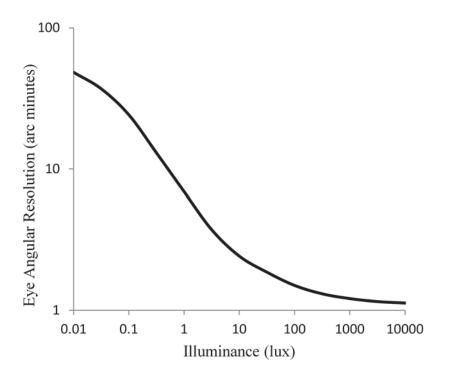


Figure 2. Log-log plot of human eye angular resolution (y-axis) vs. Illuminance (x-axis).

The x-axis spans the million-fold range of illuminance values over which human vision works well. At illuminance levels typically found in offices (often between 500 lx and 1000 lx), human angular resolution is approaching its minimum value of about 2 arc minutes, which corresponds to excellent vision. The chart shows that the eye angular resolution grows as illumination diminishes, but this happens very gradually - as the illumination decreases by a factor of a thousand, the angular resolution increases by only a factor of ten!

2.2 Color Rendering and Visual Performance

The human visual system also differentiates between spectral channels in the radiant energy it detects. We describe these perceptions as colors. Most humans are able to distinguish very fine color appearance differences [Wyszecki and Stiles 1982]. Artists and designers understand that the nuances of color appearance are a really important part of life. Indeed, considering how much time, effort and money is devoted to color perception in areas such as clothing, paints, inks, cosmetics, foods, ornaments and visual media, it is clear that color perception matters a great deal to many people. Put another way, color perception is an important component of visual perception overall.

It is interesting to consider why humans may have evolved such a sharp sense of color. Biologists generally believe that wavelength sensitivity evolved for basic survival

reasons [Pinker 1997]. Color vision would have helped our ancestors to choose non-poisonous berries, fresher food, and cleaner water, and to recognize fertile soil, a clear sky, a healthy mate, and so on. Perhaps it is not surprising that today, the emotional impact of color appearance and its design are, for many of us, an extremely important part of life. [Palmer, S. E., & Schloss, K. B. (2010), Gibson, J.J. (1977), Mollon, J. (2003)]

Of course, it would be incorrect to assume that under all circumstances people prefer illumination that produces natural color appearance in objects. An obvious counter-example is theatrical lighting, which is often used to create unnatural color appearances for dramatic effect. Also, it has been observed that more subtle distortions of color appearance, in which color saturation is mildly increased, are sometimes chosen in certain comparisons. Nevertheless, the fact remains that color perception has the practical purpose of providing us with useful information about some properties of illuminated objects, by comparison to previous observations. For that to work well, it is important that the illumination present during previous observations rendered colors in the same way as the current illumination does, which is more or less the definition of high color rendering^{vii}.

Furthermore, researchers have recently begun to examine the additional contribution that color perception makes to visual performance [O'Donell and Colombo 2008; O'Donell et al. 2010]; previously, it was generally assumed that at typical interior luminance levels, color perception would have little effect on visual performance. However recent research suggests that this is only partly true [O'Donell et al. 2011]. When luminance contrast is high (> ~60%) then chromatic information adds little to visual performance. However, when luminance contrast is very low (below ~20%), color perception makes visual performance possible; otherwise it would approach zero. This effect depends on the chromatic characteristics of the stimuli. In between 20% and 60% luminance contrast, both luminance and chromatic contrast contribute to visual performance. Although the specifics of this model await independent validation, the empirical evidence is clear: chromatic information matters. It might matter particularly to people with certain visual aberrations, such as those that reduce luminance contrast (e.g., cataracts), in which case ensuring good color rendering could be especially beneficial.

2.3 Color Vision and Illuminance

Another important consideration is the illumination-level-dependence of color vision sensitivity – that is, the ability to detect color appearance differences between objects. There is surprisingly little research on this well-known effect, but at least two experimental studies show that observers can detect smaller color appearance differences at higher illuminance levels [Baah et al. 2012; Huang et al. 2011]. This effect is depicted in Figure 3, which shows the approximate dependence of color appearance uncertainty on illuminance. Color appearance uncertainty (left y-axis) is the size of color appearance difference of two nearby objects that is required to ensure

vii There may be specialized circumstances where an important object property may best be studied using a very low CRI lamp that distorts colors in a way that makes a distinction more obvious. In such cases, the same low CRI lamp would also be used to obtain the reference information that would guide the comparison. The value of high CRI lighting is that we can use, as reference information, a great deal of previous color observations that occurred in the context of high color rendering incandescent lighting.

that the average observer would be able to perceive that they do not have the same color appearance, expressed in CIELAB [Fairchild 2005] units. Also shown, on the right y-axis, are related values for the CIE General Color Rendering Index value, R_a.

The values in Figure 3 were estimated by means of CIECAM02 [Fairchild 2005], the most recent widely adopted color appearance model approved by the CIE, and calculated using a publically available CIECAM02 spread sheet calculator [Fairchild 2008]. CIECAM02 was designed to match a wide range of color appearance data, including the Hunt effect [Fairchild 2008], whereby the non-linear response characteristics of retinal photoreceptors causes a reduction in color sensitivity as illuminance is decreased. At the various illuminance levels in Figure 3, the CIECAM02 calculator was used to determine how large a color appearance change in CIELAB space was required to cause a 1-unit change in CIECAM02, which is approximately a just noticeable difference in that space. Due to the Hunt effect this value increases as illuminance decreases. The right y-axis of Figure 3 depicts the R_a values for which the mean color rendering error associated with that value matches the color observation error shown on the left y-axis. The current R_a model is based on a slightly different measure of color difference than CIELAB, but an approximate connection can be derived from recent studies [Davis and Ohno 2005] showing that the R_a value is approximately 100 minus 3 times the mean CIELAB color error. This is the basis upon which the right Y axis values have been matched with those on the left Y axis.

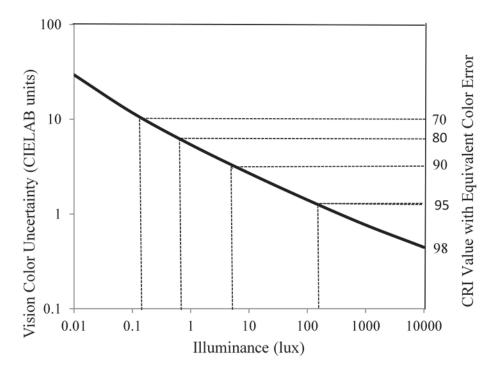


Figure 3. Log-log plot of visual color uncertainty (left Y axis) and R_a value with equivalent color error (right Y axis) vs. illuminance (X axis).

3 Light Source Color and Color Rendering

As lighting professionals know, both the color appearance of a light source itself *and* its color rendering quality depend on its spectral power distribution, (which is the

relative amount of radiation at each wavelength of the visible radiation spectrum) and importantly, they depend on it *very differently*. Because of this different dependence, two light sources can have the *exact same* light color, yet *very different* color rendering properties. Figure 4 shows the spectral power distributions of two familiar white light sources that appear to have same light color. The incandescent source has an R_a value of 100. The compact fluorescent lamp has a very different R_a value of 80. Despite their matching light color, the different spectral power distributions produce quite different color appearances for some of the objects they illuminate [CIE 1995].

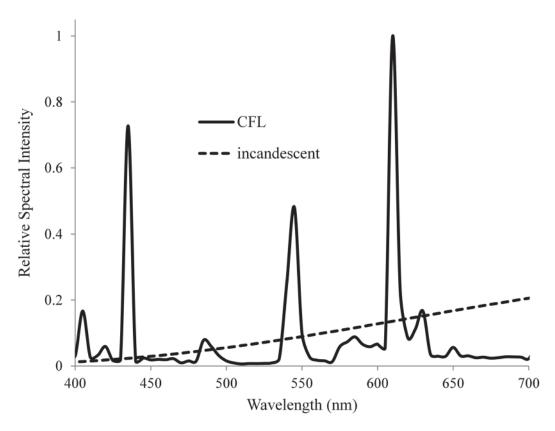


Figure 4. Spectral power distributions of an incandescent and a compact fluorescent lamp.

This distinction may be important to the adoption of new lighting technologies because people generally prefer light sources that give their surroundings the appearance they have come to value and expect. Surprisingly, only one study seems to have examined consumers' beliefs about light source color rendering as an influence on CFL uptake: Beckstead and Boyce [1992] found that people who believed that "fluorescent lighting makes your skin look an unnatural or funny color" were less likely to adopt CFLs. Recent utility surveys and consumer focus group studies concerning SSL uptake [Sandahl et al. 2006] have focused on the light source color and its consistency from one product to another (lack of color consistency is a barrier to adoption) but have not questioned people as to whether their décor, their food, or their faces, have a natural color appearance under various light sources.

4 The Relative Importance of Illuminance and Color Rendering

We have the opportunity today to choose from an almost unlimited range of possible light source spectral power distributions, and the associated optimization problem actually has been familiar to manufacturers for decades [Schanda 1981]. Put simply, there is a fundamental trade-off between the color rendering and LER for a light source. This is because, as shown in Figure 1, the sensitivity of the human eye decreases for wavelengths near either end of the visible spectrum (blue and red). As a result, lamps that emit little power at those extreme wavelengths produce more lumens per watt. However, using such lamps also causes color distortion because of the missing wavelengths; that is they have lower color rendering. An R_a value of 80 might seem like a good choice, because such a lamp typically has a 15% higher LER value than a light source with an R_a of, say, 95 (i.e., for the same power it provides 15% more visible light). While this might at first seem like a sensible choice, the arguments below indicate otherwise.

Appendix A explains, in simple terms, how over-simplified decision-making often leads to poor optimization decisions, and describes a common-sense approach for avoiding this. Anyone who feels unsure about this is encouraged to read that appendix. Its main point is that in order to make good decisions, it is important to assign the appropriate relative importance to the various desirable features. For illumination, the key issue is the relative importance of luminous efficacy and color rendering, from the perspective satisfying human needs. We provide a simple example here to illustrate the point:

Consider a room with good lighting for almost any visual task – an illuminance of 1000 lx and a CIE Color Rendering Index value R_a of 100 (i.e., perfect color rendering). The information in Figures 2 and 3 shows that this condition gives ideal visual acuity and color discrimination. A subject spends about half an hour doing some visual tasks in the room, then walks outdoors for a while and returns to continue with the same tasks. While away, unbeknownst to the subject, either the illuminance or the color rendering of the light is reduced. How sensitive would you expect a subject to be to such changes in the lighting of a room? The answers, which are well known to lighting designers, reveal the relative importance of illuminance and color rendering in terms of human perception. First, consider changes of illuminance, with the color rendering index R_a value kept at 100.

4.1 Decreasing Illuminance

If, between observations, the illuminance is reduced 20%, (from 1000 lx to 800 lx), almost no one will notice the difference and it would be virtually impossible to measure any decrease in visual acuity or color discrimination. If reduced 60%, (to 400 lx), few will notice and almost no one will care. If reduced 80%, (to 200 lx), most people will notice and care slightly, and it could be possible to measure a small decrease in visual acuity [Rea and Ouellette 1991] and color discrimination [Baah et al. 2012; Boyce and Simons 1977; Huang et al. 2011]. The widely observed truth is that such large decreases in illuminance cause only very slight reductions in visual acuity and color acuity, to the extent that they are often very difficult to observe at all. This is consistent with Figures 2 and 3, which show that big illuminance changes cause only modest changes in vision. Put simply, people are remarkably *insensitive* to changes in illuminance levels. Next, consider the very different situation in which illuminance is held at 1000 lx and the color rendering index R_0 value is reduced:

4.2 Decreasing Color Rendering

If, between observations, the R_a value has been reduced 20 points (from 100 to 80), some may say the lighting is less pleasant, and for almost all observers it will be possible to measure increased color discrimination errors [Boyce 1977]. If reduced 60 points (to 40), almost everyone will be uncomfortable and some will feel very uncomfortable. Under such light, people look like corpses, food looks rotten, and essentially only shades of grey look normal. This shows that, in stark contrast to our weak sensitivity to illumination levels, we are very sensitive to color distortion. This makes sense from an evolutionary perspective - typically natural light has a highly variable illuminance level but fairly constant high color rendering, so our highly sensitive sense of color, combined with our great tolerance of illuminance changes, would have been quite advantageous.

The results in these two cases are not particularly surprising, considering that the value of R_a is calculated by subtracting, from 100, a measure proportional to average color rendering error [CIE 1995]. This means that an R_a value of 60 (i.e. 40 points below 100) corresponds to *twice* the color distortion present with an R_a value of 80 (which is only 20 points below 100). Similarly, an R_a value of 40 has *three times* the color distortion present for an R_a value of 80. Often people are surprised to learn that R_a is calculated in this way, perhaps because of the common misconception that the R_a value represents a percentage of something, which it most certainly does not.

There is also an intriguing connection between color rendering and spatial perception research. Both spatial and temporal luminance patterns can cause discomfort and, in susceptible individuals, can provoke migraine and epileptic seizures [Wilkins 1995]. Fourier analysis of images shows that the spatial frequency pattern of natural images follows a 1/f function of higher amplitudes at lower spatial frequencies. Uncomfortable images show disproportionately high amplitude at spatial frequencies peaking somewhere between 1 and 3 cycles/deg [Fernandez and Wilkins 2008; O'Hare and Hibbard 2011]. This work has been extended to confirm that visual discomfort increases when one looks at an image whose statistics deviate from those of natural images in terms of both luminance and color contrast [Juricevic et al. 2010]. Although to our knowledge, this work has not been extended to include distortions in color appearance associated with light source color rendering, the evidence that there are perceptual preferences for naturally occurring images leads to the inference that we should tread cautiously in planning widespread application of long-life light sources that would immerse the population in potentially uncomfortable circumstances.

To summarize, the key point is that fairly large fractional decreases in light level are insignificant to most people, yet fairly modest decreases in color rendering may be quite disturbing. Roughly speaking, we estimate that a decrease of R_a from 100 to 80 (20 points) is about as significant as a decrease of illuminance from 1000 lx to 400 lx (60%), based on the comparison of the information in Figures 2 and 3. This shows that, generally, changes in color rendering are much more important to people than changes in illuminance. Let's now consider how to apply this type of thinking to make the best trade-off, for people, between efficiency and color rendering.

5 Quantifying the Efficiency versus Color Rendering Trade-off

Figure 5 shows the R_a , LER combinations for a number of light sources available today [Ohno 2013], along with the theoretical limit for possible future sources [Hung and Tsao 2013]. Two of those light sources have been selected to demonstrate a typical

trade-off in R_a and LER between them. One of the light sources (A) has an R_a value of about 94 and LER of about 308 lm/W. The other light source (B) has an R_a value of about 84 and an LER of about 362 lm/W.

Lamp B produces about 17% more light per watt of radiation than lamp A, at the cost of a 10 point reduction of R_a , corresponding to a 2.7-fold increase in color distortion. Based on the preceding discussion of the relative importance of color rendering, it is likely, in this example, that people will find lighting based on lamp type A preferable to using the same amount of power with lamp type B to produce a little more illuminance with much lower quality.

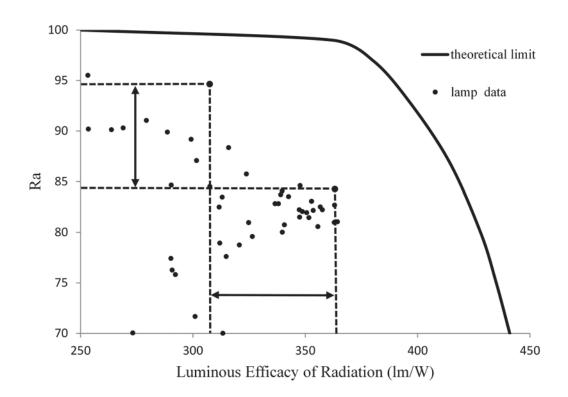


Figure 5. CRI R_a value vs. Luminous Efficacy of Radiation (LER)

It is important to emphasize that in this comparison the energy use for the two lamp types is identical; *no more energy is used* with lamp type A. For the same amount of radiant power, lamp type A will give 17% fewer lumens – a difference no one can notice – while reducing color error by a factor of 2.7, which many will value. Put simply, when people prefer something, (such as in this example lamp type A), it is generally because it provides more overall human value. In this sense, Lamp A provides more human value for the energy than does lamp type B. From this perspective, choosing the seemingly more efficient lamp B would actually be wasteful.

6 Overcoming Objections to High Quality Color

The aim of this paper has been to make the conclusions seem reasonable and straightforward. For readers who agree with this reasoning, it may seem puzzling that

some well-intentioned people cannot seem to accept any argument for using a lamp with an R_a of 95, when a lamp with an R_a of 80, from one perspective, is more "efficient", and when many people are not consciously aware of the poorer color rendering at an R_a of 80. But this argument is no different than concluding that office light levels should be only 100 lx, not 500 lx, because people can easily work at that lower illuminance level and many would not be bothered by the reduced illuminance. Both of those design approaches would fail to maximize human value. To properly optimize lighting design, it might be best for society and/or consumers to first decide how much power should be used for electric lighting in a given situation and, subject to that constraint, determine what form of light will provide most value, overall, for people. From this perspective, the question "What is the most appropriate CRI R_a value?" is absolutely not an energy issue – it is a human value issue. The only meaningful question is, "What CRI R_a value enables people to get the greatest overall value from their lighting expenditure?"

In this regard, another objection to properly valuing color rendering is that the current method for evaluating it, (the CIE Color Rendering Index), is not perfectly accurate, and improvements are in the process of being made. However, for the fairly high color rendering lamps that are the topic of this paper, the errors in question are small and they therefore do not detract from the overall reasoning. (To hold back for this reason would be somewhat like eliminating automotive speed limits because speedometers aren't perfectly accurate.) The CRI is sufficiently accurate to support the arguments presented in this paper and in any event the anticipated improvements should be available soon [Smet 2013]. Another article in this Leukos issue provides more information about the CIE Color Rendering Index and its future [Smet et al. 2014].

Probably the only way to fully resolve these issues to everyone's satisfaction will be to carry out exhaustive experiments in which people compare equal-power options ranging from higher illuminance levels with poorer color rendering to lower light levels with better color rendering, to determine what point along the trade-off they value most. An international collaboration is now preparing to commence this long-overdue research, and based on the kinds of preliminary observations described above, certain results are anticipated with high confidence. One of these is that the level of illuminance matters. At higher illuminance levels, which are used when visual tasks demand them, as shown in Figure 3, people are more sensitive to color error, so color rendering will matter more and therefore the optimal value for R_a will be higher. For offices and bright regions in homes, with illuminance values around 500 lx, the authors of this paper anticipate that the preferred value for R_a will be about 95. For bright nighttime outdoor lighting, with an illuminance of about 20 lx, it is expected to be about 85, and for dim nighttime outdoor lighting, with an illuminance of about 5 lx, probably about 80 will be an optimal value.

The adoption of such R_a values need not cause any power consumption increase in most settings compared to present-day practices; indeed, there is the possibility of power savings. In office settings, illuminance preferences with fluorescent lamps have been found to be lower when color rendering is greater [Boyce 1977; Fotios and Levermore 1997]. Already, the outdoor lighting standard in the UK permits an illuminance reduction when the light source has $R_a > 60$ [Fotios and Goodman 2012]. Again, this is intrinsically a power-neutral decision, and the resultant increased satisfaction will likely accelerate adoption of LED technology, thereby accelerating energy savings that are badly needed.

There is one additional possible argument against high color rendering lighting – that it might cost more. However new entries in the marketplace are indicating otherwise. For example, the California Energy Commission recently set a minimum R_a requirement of 90 for LED lamps to qualify for energy rebates [CEC 2013], and recently at least three omnidirectional commercial lamps are listed in that R_a range [US DOE 2013] in the same general price range as lower CRI lamps.

Above all, it is critical to understand that higher color rendering does not intrinsically require more power, because higher color rendering lamps produce light that works better for people, and therefore fewer lumens are needed to achieve the same human value. To incentivize such proper design, lighting codes should call for both appropriate power densities and the optimal combination of color quality and luminous efficacy. This could include setting slightly reduced illuminance requirements for higher color rendering light, to ensure that the resultant significant improvement in lighting value can be achieved without increasing power consumption.

7 Conclusion

Overall, it is clear there is now no significant barrier preventing the use of truly high quality, energy efficient LED lighting in our homes, offices, schools, stores, streets, or factories. Therefore, it is time to urge regulators and manufacturers to pursue excellent human value in lighting as the best way forward for both human well-being and energy efficiency. Likely, regulators will respond favorably to further research firmly establishing this idea; such work is strongly recommended. In the long run, everyone will benefit from high color rendering standards for our light, just as we have already benefited from high quality standards for our food, water, and air.

Appendix A: Making Optimal Trade-off Decisions

This appendix describes the conceptual issues present in decisions that involve tradeoffs between two or more performance parameters. Non-experts and experts alike make common, but avoidable, mistakes in such matters. The issues are similar for all such trade-off decisions, so we begin with a familiar everyday example: A person has decided to spend a certain fixed amount of money to buy a house. For simplicity, imagine that there are just two factors that matter to this purchaser in this case. They are (1) the size of the house and (2) the number of useful services close to it. There is a trade-off between those two factors, because with the fixed amount of money available, it is possible to buy a large home in a remote suburb with few services nearby, or a small house in a very well-serviced neighborhood, but the combination of the two is unaffordable. Thus, there is a need to compromise between these extremes and the key question is how to determine the best compromise.

To find this, it is necessary to understand how the purchaser's overall enjoyment of a house will depend on these two desirable features. Ideally, the purchaser would have a chance to try out various affordable combinations of these features, in order to find the most appealing available combination. Failing that, one could study and take into account the experiences others have had in making such decisions. These would be reasonable approaches, but trying out many combinations is impractical for most individuals, and obtaining the information about a range of other people's experiences is difficult.

Consequently, people often use a method that is much simpler, but which has significant shortcomings. One could call this the "sequential choices" method, and it comes in two equivalent approaches, each being the reverse of the other. In this example they are:

- (A) The purchaser first chooses the smallest house size they can tolerate living in, and then purchases such a house in the best-serviced neighborhood in which that house size is affordable.
- (B) The purchaser first chooses the least-serviced neighborhood they think they can tolerate living in, and then within that neighborhood they purchase the largest house they can afford.

Both of these "sequential choices" are easy to follow because they are methodical and fast. That is, first you choose the required minimum value for one of the two desirable factors, significantly reducing the number of possibilities to consider, and then from that smaller set you choose the option which is best according to the second desirable factor. Unfortunately, as depicted in Figure A1, this easy method generally yields poor decisions. One way to see this is that approaches A and B almost always give different answers. Worse, there are usually significantly better choices that are overlooked by this simplistic approach. Unfortunately, as described below, it is precisely the method that was used in the past for making the luminous efficacy and color rendering tradeoff decision.

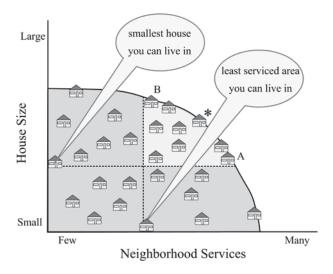


Figure A1. This graph plots houses you can afford (black squares) according to the size of the house (y-axis) and the number of nearby services (x-axis).

The curved line in Figure A1 depicts the "boundary of affordability" – houses above and to the right of it are priced beyond your reach. The lighter gray zone contains houses that would be tolerable for you, because they exceed your minimum required size and also your minimal services requirement. The question is which house is the *best* choice for you. Using method (A) you would first choose the smallest house size you can tolerate living in and then find the best serviced neighborhood where houses that size are affordable; yielding the house marked "A" in Figure A1. Alternatively

using method (B) you would first choosing the least well serviced neighborhood you can tolerate living in and then finding the largest house you can afford in that neighborhood, yielding the house marked "B" in Figure A1. Likely, neither is the house in which you would be happiest –the optimal choice is probably somewhere in between, such as the house denoted with a star in Figure A1.

Consider another example involving decision-making while designing a car. It is desirable for a car to be *both* attractive *and* inexpensive. Following the "sequential choices" approach described above, one could first determine a "reasonable minimum level of attractiveness", and then design the least expensive car based on that constraint. The result might look like the car in Figure A2a. Instead, if a manufacturer explores the range of possible combinations of attractiveness and cost, it is usually found that with a very modest added cost, a much more attractive design is possible, resulting in greater overall value for the consumer, as depicted in Figure A2b.

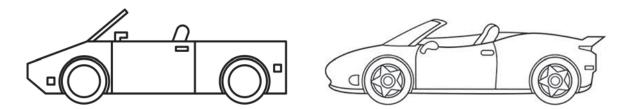


Figure A2 Cars with (a) lowest acceptable attractiveness and (b) highest overall human value per dollar

In our society, the free market has ensured that manufacturers who take the more enlightened optimization approach stay in business. As a result, cars look more like Figure A2b than Figure A2a, which is more reminiscent of vehicles that were produced in communist or fascist countries where human preference was not usually considered an important factor (e.g., the Ladas produced in the 1980s in the USSR).

For good reasons, free market forces don't entirely apply to light bulbs; energy regulators are empowered to make certain design decisions on our behalf. Unfortunately for everyone, energy regulators might not make the optimal choice for overall well-being, if by using the sequential choices method they prioritize one dimension of the decision (in this case, LER) over the other (CRI). To help make this clearer, consider two fictional examples where energy regulators could inadvertently make the "sequential choices" mistake:

- 1. People drink a lot of soda pop, which often contains a lot of sugar made from corn, and corn farming consumes a lot of fuel. Production of artificial sweeteners requires less fuel. Imagine how citizens would feel if regulators banned sugar in pop, requiring instead that manufacturers use only artificial sweeteners, in order to reduce farm fuel use. Their justification might be that "most people say artificial sweetener tastes OK".
- 2. Consider the use of power in home audio systems. It is well known that people are less sensitive to low bass and high treble tones. Imagine regulators banning such frequencies, in the hopes of marginally reducing home audio power consumption. The justification would be "only musicians and sound studios really need to hear low bass and high treble".

Of course those examples sound absurd, but they demonstrate the fallacy of "sequential choices" optimization. Unfortunately, it seems that this sort of simplistic reasoning has been applied to the trade-off between efficiency and color rendering for light sources.

On that topic, a compromise approach could be to average these two extreme approaches: First, identify the minimum value for R_a that most people will tolerate in their homes, and then based on that value (about 84), design the spectral distribution function that has maximum LER subject to that constraint. Second, and no less reasonably, identify, for a standard electrical power budget, how low a value of LER (and hence lower illuminance) people will generally tolerate, and within that constraint, maximize R_a , which would give a result close to 100. Just as in the house purchase example above, these two approaches yield different answers and both would fail to provide people with the best compromise. However, the average of these two approaches could be close to the optimum – suggesting an R_a value of 92. We hope that upcoming research will be able to establish this unequivocally.

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