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Vertical Plume Velocity Assessment

# SVY Backup Generating Facility

San Jose, California

Submitted to  
California Energy Commission

Submitted by



Prepared by  
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ATMOSPHERIC DYNAMICS, INC  
Meteorological & Air Quality Modeling

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## Introduction

This report presents the evaluation of the STACK Infrastructure Backup Generating Facility (SVYBGF) thermal source generated plumes from the 36 Caterpillar diesel engines and 72 rooftop chillers on the effects on airport/aircraft operations. The Normal Y. Mineta San Jose International Airport is located approximately 3.1 miles southwest of the SVYBGF. This report is based upon an analysis prepared by Atmospheric Dynamics, Inc. in accordance with the California Energy Commission (CEC) application requirements for a Small Power Plant Exemption (SPPE) pursuant to the power plant siting regulations. This analysis is but one part of a larger analysis, which seeks an SPPE Decision from the CEC.

Based on the stack parameter data, an analysis of the potential plume characteristics from the routine operation the diesel engines and rooftop chillers on vertical winds was prepared and compared to the California Energy Commission (CEC) significance criteria of 5.3 meters per second (m/s) for the average vertical plume velocities as described below.

Atmospheric Dynamics, Inc. (ADI) prepared a screening level plume vertical velocity assessment which are based on the calm wind Spillane methodology outlined in the *“Aviation Safety and Buoyant Plumes”* paper (Peter Best, et. al., presented at the Clean Air Conference, Newcastle, New South Wales, Australia, 2003). This methodology is also recognized as a screening tool for aviation safety set out by the Australian Civil Aviation Safety Authority (CASA) and presented in *“AC 139-5(1) Plume Rise Assessments (CASA, 2012)”*.

The aim of this screening assessment is to conservatively determine the potential for turbulence generated by the diesel engines and rooftop chillers waste heat exhaust plumes. Part 139.370 of the Australian Civil Aviation Safety Regulations (1998, 2004) provides that CASA may determine that plume velocities in excess of 4.3 m/s is or will be a potential hazard to aircraft operations. The *Manual of Aviation Meteorology* (Australian Bureau of Meteorology 2003) defines severe turbulence as a vertical wind gust velocity in excess of 10.6 m/s. The assumed critical vertical velocity used as a CEC significance threshold is 5.3 meters per second\* (m/s) but it should be noted that the basis of the original CASA derived threshold of 4.3 m/s has been lost in antiquity and that CASA no longer relies on the 1998 and 2004 regulations that established this critical threshold other than to note that a more rigorous analysis, which includes site specific meteorology, should be used if the 4.3 m/s and 10.6 m/s screening thresholds are exceeded. The screening method uses absolute worst-case assumptions of calm winds and neutral atmospheric conditions for the entire vertical extent of the plume to determine these worst-case impacts. It should be noted that these results are extremely conservative in that these worst-case conditions typically only occur during a few hours each year.

The Spillane methodology is generally applied to a limited number of plume source geometry's (turbines, power plant boilers, etc.) with the stacks arranged linearly (in a single straight-line) and separated by distances that typically exceed the individual stack diameters. For the diesel engines, this assumption was maintained. Only one engine stack was modeled consistent with the normal operational testing schedule of the emergency generator engines. For the chiller assessment, a conservative assumption was made in order to use the Spillane methodology on an atypical chiller plume configuration, which is made up of 72 chillers arranged on a two-dimensional surface. Here, the methodology, as described below, assumed that all 18 chiller cells for each chiller were merged into a single stack with an effective diameter based on the combined area of all 18 chiller cells, which was calculated to be 3.66 meters. In other words, a single stack

\*For the Puente Power Project (Docket#15-AFC-01, TN#213674, 9/15/2016), “CEC staff ... concluded that an average velocity of 5.3 m/s is the appropriate velocity ... [for a plume velocity threshold].” The CEC staff “Plume Background Threshold” attached to the docketed document concludes with “...[CEC] staff will use 10.6 m/s peak vertical plume velocity as the new threshold. The altitude at which a plume would have a peak vertical velocity of 10.6 m/s would be the same altitude at which a plume would have an average vertical velocity of half that, 5.3 m/s.”



was assumed to initially describe the release parameters of the combined chiller cells in each of the 72 individual chillers. The effective plume diameter is appropriate for each individual chiller based on the close proximity and arrangement of the 18 chiller cells.

### Screening Methodology and Vertical Plume Velocity Calculations

The Spillane methodology is based on worst-case calm wind neutral stability conditions to assess the average plume vertical velocity as a function of height. The methodology is based on well-verified laboratory and theoretical treatments of the rise and spread of a buoyant jet, both into a still ambient environment and into a light crosswind. This treatment covers in detail the initial dynamics of the plume as it exits the stack and the entrainment of ambient air into the plume as it rises directly above the stack. In addition to providing clarifications and algebraic solutions to the Spillane methodology, the 2003 Peter Best paper provides additional methodologies that also consider the enhancement of vertical velocities that may occur if the plumes from multiple identical stacks merge and form a higher buoyancy combined plume (referred to here as the enhanced Spillane methodology).

The vertical plume assessment will involve several stages of development. For individual plumes, the stages are:

- (a) In the first stage very close to the stack exit, the high plume momentum will result in a short section in which the conditions at the center of the plume are relatively unaffected by ambient and plume buoyancy conditions. This jet phase extends from the stack exit to approximately a distance of  $6.25 D$  above the stack (where  $D$  is the stack diameter) in calm conditions. At the end of this stage, the plume-averaged vertical velocity has decreased to half of the stack exit velocity, with a corresponding increase, or doubling, in effective plume diameter.
- (b) In the second stage, the plume responds to differences between ambient and plume buoyancy conditions, with much cooler and less turbulent ambient air being entrained into the plume from the outside regions of the plume towards the plume centerline. The momentum and buoyancy of the plume significantly influences plume rise and subsequently the dilution of the stack exhaust to decrease plume vertical velocities. This dilution is very sensitive to ambient wind speed, so the calm wind conditions considered here are extremely conservative.
- (c) In the third stage of plume development, plume rise is due entirely to the buoyancy of the plume and continues from some distance until there is an equalization of turbulence conditions within and outside the plume. This final rise is often only achieved at considerable heights/distances from the stack where the effective average vertical velocity is then close to zero. Since there is very little turbulence and near-zero vertical velocities, this stage of plume development is usually not considered for this type of analysis.

In the second stage of development, the analytical solution of the governing equations under these conditions is given by:

$$a = 0.16(z - z_v)$$
$$V = \{(Va)a^3 + 0.12Fo [(z - z_v)^2 - (6.25D - z_v)^2]\}^{1/3} / a$$



Where the subscript 'o' refers to values of the parameters at the stack outlet and the variables are:

$a$	plume radius (m)
$V$	average vertical velocity (m/s)
$z$	height above stack top (m)
$z_v$	virtual source height (m)
$D$	stack diameter (m)
$F_o$	buoyancy flux evaluated at the stack outlet ( $m^4s^{-3}$ )

These are the two primary equations governing the growth of a single plume in the second stage of development under neutral calm wind conditions. Additional equations governing the first stage of single plume development as well as the interaction of multiple plumes in the second stage of development are discussed in detail in the Best paper.

For multiple stacks in the enhanced Spillane methodology, the equations governing the second stage are calculated from the point when the plumes begin to merge until they are fully merged. The plume merging begins at the height where the plume diameters equal the stack separations and the plumes are fully merged at the height where the plume diameters are equal to  $2d(N-1)/2$  for three or more stacks or  $2d$  for two stacks. At the fully merged height, the merged plume diameter and velocity is enhanced by the fourth root of the number of stacks. Above the fully merged plume height, the enhanced plume diameter and plume velocities follow the regular equations given for the second stage. Below the fully merged plume height for the merging phase, plume velocities are linearly interpolated by height from the single plume velocity at the height where the plumes begin to merge to the enhanced plume velocity at the fully merged plume height.

### **Vertical Plume Velocity Calculations for the Diesel Engines**

The SVYBGF is comprised of 36 individual large and three (3) small diesel emergency generator stacks. The small diesel emergency generators were not assessed as it would have smaller plume vertical velocities. Generator stack parameter data (plume exit velocity, plume exit temperature and stack exit diameter) were provided by Caterpillar. Only one (1) engine will be tested during any one hour. While the engines will be tested at minimum loads, the 100 percent load case was utilized for the worst-case plume analysis. For the engine analysis, two ambient conditions were considered: 41.0°F, the minimum monthly mean of daily minimum temperatures, and 84.3°F, the maximum monthly mean of daily maximum temperatures for the San Jose Airport (*"Climatology of the United States No. 81 – Monthly Station Normals of Temperature, Precipitation, and Heating and Cooling Degree Days 1971-2000 – California"*, February 2002, and *"Climatology of the United States No 20 – Monthly Station Climate Summaries, 1971-2000 – California"*, February 2004). These data are summarized in Table 1.



Table 1 Cummins Diesel Stack Characteristics for Vertical Plume Velocity Analysis			
	Case #	1	2
Ambient Temperature (°F)*		41.0	84.3
Stack Diameter (m)		0.5080	0.5080
Exhaust Velocity (m/s)*		53.10	53.10
Exhaust Temperature (K)*		766.48	766.48
Stack Release Height (m)		18.59	18.59
Stack Buoyancy Flux (m <sup>4</sup> /s <sup>3</sup> )		20.18	20.18
*Stack data provided by Caterpillar at 100% load with SCR/CO Catalyst			

Screening level vertical plume velocity assessments were made for two ambient temperatures with calm winds and neutral atmospheric conditions for the cases presented in Table 1 which are based on 100 percent load. The results based on the two ambient conditions are presented in Table 2 and the output from the calculation spreadsheet provided in Attachment A.

The initial jet phase extends to a height of about 71.4 feet above grade level (ft-agl) for both cases. After the jet phase, plume temperature buoyancy characteristics modeled in the Spillane methodology cause a uniform decrease in plume-averaged vertical velocities, with the critical plume-averaged vertical velocity of 5.3 m/s occurring at about 103 ft-agl for both cases

Table 2 Diesel Engine Vertical Plume Velocity Analysis Results for Reference Height			
	Case #	1	2
Ambient Temperature (°F)		41.0	84.3
Single Plume Results:			
Plume-Averaged Vertical Velocity at 200 feet-agl (m/s)		2.58	2.54
Height of 5.3 m/s Plume-Averaged Vertical Velocity (feet-agl)		102.0	102.6

These screening results indicate that mechanical and thermal turbulence levels due to the flow from the diesel engine always remain in the light turbulence category and below the significance level of 5.3 m/s at all heights above about 103 ft-agl. Even light wind speeds can dramatically decrease the predicted plume-averaged vertical velocities, so the above results are very conservative indications of adverse conditions. The important factor for a given location is the appropriateness of available information for estimating true wind and temperature profiles throughout a typical year. Theoretical calculations, as shown in the tables above, are likely to overestimate the expected vertical velocities, for the following reasons:

- The wind profile is assumed constant with height with no occurrence of wind-shear when realistically, there is a considerable variation with height, especially in light winds;
- Worst-case scenarios are based on very light-wind, near-neutral atmospheric conditions with maximum loading.

### Vertical Plume Velocity Calculations for the Rooftop Chillers

The 72 rooftop chillers are each comprised of 18 individual cells, each with a cell fan diameter of 34 inches. The two data center buildings have different chiller arrangements as is presented in Figure 1. SVY05 is comprised of 30 chillers with SVY06 comprised of 42 individual chillers. The 42 chillers on SVY06 have a larger capacity (295.7 tons) and fan airflow (257,143 ACFM) than the 30 chillers on SVY05 (276 tons and 240,000 ACFM). As the potential for combining the two data



center plumes is not possible, SVY06 with the larger air flow and larger number of chillers was used to assess the chiller plume velocities. The 42 chillers on SVY06 are generally arranged in rows of six (6) along the longer building length (averaging 24.5 feet between adjacent chillers) by eight (8) along the shorter building width (averaging 15 feet between adjacent chillers). Based on the groupings of chillers, the single and merged plumes were based on the 42 (6x8) chiller arrangement by merging plumes along the length (6 merged stacks) and width (8 merged stacks). Chiller stack parameter data (exit velocity and temperature) were provided by the applicant. An effective stack diameter for all 18 cells of 3.66 meters was utilized for each chiller. The chillers will utilize variable speed fans and the number of fans that are operational are dependent upon ambient temperature and plant load. However, to be conservative, all chillers/cells were assumed to be operating at full load. These data are summarized in Table 3 for the same ambient temperatures used for the engine analysis.

Table 3 Chiller Stack Characteristics for Vertical Plume Velocity Analysis			
Case #	1	2	
Ambient Temperature (°F)*	41.0	84.3	
Effective Stack Diameter (m)**	3.66	3.86	
Exhaust Velocity (m/s)*	11.51	8.06	
Exhaust Temperature (K)*	289.26	313.32	
Stack Release Height (m)	24.38	24.38	
Stack Buoyancy Flux (m <sup>4</sup> /s <sup>3</sup> )	14.56	13.43	
*Chiller stack data provided by the applicant			
** Calculated value based on the cell diameter of 34 inches multiplied by the square of the number of operating cells, or $D_{eff} = 34^{**}\sqrt{18}$			

The Spillane methodology was originally developed to treat multiple individual stacks that are arranged along a linear x or y direction, but not both directions at once, with stack separations much greater than the stack diameters, typical of boilers/turbines at large power plants. As noted above, the 42 chillers on SVY06 are generally arranged in a 6 x 8 pattern. Therefore, the enhanced Spillane methodology was based on calculating the total merging height for the largest linear direction of chiller placements (which is eight chillers spaced 27.1 feet apart along the shorter length (width) of the building). The largest grouping of 42 (6x8) chillers were considered in the calculation of vertical velocity plume enhancement (both at and above the totally merged height, and for the interpolation down to the plume touching height). Again, the effective single stack diameter of each chiller was based on the combined 18 chiller cells.

Screening level vertical plume velocity assessments were made for the same ambient temperatures with calm winds and neutral atmospheric conditions as was done for the emergency generator engines. The results are presented in Table 4 and the output from the calculation spreadsheets are provided in Attachment A.

The initial jet phase extends to a height of about 155.1 ft-agl for both winter and summer cases (the larger of the merged length or merged width are presented). The critical plume-averaged vertical velocity of 5.3 m/s occurs in the jet phase at about 155.1 ft-agl for both cases. The plumes touch (begin to merge) at about 166 ft-agl and are fully merged at about 674 ft-agl for both cases. Under the enhanced Spillane methodology, the merged plume-averaged vertical velocities never approach 5.3 m/s (either above the totally merged height or when interpolated down to the touching height).



Table 4 Chiller Vertical Plume Velocity Analysis Results for Reference Height		
Case #	1	2
Ambient Temperature (°F)	41.0	84.3
<b>Single Plume Results:</b>		
Height of 5.3 m/s Plume-Averaged Vertical Velocity (Within the Jet Phase, feet-agl)	162.0	161.9
<b>Merged Plume Results:</b>		
Plume-Averaged Vertical Velocity at 1,000 feet-agl (m/s)	3.20	3.12

From these results and for each ambient condition, the vertical plume velocities are less than the threshold value of 5.3 m/s for all heights above about 162 ft-agl and above for the chillers. The heights at which plume-averaged vertical velocities exceed 5.3 m/s only occur during the jet phase for both cases. These cases also represent worst-case conditions of calm winds at all levels of a neutral atmosphere.

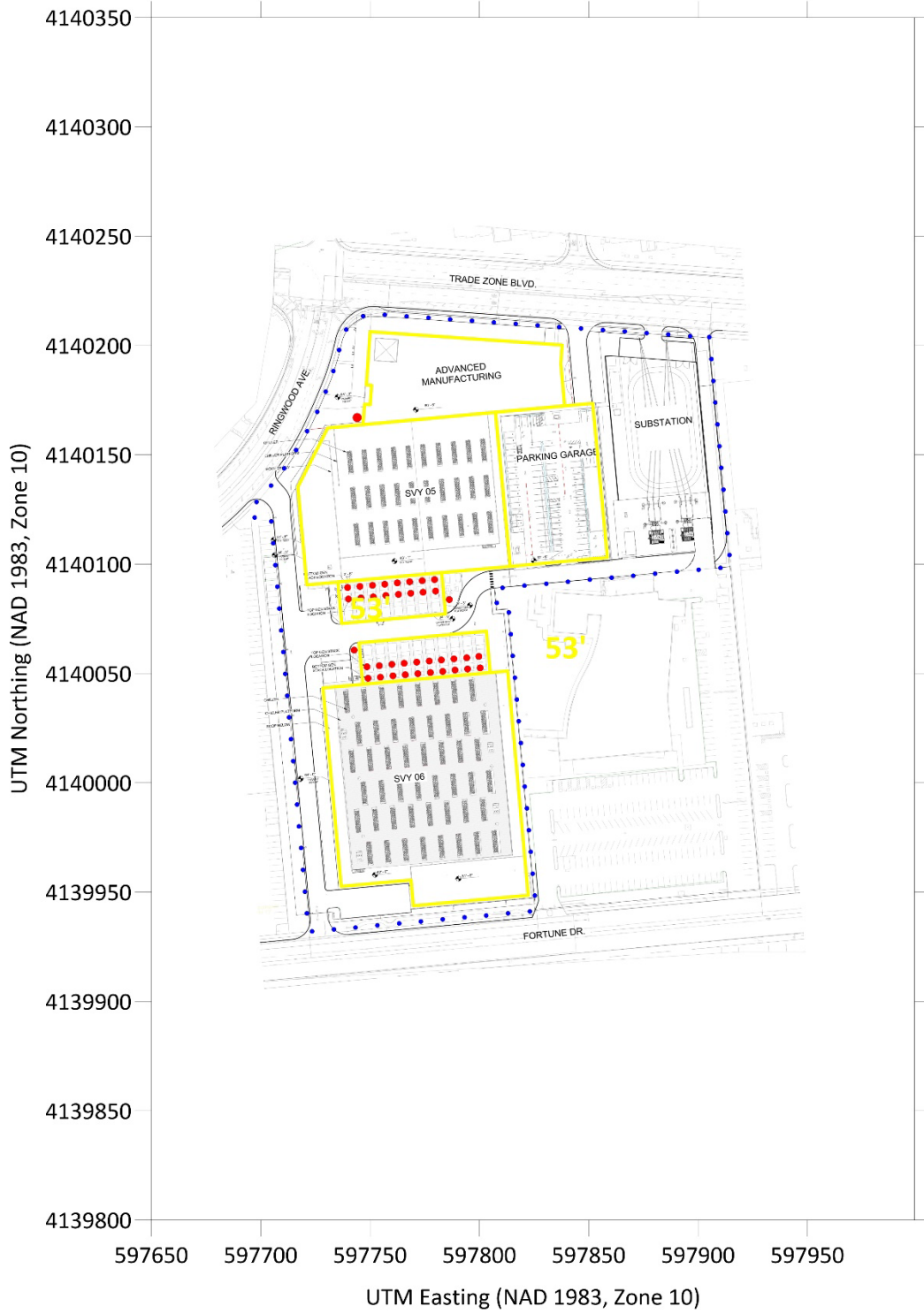
These screening results indicate that mechanical and thermal turbulence levels due to the flow from the chillers always remain in the light turbulence category and below the significance level of 5.3 m/s at all heights above about 162 ft-agl. Even light wind speeds can dramatically decrease the predicted plume-averaged vertical velocities, so the above results are very conservative indications of adverse conditions. The important factor for a given location is the appropriateness of available information for estimating true wind and temperature profiles throughout a typical year. Theoretical calculations, as shown in the tables above, are likely to overestimate the expected vertical velocities, for the following reasons:

- The wind profile is assumed constant with height with no occurrence of wind-shear when realistically, there is a considerable variation with height, especially in light winds;
- Worst-case scenarios are based on very light-wind, near-neutral atmospheric conditions with maximum loading.





**Figure 1**  
**SVYBGF Engine and Chiller Layout**



**Attachment A**  
**Spillane Method Plume Velocity Calculations**



SINGLE Plume Average Vertical Velocities for Stacks Large Emer.Gen Engine, 100% Load, and Maximum Stack Height - Winter Min*					
"Aviation Safety and Buoyant Plumes," Peter Best, et. al.					
"The Evaluation of Maximum Updraft Speeds for Calm Conditions at Various Heights in the Plume from a Gas-Turbine Power Station at Oakey, Queensland, Australia," Dr. K.T. Spillane					
<b>Ambient Conditions:</b>		Ambient Potential Temp $\theta_a$		Constants: Assume neutral conditions ( $d\theta/dz=0$ or $\theta_a=\theta_0$ )	
	278.15 Kelvins	41.0 °F		0.3048 meters/feet	
<b>Plume Exit Conditions:</b>		Maximum Stack Height $h_s$		Gravity $g$	
	18.59 meters	61 feet-inches		9.81 m/s <sup>2</sup>	
	Stack Diameter $D$	20 inches		$\lambda$	1.11
	Stack Velocity $V_{exit}$	174.21 ft/sec		$\lambda_0$	-1.0
	Volumetric Flow	22,987 ACFM		$\pi V_{exit} D^2 / 4$	Sect.2/¶1
	Stack Potential Temp $\theta_s$	902 °F		$g V_{exit} D^2 (1-\theta_0/\theta_s) / 4 = \text{Vol. Flow}(g/\pi)(1-\theta_0/\theta_s)$	Sect.2/¶1
	Initial Stack Buoyancy Flux $F_b$	21,4178 m <sup>4</sup> /s <sup>3</sup>		$\lambda^2 g V a^2 (1-\theta_0/\theta_s)$ for a, V, $\theta_s$ at plume height (see below)	
	Plume Buoyancy Flux $F$	N/A m <sup>4</sup> /s <sup>3</sup>		1,000 Multiple Stack Multiplication Factor ( $N^{0.25}$ )	
	No. of Stacks $N$	1			
<b>Conditions at End (Top) of Jet Phase:</b>					
	Height above Stack $Z_{jet}$	3.188 meters*	10.5 feet*	$Z_{jet} = 6.25D$ , meters*=meters above stack top	Sect.3/¶1
	Height above Ground $Z_{jet}+h_s$	21.778 meters	71.4 feet		-
	Vertical Velocity $V_{jet}$	26.550 m/s	87.11 ft/sec	$V_{jet} = 0.5 V_{exit} = V_{exit}/2$	-
	Plume Top-Hat Diameter $2a_{jet}$	1.020 meters	3.3 feet	$2a_{jet} = 2D$	Conservation of momentum
<b>Spillane Methodology - Analytical Solutions for Calm Conditions for Plume Heights above Jet Phase</b>					
Single Plume-averaged Vertical Velocity $V$ given by Analytical Solution in Paper where Product $Va$ given by equations below:					
	Plume Top-Hat Radius $a$	Solutions in Table Below		0.16(z-z <sub>v</sub> ), or linear increase with height	Sect.2/Eq.6
	Virtual Source Height $z_v$	1.255 meters*	4.1 feet*	$6.25D[1-(\theta_0/\theta_s)^{1/2}]$ , meters*=meters above stack top	Sect.2/Eq.6
	Height above Ground $Z_v+h_s$	19.845 meters	65.1 feet	where $(\theta_0/\theta_s)^{1/2} = (\theta_0/\theta_s)^{1/2}$	0.6064
	Vertical Velocity $V$	Solutions in Table Below		$\{(Va)_0^3 + 0.12F_b [(z-z_v)^2 - (6.25D-z_v)^2]^{1/2}\} / a$	Sect.2.1(6)
	Product $(Va)_0$	8.211 m <sup>2</sup> /s		$V_{exit} D / 2 (\theta_0/\theta_s)^{1/2}$	
<b>Solve for plume-averaged vertical velocity at height 200.0 feet</b> 60.96 meters above ground (z+h <sub>s</sub> )					
	Gives the following Height above Stack $z'$	42.370 meters*	139.0 feet*		
	Plume Top-Hat Diameter $2a'$	13.157 meters	43.2 feet	$2a' = 2 \cdot 0.16(z'-z_v)$	Sect.2/Eq.6
	Vertical Velocity $V$	2.580 m/s	8.46 ft/sec	$V = \{(Va)_0^3 + 0.12F_b [(z-z_v)^2 - (6.25D-z_v)^2]^{1/2}\} / (2a'/2)$	Sect.2/Eq.6
<b>Solve for Height of CASC critical vertical velocity <math>V_{crit}</math> 5.30 m/s plume-averaged vertical velocity</b> Critical $VW >$ Top of Jet (Spillane)					
	Find Height above Stack $z_{crit}$	12.511 meters	41.0 feet	Solve for $x=(z-z_v)$ simultaneously in both eqs. (i.e., $Va$ and $a$ )	-4,2147
	Height above Ground $Z_{crit}+h_s$	31.101 meters	102.0 feet	for $V=4.3$ m/s using the cubic equation $ax^3+bx^2+cx+d=0$ , where	-892.08
				$a=1$ , $c=0$ , and $b=-0.12F_b/(4 \cdot 3^0 \cdot 16^3) =$	
				and $d=[0.12F_b(6.25D-z_v)^2 - (Va)_0^3]/(4 \cdot 3^0 \cdot 16^3) =$	
<b>Interpolated Height of critical vertical velocity in Jet Phase:</b>					
	Find Height above Stack $z_{crit}$	#N/A meters	#N/A feet	<a href="http://www.1728.org/cubic.htm">http://www.1728.org/cubic.htm</a>	
	Height above Ground $Z_{crit}+h_s$	#N/A meters	#N/A feet	gives the real solution $x = z-z_v =$	11.2559
				or $z$ (m/above stack) =	12.511
				$z$ (ft/above ground) =	102.0
<b>Table of Plume Top-Hat Diameters (2a) and Plume-Averaged Vertical Velocities starting at end of jet phase:</b>					
	Height (feet)	(meters)	Plume Radius(m)	SingleStk VertVel(m/s)	Plume Temp(K)
	above ground	above stack			
	<b>Stack.Rel.Ht = 61.0</b>		<b>0.00</b>	<b>0.255</b>	<b>53.10</b>
	65.0	1.22	0.353	42.89	
	70.0	2.75	0.476	30.12	
	<b>Top of jet = 71.4</b>		<b>3.17</b>	<b>0.510</b>	<b>26.55</b>
	80.0	5.79	0.726	11.59	358.75
	90.0	8.84	1.214	7.29	324.05
	100.0	11.89	1.702	5.53	308.91
	<b>Spillane 5.3 m/s Height = 102.0</b>		<b>12.51</b>	<b>1.801</b>	<b>5.30</b>
	110.0	14.94	2.189	4.61	300.48
	120.0	17.99	2.677	4.04	295.18
	130.0	21.03	3.165	3.66	291.61
	140.0	24.08	3.652	3.38	289.08
	150.0	27.13	4.140	3.17	287.22
	160.0	30.18	4.628	3.01	285.80
	210.0	45.42	7.066	2.51	282.09
	260.0	60.66	9.505	2.24	280.59
	310.0	75.90	11.943	2.06	279.83
	360.0	91.14	14.381	1.93	279.39
	410.0	106.38	16.820	1.83	279.10
	460.0	121.62	19.258	1.74	278.91
	510.0	136.86	21.697	1.67	278.78
	610.0	167.34	26.573	1.56	278.60
	710.0	197.82	31.450	1.48	278.49
	810.0	228.30	36.327	1.41	278.42
	910.0	258.78	41.204	1.35	278.37
	1010.0	289.26	46.081	1.30	278.33
	1110.0	319.74	50.957	1.25	278.30
	1210.0	350.22	55.834	1.22	278.28
	1310.0	380.70	60.711	1.18	278.26
	1410.0	411.18	65.588	1.15	278.25
	1510.0	441.66	70.465	1.13	278.24
	1610.0	472.14	75.341	1.10	278.23
	1710.0	502.62	80.218	1.08	278.22
	1810.0	533.10	85.095	1.06	278.21
	1910.0	563.58	89.972	1.04	278.21
	2010.0	594.06	94.849	1.02	278.20

\*Winter Min = Monthly Mean of Minimum Daily Temperatures for 1971-2000 (Lowest in December)

NOAA Sources: Climatology of the United States No.81 "Monthly Station Normals of Temperatures, Precipitation, and Heating and Cooling Degree Days, 1971-2000 California" and Climatology of the United States No. 20 "Monthly Station Climate Summaries, 1971-2000 California"



SINGLE Plume Average Vertical Velocities for Single Stacks Large Emer.Gen Engine, 100% Load, and Maximum Stack Height - Summer Max*					
"Aviation Safety and Buoyant Plumes," Peter Best, et. al.					
"The Evaluation of Maximum Updraft Speeds for Calm Conditions at Various Heights in the Plume from a Gas-Turbine Power Station at Oakey, Queensland, Australia," Dr. K.T. Spillane					
<b>Ambient Conditions:</b>		Assume neutral conditions (dθ/dz=0 or θ <sub>a</sub> =θ <sub>s</sub> )		Constants:	
Ambient Potential Temp θ <sub>a</sub>	302.21 Kelvins	84.3 °F		0.3048 meters/foot	
<b>Plume Exit Conditions:</b>		Gravity g		9.81 m/s <sup>2</sup>	
Maximum Stack Height h <sub>s</sub>	18.59 meters	61 feet-inches	λ	1.11	
Stack Diameter D	0.5080 meters	20 inches	λ <sub>0</sub>	-1.0	
Stack Velocity V <sub>exit</sub>	53.10 m/s	174.21 ft/sec			
Volumetric Flow	10.76 cu.m/sec	22,804 ACFM	πV <sub>exit</sub> D <sup>2</sup> /4		Sect.2/¶1
Stack Potential Temp θ <sub>s</sub>	756.48 Kelvins	902 °F			
Initial Stack Buoyancy Flux F <sub>g</sub>	20.1812 m <sup>4</sup> /s <sup>3</sup>		gV <sub>exit</sub> D <sup>2</sup> (1-θ <sub>s</sub> /θ <sub>a</sub> )/4 = Vol.Flow(g/π)(1-θ <sub>s</sub> /θ <sub>a</sub> )		Sect.2/¶1
Plume Buoyancy Flux F	N/A m <sup>4</sup> /s <sup>3</sup>		λ <sup>2</sup> gVa <sup>2</sup> (1-θ <sub>s</sub> /θ <sub>a</sub> ) for a, V, θ <sub>s</sub> at plume height (see below)		
No. of Stacks N	1		1.000 Multiple Stack Multiplication Factor (N <sup>0.25</sup> )		
<b>Conditions at End (Top) of Jet Phase:</b>					
Height above Stack z <sub>jet</sub>	3.175 meters*	10.4 feet*	z <sub>jet</sub> = 6.25D, meters*=meters above stack top		Sect.3/¶1
Height above Ground z <sub>jet</sub> +h <sub>s</sub>	21.765 meters	71.4 feet			
Vertical Velocity V <sub>jet</sub>	26.550 m/s	87.11 ft/sec	V <sub>jet</sub> = 0.5V <sub>exit</sub> = V <sub>exit</sub> /2		
Plume Top-Hat Diameter 2a <sub>jet</sub>	1.016 meters	3.3 feet	2a <sub>jet</sub> = 2D	Conservation of momentum	
<b>Spillane Methodology - Analytical Solutions for Calm Conditions for Plume Heights above Jet Phase</b>					
Single Plume-averaged Vertical Velocity V given by Analytical Solution in Paper where Product Va given by equations below:					
Plume Top-Hat Radius a	Solutions in Table Below		0.16(z-z <sub>v</sub> ), or linear increase with height		Sect.2/Eq.6
Virtual Source Height z <sub>v</sub>	1.168 meters*	3.8 feet*	6.25D[1-(θ <sub>s</sub> /θ <sub>a</sub> ) <sup>1/2</sup> ], meters*=meters above stack top		Sect.2/Eq.6
Height above Ground z <sub>v</sub> +h <sub>s</sub>	19.758 meters	64.8 feet	where (θ <sub>s</sub> /θ <sub>a</sub> ) <sup>1/2</sup> = (θ <sub>s</sub> /θ <sub>a</sub> ) <sup>1/2</sup>		0.6321
Vertical Velocity V	Solutions in Table Below		{(Va) <sub>s</sub> <sup>3</sup> + 0.12F <sub>g</sub> [(z-z <sub>v</sub> ) <sup>2</sup> - (6.25D-z <sub>v</sub> ) <sup>2</sup> ] <sup>1/3</sup> } / a		Sect.2.1(6)
Product (Va) <sub>s</sub>	8.525 m <sup>2</sup> /s		V <sub>exit</sub> D/2(θ <sub>s</sub> /θ <sub>a</sub> ) <sup>1/2</sup>		
<b>Solve for plume-averaged vertical velocity at height 200.0 feet</b> 60.96 meters above ground (z+h <sub>s</sub> )					
Gives the following Height above Stack z'	42.370 meters*	139.0 feet*			
Plume Top-Hat Diameter 2a'	13.185 meters	43.3 feet	2a' = 2*0.16(z'-z <sub>v</sub> )		Sect.2/Eq.6
Vertical Velocity V	2.545 m/s	8.35 ft/sec	V = {(Va) <sub>s</sub> <sup>3</sup> + 0.12F <sub>g</sub> [(z-z <sub>v</sub> ) <sup>2</sup> - (6.25D-z <sub>v</sub> ) <sup>2</sup> ] <sup>1/3</sup> } / (2a'/2)		Sect.2/Eq.6
<b>Solve for Height of CASC critical vertical velocity V<sub>crit</sub> = 5.30 m/s plume-averaged vertical velocity</b> Critical VW > Top of Jet (Spillane)					
Find Height above Stack z <sub>crit</sub>	12.683 meters	41.6 feet	Solve for x=(z-z <sub>v</sub> ) simultaneously in both eqs. (i.e., Va and a)		
Height above Ground z <sub>crit</sub> +h <sub>s</sub>	31.273 meters	102.6 feet	for V=4.3 m/s using the cubic equation ax <sup>3</sup> +bx <sup>2</sup> +cx+d=0, where		
				a=1, c=0, and b=-[0.12F <sub>g</sub> ]/(4.3 <sup>3</sup> 0.16 <sup>3</sup> )=	-3.9714
				and d=[0.12F <sub>g</sub> (6.25D-z <sub>v</sub> ) <sup>2</sup> -(Va) <sub>s</sub> <sup>3</sup> ]/(4.3 <sup>3</sup> 0.16 <sup>3</sup> )=	-1000.01
<b>Interpolated Height of critical vertical velocity in Jet Phase:</b>					
Find Height above Stack z <sub>crit</sub>	#N/A meters	#N/A feet			<a href="http://www.1728.org/cubic.htm">http://www.1728.org/cubic.htm</a>
Height above Ground z <sub>crit</sub> +h <sub>s</sub>	#N/A meters	#N/A feet	gives the real solution x = z-z <sub>v</sub> =	11.5145	
				or z(m/above stack) =	12.683
				z(ft/above ground) =	102.6
<b>Table of Plume Top-Hat Diameters (2a) and Plume-Averaged Vertical Velocities starting at end of jet phase:</b>					
Height (feet)	(meters)	Plume Radius(m)	SingleStk VertVel(m/s)	Plume Temp(K)	
<b>above ground above stack</b>		<b>0.00</b>	<b>0.254</b>	<b>53.10</b>	
<b>Stack.Rel.Ht = 61.0</b>					
65.0	1.22	0.352	42.89		<b>Jet Phase Eqs:</b> 5 foot Intervals
70.0	2.75	0.474	30.12		
<b>Top of jet = 71.4</b>					
80.0	5.79	0.740	11.77	380.45	<b>Spillane Equations:</b>
90.0	8.84	1.228	7.41	347.39	
100.0	11.89	1.715	5.60	332.81	V <sub>plume</sub> = {(Va) <sub>s</sub> <sup>3</sup> + 0.12F <sub>g</sub> [(z-z <sub>v</sub> ) <sup>2</sup> - (6.25D-z <sub>v</sub> ) <sup>2</sup> ] <sup>1/3</sup> } / a
<b>Spillane 5.3 m/s Height = 102.6</b>					
110.0	14.94	2.203	4.64	324.61	a = 0.16(z-z <sub>v</sub> )
120.0	17.99	2.691	4.05	319.42	θ <sub>s</sub> = θ <sub>a</sub> [1 + (1 - θ <sub>s</sub> /θ <sub>a</sub> ) * (V <sub>exit</sub> D <sup>2</sup> / (4V <sub>plume</sub> a <sup>2</sup> λ <sup>2</sup> ))]
130.0	21.03	3.179	3.65	315.88	
140.0	24.08	3.666	3.37	313.36	
150.0	27.13	4.154	3.15	311.49	
160.0	30.18	4.642	2.98	310.07	
210.0	45.42	7.080	2.47	306.28	
260.0	60.66	9.518	2.20	304.74	
310.0	75.90	11.957	2.02	303.96	
360.0	91.14	14.395	1.89	303.50	
410.0	106.38	16.834	1.79	303.20	
460.0	121.62	19.272	1.71	303.00	
510.0	136.86	21.710	1.64	302.86	
610.0	167.34	26.587	1.53	302.68	
710.0	197.82	31.464	1.45	302.56	
810.0	228.30	36.341	1.38	302.49	
910.0	258.78	41.218	1.32	302.43	
1010.0	289.26	46.094	1.27	302.40	
1110.0	319.74	50.971	1.23	302.37	
1210.0	350.22	55.848	1.19	302.35	
1310.0	380.70	60.725	1.16	302.33	
1410.0	411.18	65.602	1.13	302.31	
1510.0	441.66	70.478	1.10	302.30	
1610.0	472.14	75.355	1.08	302.29	
1710.0	502.62	80.232	1.06	302.28	
1810.0	533.10	85.109	1.04	302.28	
1910.0	563.58	89.986	1.02	302.27	
2010.0	594.06	94.862	1.00	302.27	

\*Summer Max = Monthly Mean of Maximum Daily Temperatures for 1971-2000 (Highest in July)  
 NOAA Sources: Climatology of the United States No.81 "Monthly Station Normals of Temperatures, Precipitation, and Heating and Cooling Degree Days, 1971-2000 California" and Climatology of the United States No. 20 "Monthly Station Climate Summaries, 1971-2000 California"



SINGLE/Approximated Plume Average Vertical Velocities for Stacks Chillers using CEC Staff Methodology - Winter Min*					
Based on 42 chillers w/ 18 cells/chiller. Calc' eff diam for each chiller with each cell at 34" ID (257,143 ACFM total for each chiller).					
"Aviation Safety and Buoyant Plumes," Peter Best, et. al.					
"The Evaluation of Maximum Updraft Speeds for Calm Conditions at Various Heights in the Plume from a Gas-Turbine Power Station at Oakey, Queensland, Australia," Dr. K.T. Spillane					
Ambient Conditions:		Ambient Potential Temp $\theta_a$		Constants: Assume neutral conditions ( $d\theta/dz=0$ or $\theta_a=\theta_b$ )	
		278.15 Kelvins	41.0 °F	0.3048 meters/feet	
Plume Exit Conditions:		Stack Height $h_s$		Gravity g	
		24.38 meters	80 feet-inches	9.81 m/s <sup>2</sup>	
Individual Chiller		Stack Diameter D		$\lambda$	
		3.6639 meters	144.2 inches	1.11	
		Stack Velocity $V_{exit}$		$\lambda_c$	
		11.51 m/s	37.76 ft/sec	~1.0	
Individual Chiller		Volumetric Flow		$4Vol/(60\pi D^2)$	
		121.36 cu.m/sec	257,143 ACFM	$\pi V_{exit} D^2/4$	
		Stack Potential Temp $\theta_s$			
		289.26 Kelvins	61.0 °F		
Initial Stack Buoyancy Flux $F_o$		14.5564 m <sup>3</sup> /s <sup>3</sup>		$gV_{exit} D^2(1-\theta_p/\theta_a)/4 = Vol.Flow(g/\pi)(1-\theta_p/\theta_a)$	
Plume Buoyancy Flux F		N/A m <sup>3</sup> /s <sup>3</sup>		$\lambda^2 g Va^2(1-\theta_p/\theta_a)$ for a, V, $\theta_p$ at plume height (see below)	
Number of Chillers n		42		2.546 Multiple Stack Multiplication Factor ( $n^{0.25}$ )	
Conditions at End (Top) of Jet Phase:					
Height above Stack $z_{jet}$		22,900 meters*		75.1 feet*	
Height above Ground $z_{jet}+h_s$		47,284 meters		155.1 feet	
Vertical Velocity $V_{jet}$		5.755 m/s		18.88 ft/sec	
Plume Top-Hat Diameter $2a_{jet}$		7.328 meters		24.0 feet	
				$V_{jet} = 0.5V_{exit} = V_{exit}/2$	
				$2a_{jet} = 2D$ Conservation of momentum	
Spillane Methodology - Analytical Solutions for Calm Conditions for Plume Heights above Jet Phase					
Single Plume-averaged Vertical Velocity V given by Analytical Solution in Paper where Product Va given by equations below:					
Plume Top-Hat Radius a		Solutions in Table Below		0.16(z-z <sub>v</sub> ), or linear increase with height	
Virtual Source Height z <sub>v</sub>		0.444 meters*		1.5 feet*	
Height above Ground z <sub>v</sub> +h <sub>s</sub>		24.828 meters		81.5 feet	
Vertical Velocity V		Solutions in Table Below		$\{(Va)_o^3 + 0.12F_o [(z-z_v)^2 - (6.25D-z_v)^2]^{1/3}\} / a$	
Product (Va) <sub>o</sub>		20.677 m <sup>2</sup> /s		$V_{exit} D/2(\theta_p/\theta_a)^{1/2}$	
Single Chiller Results:					
Solve for plume-averaged vertical velocity at height		540.0 feet		164.592 meters above ground (z'+h <sub>s</sub> )	
Gives the following Height above Stack z'		140.208 meters*		460.0 feet*	
Plume Top-Hat Diameter 2a'		44.724 meters		146.7 feet	
Vertical Velocity V		1.555 m/s		5.10 ft/sec	
				$2a' = 2 \cdot 0.16(z'-z_v)$	
				$V = \{(Va)_o^3 + 0.12F_o [(z-z_v)^2 - (6.25D-z_v)^2]^{1/3}\} / (2a'/2)$	
Solve for Height of CASC critical vertical velocity V <sub>crit</sub> 5.30 m/s plume-averaged vertical velocity Critical VV > Top of Jet (Spillane)					
Find Height above Stack z <sub>crit</sub>		24,984 meters		82.0 feet	
Height above Ground z <sub>crit</sub> +h <sub>s</sub>		49,368 meters		162.0 feet	
Interpolated Height of critical vertical velocity in Jet Phase:				Solve for x=(z-z <sub>v</sub> ) simultaneously in both eqs. (i.e., Va and a)	
Find Height above Stack z <sub>crit</sub>		#N/A meters		#N/A feet	
Height above Ground z <sub>crit</sub> +h <sub>s</sub>		#N/A meters		#N/A feet	
				for V=V <sub>crit</sub> using the cubic equation $ax^3+bx^2+cx+d=0$ , where	
				a=1, c=0, and b=-0.12F <sub>o</sub> /(V <sub>crit</sub> <sup>3</sup> ·0.16 <sup>3</sup> )= -2.86450	
				and d=[0.12F <sub>o</sub> (6.25D-z <sub>v</sub> ) <sup>2</sup> -(Va) <sub>o</sub> <sup>2</sup> ]/(V <sub>crit</sub> <sup>3</sup> ·0.16 <sup>3</sup> )= -13052.47	
				gives the real solution x = z-z <sub>v</sub> = 24.5395	
				or z(m/above stack) = 24.984	
				z(ft/above ground) = 162.0	
Table of Plume Top-Hat Diameters (2a) and Plume-Averaged Vertical Velocities starting at end of jet phase:					
Height (feet)	(meters)	Plume SingleStk	Plume		
above ground	above stack	Radius(m)	VertVel(m/s)	Temp(K)	
Stack, Rel.Ht = 80.0					
	0.00	1.832	11.51		
100.0	6.10	2.198	10.36		Jet Phase Eqs: 20 ft Intervals
120.0	12.19	2.565	9.21		Linearly interpolated from Stack Rel.Ht to Top of Jet
140.0	18.29	2.931	8.06		Spillane Equations:
160.0	24.38	3.298	6.91		
Top of Single jet = 155.1					
	22.90	3.208	7.19		$V_{plume} = \{(Va)_o^3 + 0.12F_o [(z-z_v)^2 - (6.25D-z_v)^2]^{1/3}\} / a$
180.0	30.48	3.664	5.76	282.68	a = 0.16(z-z <sub>v</sub> )
160.0	24.38	3.830	5.42	282.49	$\theta_p = \theta_a(1 + (1 - (\theta_p/\theta_a)) * (V_{exit} D^2 / (4V_{plume} * a^2 * \lambda^2)))$
180.0	30.48	4.806	4.41	282.36	CEC Staff Equation:
200.0	36.58	5.781	3.76	281.44	$V_{mp} = n^{0.25} V_{sp}$
220.0	42.67	6.756	3.30	280.82	Brigg's Equation:
240.0	48.77	7.732	2.96	280.37	$V_{ Briggs } = (2/3) \times 1.6^{(2/3)} \times F_{mp}^{(1/3)} \times U^{(1/2)} \times z^{(1/2)}$
260.0	54.86	8.707	2.71	280.04	where $F_{mp} = nF_{sp}$
280.0	60.96	9.683	2.51	279.78	
300.0	67.06	10.658	2.35	279.57	
350.0	82.30	13.096	2.06	279.40	50 ft Intervals
400.0	97.54	15.535	1.87	279.10	Max < 5.3 m/s
450.0	112.78	17.973	1.73	278.89	
500.0	128.02	20.412	1.62	278.75	
550.0	143.26	22.850	1.54	278.65	
600.0	158.50	25.288	1.47	278.57	
650.0	173.74	27.727	1.42	278.51	
700.0	188.98	30.165	1.37	278.46	
800.0	219.46	35.042	1.29	278.42	100 ft Intervals
900.0	249.94	39.919	1.22	278.36	
1000.0	280.42	44.796	1.17	278.32	
1100.0	310.90	49.672	1.13	278.29	
1200.0	341.38	54.549	1.09	278.27	
1300.0	371.86	59.426	1.06	278.25	
1400.0	402.34	64.303	1.03	278.24	
1500.0	432.82	69.180	1.00	278.23	
2000.0	585.22	93.564	0.90	278.22	500 ft Intervals
2500.0	737.62	117.948	0.84	278.19	
3000.0	890.02	142.332	0.78	278.18	
3500.0	1042.42	166.716	0.74	278.17	
4000.0	1194.82	191.100	0.71	278.17	
4500.0	1347.22	215.484	0.68	278.16	



MERGED (along length) Plume Average Vertical Velocities for Stacks Chillers using CEC Staff Methodology - Winter Min*					
"Aviation Safety and Buoyant Plumes," Peter Best, et. al.					
"The Evaluation of Maximum Updraft Speeds for Calm Conditions at Various Heights in the Merged Plume from Two Gas-Turbine Power Station at Oaky, Queensland, Australia," Dr. K.T. Spillane					
Ambient Conditions:			Constants: Assume neutral conditions (dθ/dz=0 or θ <sub>s</sub> =θ <sub>a</sub> )		
Ambient Potential Temp θ <sub>a</sub>	278.15 Kelvins	41.0 °F		0.3048 meters/feet	
Plume Exit Conditions:			Gravity g	9.81 m/s <sup>2</sup>	
Stack Height h <sub>s</sub>	24.38 meters	80 feet-inches	λ	1.11	
Individual Stack Diameter D	3.6639445 meters	144.2 inches	λ <sub>0</sub>	-1.0	
Stack Velocity V <sub>exit</sub>	11.51 m/s	37.76 ft/sec	4Vol/(60πD <sup>2</sup> )		
Individual Volumetric Flow	121.36 cu.m/sec	257.143 ACFM	πV <sub>exit</sub> D <sup>2</sup> /4		Sect.2¶1
Stack Potential Temp θ <sub>s</sub>	289.26 Kelvins	61.0 °F			
Initial Stack Buoyancy Flux F <sub>0</sub>	14.56 m <sup>4</sup> /s <sup>3</sup>	20.0 ΔT(°F)	gV <sub>exit</sub> D <sup>2</sup> (1-θ <sub>s</sub> /θ <sub>a</sub> )/4 = Vol.Flow(g/m)(1-θ <sub>s</sub> /θ <sub>a</sub> )		Sect.2¶1
Plume Buoyancy Flux F	N/A	m <sup>4</sup> /s <sup>3</sup>	λ <sup>2</sup> gVa <sup>2</sup> (1-θ <sub>s</sub> /θ <sub>a</sub> ) for a, V, θ <sub>s</sub> at plume height (see below)		
Total Number of Stacks n	42				
Average Adjacent Stack Separation d	13.44 meters	44.1 feet	<div style="border: 1px solid black; padding: 2px;">           Calcs based on multiple plume treatment in Peter Best Paper: plume velocities increased by N<sup>0.25</sup> at the height where plumes fully merged (interp. below ht, single merged stack above ht)         </div>		
Number of Stacks along Orientation N	6				
Conditions at End (Top) of Jet Phase:					
Height above Stack z <sub>jet</sub>	22.900 meters*	75.1 feet*	z <sub>jet</sub> = 6.25D, meters*=meters above stack top		Sect.3¶1
Height above Ground z <sub>jet</sub> +h <sub>s</sub>	47.284 meters	155.1 feet			"
Vertical Velocity V <sub>jet</sub>	5.755 m/s	18.88 ft/sec	V <sub>jet</sub> = 0.5V <sub>exit</sub> = V <sub>exit</sub> /2		"
Plume Top-Hat Diameter 2a <sub>jet</sub>	7.328 meters	24.0 feet	2a <sub>jet</sub> = 2D		Conservation of momentum
Spillane Methodology - Analytical Solutions for Calm Conditions for Plume Heights above Jet and Merging Phases					
Single Plume-averaged Vertical Velocity V given by Analytical Solution in Paper where Product Va given by equations below:					
Single Plume Values: Plume Top-Hat Radius a Used in Plume Merging Only a = 0.16(z-z <sub>v</sub> ), or linear increase with height Sect.2/Eq.6					
Virtual Source Height z <sub>v</sub>	0.444 meters*	1.5 feet*	z <sub>v</sub> = 6.25D[1-(θ <sub>s</sub> /θ <sub>a</sub> ) <sup>1/2</sup> ], meters*=meters above stack top		Sect.2/Eq.6
Height above Ground z <sub>v</sub> +h <sub>s</sub>	24.828 meters	81.5 feet	where (θ <sub>s</sub> /θ <sub>a</sub> ) <sup>1/2</sup> = (θ <sub>s</sub> /θ <sub>a</sub> ) <sup>1/2</sup> = 0.9806		
Single Plume Values: Vertical Velocity V Used in Plume Merging Only ((Va) <sup>3</sup> + 0.12F <sub>0</sub> [(z-z <sub>v</sub> ) <sup>2</sup> - (6.25D-z <sub>v</sub> ) <sup>2</sup> ]) <sup>1/3</sup> / a Sect.2.1(6)					
Product (Va) <sub>s</sub>	20.677 m <sup>2</sup> /s		V <sub>exit</sub> (D/2)(θ <sub>s</sub> /θ <sub>a</sub> ) <sup>1/2</sup>		
Plume Merging - Based on Single Plume Calculations where: Sect.3¶3					
Begin Merging Plume Top-Hat Diameter 2a <sub>touch</sub> 13.440 meters 44.1 feet 2a <sub>touch</sub> =d, (or a <sub>touch</sub> =d/2)					
Height above Stack z <sub>touch</sub>	42.444 meters*	139.3 feet*	z <sub>touch</sub> = z <sub>v</sub> +d/(2*0.16), meters*=meters above stack top		
Height above Ground z <sub>touch</sub> +h <sub>s</sub>	66.828 meters	219.3 feet			
Vertical Velocity V <sub>touch</sub>	3.314 m/s	10.9 ft/sec	V <sub>touch</sub> = ((Va) <sup>3</sup> + 0.12F <sub>0</sub> [(z-z <sub>v</sub> ) <sup>2</sup> - (6.25D-z <sub>v</sub> ) <sup>2</sup> ]) <sup>1/3</sup> / a		
Total Merging Plume Top-Hat Diameter 2a <sub>full</sub> 67.200 meters 220.5 feet 2a <sub>full</sub> =2d(N-1)/2, (or 2a <sub>full</sub> =d(N-1)/2) FOR 2 STACKS, 2a <sub>full</sub> =2d					
Height above Stack z <sub>full</sub>	210.444 meters*	690.4 feet*	z <sub>full</sub> = z <sub>v</sub> +2d/(2*0.16), meters*=meters above stack top		
Height above Ground z <sub>full</sub> +h <sub>s</sub>	234.828 meters	770.4 feet			
Vertical Velocity V <sub>full</sub>	1.309 m/s	4.3 ft/sec	V <sub>full</sub> = ((Va) <sup>3</sup> + 0.12F <sub>0</sub> [(z <sub>full</sub> -z <sub>v</sub> ) <sup>2</sup> - (6.25D-z <sub>v</sub> ) <sup>2</sup> ]) <sup>1/3</sup> / 2a <sub>full</sub>		
Product (V <sup>3</sup> a) <sub>full</sub>	75 m <sup>4</sup> /s <sup>3</sup>				
Conditions at End (Top) of Merging Phase - Define new values for V <sub>full</sub> and 2a <sub>full</sub> in Merged Plume calculations (based on TOTAL number of stacks):					
Merged Plume Values: Plume Diameter 2a Solutions in Table Below 2a = 2 x (a <sub>m</sub> + 0.16(z-z <sub>full</sub> )), or linear increase with height					
Revised Merged Plume Radius a <sub>m</sub>	85.537 meters	280.6 feet	where a <sub>m</sub> = n <sup>0.25</sup> a <sub>full</sub> where Total Merging Occurs		
Revised Merged Plume Velocity V <sub>m</sub>	3.331 m/s	10.93 ft/sec	and V <sub>m</sub> = n <sup>0.25</sup> V <sub>full</sub> where Total Merging Occurs		
Revised Virtual Source Height z <sub>v,full</sub>	210.444 meters*	690.4 feet*	Height above stack where Total Merging Occurs (shown above)		
Revised Vertical Velocity V			V = (n(V <sup>3</sup> a) <sub>full</sub> ) <sup>1/3</sup> for heights above total merging elevation		
Multiple Plume Calculations					
Solve for plume-averaged vertical velocity at height 540.0 feet 164.592 meters above ground (z+h <sub>s</sub> )					
Gives the following Height above Stack z 140.208 meters* 460.0 feet* LESS THAN TOP OF MERGING PHASE-INTERPOLATE					
Plume Top-Hat Radius a	#N/A meters	#N/A feet	a=a <sub>m</sub> +0.16(z-z <sub>full</sub> ) if z>z <sub>full</sub>		
Vertical Velocity V	3.324 m/s	10.90 ft/sec	V=(n(V <sup>3</sup> a) <sub>full</sub> ) <sup>1/3</sup> if z>z <sub>full</sub>		
Solve for Height of CASC critical vertical velocity V <sub>crit</sub> 5.30 m/s BEFORE TOUCHING Critical VV < Top of Jet					
Find Height above Stack z <sub>crit</sub>	JET meters	JET feet	z <sub>crit</sub> = z <sub>full</sub> + ((n(V <sup>3</sup> a) <sub>full</sub> )/(V <sub>crit</sub> ) <sup>3</sup> - a <sub>m</sub> )/0.16 if V <sub>crit</sub> <V <sub>m</sub>		
Height above Ground z <sub>crit</sub> +h <sub>s</sub>	JET meters	JET feet	z <sub>crit</sub> =z <sub>touch</sub> +(z <sub>full</sub> -z <sub>touch</sub> )(V <sub>crit</sub> -V <sub>touch</sub> )/(V <sub>crit</sub> -V <sub>m</sub> ) if V <sub>crit</sub> >V <sub>m</sub>		
Table of MERGED Plume-Averaged Vertical Velocities starting at Touching Height: Single Plume Eqns (see Single Plume spreadsheet)					
Height (feet)	(meters)	Plume Radius(m)	Vert. Vel(m/s)	V <sub>plume</sub> =(Va) <sup>3</sup> +0.12F <sub>0</sub> [(z-z <sub>v</sub> ) <sup>2</sup> -(6.25D-z <sub>v</sub> ) <sup>2</sup> ] <sup>1/3</sup> / a	
above ground above stack					
Begin Merging (touch) = 219.3 42.46 6.720 3.31 a = 0.16(z-z <sub>v</sub> )					
220.0	42.67	#N/A	3.31	θ <sub>s</sub> =θ <sub>a</sub> (1+(1-(θ <sub>s</sub> /θ <sub>a</sub> ))(V <sub>exit</sub> D <sup>2</sup> /(4V <sub>plume</sub> <sup>2</sup> a <sup>2</sup> λ <sup>2</sup> )))	
240.0	48.77	#N/A	3.31	Interpolated Layer Eqns	
260.0	54.86	#N/A	3.31	V=V <sub>touch</sub> +(V <sub>m</sub> -V <sub>touch</sub> )(z-z <sub>touch</sub> )/(z <sub>full</sub> -z <sub>touch</sub> )	
280.0	60.96	#N/A	3.32		
300.0	67.06	#N/A	3.32		
320.0	73.15	#N/A	3.32		
340.0	79.25	#N/A	3.32		
360.0	85.34	#N/A	3.32		
End Merging (full/mp) = 770.4 210.43 85.537 3.33 Merged Plume Eqns					
400.0	97.54	67.471	3.61	V=(n(V <sup>3</sup> a) <sub>full</sub> ) <sup>1/3</sup>	
450.0	112.78	69.910	3.56	a=a <sub>m</sub> +0.16(z-z <sub>full</sub> )	
500.0	128.02	72.348	3.52		
550.0	143.26	74.786	3.48		
600.0	158.50	77.225	3.45		
700.0	188.98	82.102	3.38	100 ft Intervals	
800.0	219.46	86.978	3.31		
900.0	249.94	91.855	3.25		
1000.0	280.42	96.732	3.20		
1100.0	310.90	101.609	3.15		
1200.0	341.38	106.486	3.10		
1300.0	371.86	111.362	3.05		
1400.0	402.34	116.239	3.01		
1500.0	432.82	121.116	2.97	500 ft Intervals	
2000.0	585.22	145.500	2.79		
2500.0	737.62	169.884	2.65		
3000.0	890.02	194.268	2.53		
3500.0	1042.42	218.652	2.44		
4000.0	1194.82	243.036	2.35		
4500.0	1347.22	267.420	2.28		
5000.0	1499.62	291.804	2.21		



MERGED (along width) Plume Average Vertical Velocities for Stacks Chillers using CEC Staff Methodology - Winter Min*				
*Aviation Safety and Buoyant Plumes,* Peter Best, et. al.				
*The Evaluation of Maximum Updraft Speeds for Calm Conditions at Various Heights in the Merged Plume from Two Gas-Turbine Power Station at Oakey, Queensland, Australia,* Dr. K.T. Spillane				
<b>Ambient Conditions:</b>		Constants: Assume neutral conditions (dB/dz=0 or $\theta_a=\theta_b$ )		
Ambient Potential Temp $\theta_a$	278.15 Kelvins	41.0 °F	0.3048 meters/feet	
<b>Plume Exit Conditions:</b>		Gravity g 9.81 m/s <sup>2</sup>		
Stack Height $h_s$	24.38 meters	80 feet-inches	$\lambda$	1.11
Individual Stack Diameter D	3.663945 meters	144.2 inches	$\lambda_b$	~1.0
Stack Velocity $V_{exit}$	11.51 m/s	37.76 ft/sec	4Vol/(60mD <sup>2</sup> )	
Individual Volumetric Flow	121.36 cu.m/sec	257,143 ACFM	$\pi V_{exit} D^2/4$	
Stack Potential Temp $\theta_s$	289.26 Kelvins	61.0 °F	Sect.2/¶1	
Initial Stack Buoyancy Flux $F_0$	14.56 m <sup>3</sup> /s <sup>3</sup>	20.0 ΔT(F)	$g V_{exit} D^2 (1-\theta_s/\theta_a)/4 = \text{Vol. Flow}(g/\pi)(1-\theta_s/\theta_a)$	
Plume Buoyancy Flux F	N/A m <sup>3</sup> /s <sup>3</sup>		$\lambda^2 g V a^2 (1-\theta_s/\theta_p)$ for a, V, $\theta_p$ at plume height (see below)	
Total Number of Stacks n	42			
Average Adjacent Stack Separation d	8.25 meters	27.1 feet	Calcs based on multiple plume treatment in Peter Best Paper:	
Number of Stacks along Orientation N	8		plume velocities increased by $N^{0.25}$ at the height where plumes fully merged (interp. below ht, single merged stack above ht)	
<b>Conditions at End (Top) of Jet Phase:</b>				
Height above Stack $z_{jet}$	22.900 meters*	75.1 feet*	$z_{jet} = 6.25D$ , meters*=meters above stack top	
Height above Ground $z_{jet}+h_s$	47.284 meters	155.1 feet	*	
Vertical Velocity $V_{jet}$	5.755 m/s	18.88 ft/sec	$V_{jet} = 0.5V_{exit} = V_{exit}/2$	
Plume Top-Hat Diameter $2a_{jet}$	7.328 meters	24.0 feet	$2a_{jet} = 2D$ Conservation of momentum	
<b>Spillane Methodology - Analytical Solutions for Calm Conditions for Plume Heights above Jet and Merging Phases</b>				
Single Plume-averaged Vertical Velocity V given by Analytical Solution in Paper where Product Va given by equations below:				
Single Plume Values: Plume Top-Hat Radius a		Used in Plume Merging Only		a = 0.16(z-z <sub>v</sub> ), or linear increase with height
Virtual Source Height $z_v$	0.444 meters*	1.5 feet*	$z_v = 6.25D[1-(\theta_s/\theta_a)]^{1/2}$ , meters*=meters above stack top	
Height above Ground $z_v+h_s$	24.828 meters	81.5 feet	where $(\theta_s/\theta_a)^{1/2} = (\theta_s/\theta_a)^{1/2} = 0.9806$	
Single Plume Values: Vertical Velocity V	Used in Plume Merging Only		$\{(Va)_0^3 + 0.12F_0 [(z-z_v)^2 - (6.25D-z_v)^2]^{1/3}\} / a$	
Product (Va) <sub>0</sub>	20.677 m <sup>3</sup> /s		$V_{exit}(D/2)(\theta_s/\theta_a)^{1/2}$	
Sect.2/Eq.6				
Sect.2/Eq.6				
Sect.2.1(6)				
Sect.3/¶3				
<b>Plume Merging - Based on Single Plume Calculations where:</b>				
Begin Merging Plume Top-Hat Diameter $2a_{touch}$	8.250 meters	27.1 feet	$2a_{touch}=d$ , (or $a_{touch}=d/2$ )	
Height above Stack $z_{touch}$	26.225 meters*	86.0 feet*	$z_{touch} = z_v + d/(2*0.16)$ , meters*=meters above stack top	
Height above Ground $z_{touch}+h_s$	50.609 meters	166.0 feet		
Vertical Velocity $V_{touch}$	5.065 m/s	16.6 ft/sec	$V_{touch} = \{(Va)_0^3 + 0.12F_0 [(z-z_v)^2 - (6.25D-z_v)^2]^{1/3}\} / a$	
Total Merging Plume Top-Hat Diameter $2a_{full}$	57.750 meters	189.5 feet	$2a_{full}=2d(N-1)^{1/2}$ , (or $a_{full}=d(N-1)^{1/2}$ ) FOR 2 STACKS, $2a_{full}=2d$	
Height above Stack $z_{full}$	180.913 meters*	593.5 feet*	$z_{full} = z_v + 2d/(2*0.16)$ , meters*=meters above stack top	
Height above Ground $z_{full}+h_s$	205.297 meters	673.5 feet		
Vertical Velocity $V_{full}$	1.391 m/s	4.6 ft/sec	$V_{full} = \{(Va)_0^3 + 0.12F_0 [(z_{full}-z_v)^2 - (6.25D-z_v)^2]^{1/3}\} / a_{full}$	
Product (V <sup>3</sup> a) <sub>full</sub>	78 m <sup>4</sup> /s <sup>3</sup>			
<b>Conditions at End (Top) of Merging Phase - Define new values for <math>V_{full}</math> and <math>a_{full}</math> in Merged Plume calculations (based on TOTAL number of stacks):</b>				
Merged Plume Values: Plume Diameter $2a$	Solutions in Table Below		$2a = 2x (a_m + 0.16(z-z_{full}))$ , or linear increase with height	
Revised Merged Plume Radius $a_m$	73.508 meters	241.2 feet	where $a_m = n^{0.25} a_{full}$ where Total Merging Occurs	
Revised Merged Plume Velocity $V_m$	3.542 m/s	11.62 ft/sec	and $V_m = n^{0.25} V_{full}$ where Total Merging Occurs	
Revised Virtual Source Height $z_{full}$	180.913 meters*	593.5 feet*	Height above stack where Total Merging Occurs (shown above)	
Revised Vertical Velocity V	Solutions in Tables Below		$V = \{(V^3 a)_{full}\}^{1/3}$ for heights above total merging elevation	
$V = V_{touch} + (V_m - V_{touch})^2 (z - z_{touch}) / (z_{full} - z_{touch})$				
for heights below total merging elevation				
<b>Multiple Plume Calculations</b>				
Solve for plume-averaged vertical velocity at height	540.0 feet	164.592 meters above ground (z+h <sub>s</sub> )	LESS THAN TOP OF MERGING PHASE-INTERPOLATE	
Gives the following Height above Stack z	140.208 meters*	460.0 feet*		
Plume Top-Hat Radius a	#N/A meters	#N/A feet	$a = a_m + 0.16(z-z_{full})$ if $z > z_{full}$	
Vertical Velocity V	3.943 m/s	12.94 ft/sec	$V = \{(V^3 a)_{full}\}^{1/3}$ if $z > z_{full}$	
$V = V_{touch} + (V_m - V_{touch})^2 (z - z_{touch}) / (z_{full} - z_{touch})$ if $z_{touch} < z < z_{full}$				
$V = \text{single plume values if } z < z_{touch}$				
Solve for Height of CASC critical vertical velocity $V_{crit}$	5.30 m/s		BEFORE TOUCHING Critical VV < Top of Jet	
Find Height above Stack $z_{crit}$	JET meters	JET feet	$z_{crit} = z_{full} + \{(n(V^3 a)_{full} / (V_{crit})^3) - a_m\} / 0.16$ if $V_{crit} < V_m$	
Height above Ground $z_{crit}+h_s$	JET meters	JET feet	$z_{crit} = z_{touch} + (z_{full} - z_{touch}) (V_{crit} - V_{touch}) / (V_m - V_{touch})$ if $V_{crit} > V_m$	
<b>Table of MERGED Plume-Averaged Vertical Velocities starting at Touching Height:</b>				
Height (feet)	(meters)	Plume Radius(m)	Vert. Vel(m/s)	Single Plume Eqns (see Single Plume spreadsheet)
above ground	above stack			$V_{plume} = \{(Va)_0^3 + 0.12F_0 [(z-z_v)^2 - (6.25D-z_v)^2]^{1/3}\} / a$
				$a = 0.16(z-z_v)$
Begin Merging (touch) = 166.0	26.21	4.125	5.07	$\theta_s = \theta_a (1 + (1 - \theta_s/\theta_a)) (V_{exit} D^2 / (4V_{plume} a^2 a^2))$
180.0	30.48	#N/A	5.02	Interpolated Layer Eqns
200.0	36.58	#N/A	4.96	$V = V_{touch} + (V_m - V_{touch})^2 (z - z_{touch}) / (z_{full} - z_{touch})$
220.0	42.67	#N/A	4.90	
240.0	48.77	#N/A	4.84	
260.0	54.86	#N/A	4.78	
280.0	60.96	#N/A	4.72	
300.0	67.06	#N/A	4.66	50 ft Intervals
350.0	82.30	#N/A	4.51	
400.0	97.54	#N/A	4.36	
450.0	112.78	#N/A	4.21	
500.0	128.02	#N/A	4.06	
550.0	143.26	#N/A	3.91	
600.0	158.50	#N/A	3.76	
650.0	173.74	#N/A	3.61	
End Merging (full/mp) = 673.5	180.90	73.508	3.54	
700.0	188.98	74.798	3.46	100 ft Intervals
800.0	219.46	79.675	3.16	
900.0	249.94	84.552	2.86	
1000.0	280.42	89.428	2.56	
1100.0	310.90	94.305	2.26	
1200.0	341.38	99.182	3.54	Merged Plume Eqns
1200.0	341.38	99.182	3.21	$V = \{(V^3 a)_{full}\}^{1/3}$
1300.0	371.86	104.059	3.15	$a = a_m + 0.16(z-z_{full})$
1500.0	432.82	113.812	3.06	
2000.0	585.22	138.196	2.87	
2500.0	737.62	162.580	2.72	500 ft Intervals
3000.0	890.02	186.964	2.59	
3500.0	1042.42	211.348	2.49	
4000.0	1194.82	235.732	2.40	
4500.0	1347.22	260.116	2.32	
5000.0	1499.62	284.500	2.26	



SINGLE/Approximated Plume Average Vertical Velocities for Stacks Chillers using CEC Staff Methodology - Summer Max*					
Based on 42 chillers w/ 18 cells/chiller. Calc' eff diam for each chiller with each cell at 34" ID (257,143 ACFM total for each chiller).		"Aviation Safety and Buoyant Plumes," Peter Best, et. al. "The Evaluation of Maximum Updraft Speeds for Calm Conditions at Various Heights in the Plume from a Gas-Turbine Power Station at Oakey, Queensland, Australia," Dr. K.T. Spillane			
<b>Ambient Conditions:</b>		Ambient Potential Temp $\theta_a$		Constants: Assume neutral conditions ( $d\theta/dz=0$ or $\theta_a=\theta_0$ )	
		302.21 Kelvins	84.3 °F	0.3048 meters/foot	
<b>Plume Exit Conditions:</b>		Stack Height $h_s$		Gravity $g$	
		24.38 meters	80 feet-inches	9.81 m/s <sup>2</sup>	
				$\lambda$ 1.11	
	<b>Individual Chiller</b>	Stack Diameter $D$	144.2 inches	$\lambda_0$ ~-1.0	
		3.6639 meters		4Vol/(60 $\pi$ D <sup>2</sup> )	
		Stack Velocity $V_{exit}$	37.76 ft/sec	$\pi V_{exit} D^2/4$	
	<b>Individual Chiller</b>	Volumetric Flow	257,143 ACFM	Sect.2/¶1	
		121.36 cu.m/sec			
		Stack Potential Temp $\theta_s$	104.3 °F		
		313.32 Kelvins			
		Initial Stack Buoyancy Flux $F_o$	20.0 $\Delta T$ (°F)	$g V_{exit} D^2 (1-\theta_s/\theta_a)/4 = \text{Vol.Flow}(g/\pi)(1-\theta_s/\theta_a)$ Sect.2/¶1	
		13.4335 m <sup>3</sup> /s <sup>3</sup>		$\lambda^2 g V_a^2 (1-\theta_s/\theta_a)$ for a, V, $\theta_s$ at plume height (see below)	
		Plume Buoyancy Flux $F$	N/A m <sup>3</sup> /s <sup>3</sup>		
		Number of Chillers $n$	42	2.546 Multiple Stack Multiplication Factor ( $n^{0.25}$ )	
<b>Conditions at End (Top) of Jet Phase:</b>					
		Height above Stack $z_{jet}$	75.1 feet*	$z_{jet} = 6.25D$ , meters*=meters above stack top	
		22.900 meters*	155.1 feet	Sect.3/¶1	
		Height above Ground $z_{jet}+h_s$	47.284 meters	"	
		Vertical Velocity $V_{jet}$	18.88 ft/sec	$V_{jet} = 0.5 V_{exit} = V_{exit}/2$	
		5.755 m/s		"	
		Plume Top-Hat Diameter $2a_{jet}$	24.0 feet	$2a_{jet} = 2D$ Conservation of momentum	
<b>Spillane Methodology - Analytical Solutions for Calm Conditions for Plume Heights above Jet Phase</b>					
Single Plume-averaged Vertical Velocity $V$ given by Analytical Solution in Paper where Product $Va$ given by equations below:					
		Plume Top-Hat Radius $a$	Solutions in Table Below		0.16(z-z <sub>v</sub> ), or linear increase with height
		0.410 meters*	1.3 feet*	6.25D[1-( $\theta_s/\theta_a$ ) <sup>1/2</sup> ], meters*=meters above stack top	
		Virtual Source Height $z_v$	81.3 feet	where ( $\theta_s/\theta_a$ ) <sup>1/2</sup> = ( $\theta_s/\theta_a$ ) <sup>1/2</sup> = 0.9821	
		Height above Ground $z_v+h_s$	24.794 meters	Sect.2/Eq.6	
		Vertical Velocity $V$	Solutions in Table Below		$\{(Va)_0^3 + 0.12F_o [(z-z_v)^2 - (6.25D-z_v)^2]^{1/3}\} / a$ Sect.2.1(6)
		Product $(Va)_0$	20.709 m <sup>2</sup> /s	$V_{exit} D/2(\theta_s/\theta_a)^{1/2}$	
<b>Single Chiller Results:</b>					
		Solve for plume-averaged vertical velocity at height	540.0 feet	164.592 meters above ground (z'+h <sub>s</sub> )	
		Gives the following Height above Stack $z'$	140.208 meters*	460.0 feet*	
		Plume Top-Hat Diameter $2a'$	44.736 meters	146.8 feet	
		Vertical Velocity $V$	1.523 m/s	5.00 ft/sec	
				$2a'=2*0.16(z'-z_v)$ Sect.2/Eq.6	
				$V=\{(Va)_0^3+0.12F_o[(z-z_v)^2-(6.25D-z_v)^2]^{1/3}\}/(2a'/2)$ Sect.2/Eq.6	
		Solve for Height of CASC critical vertical velocity $V_{crit}$	5.30 m/s plume-averaged vertical velocity	Critical $VV >$ Top of Jet (Spillane)	
		Find Height above Stack $z_{crit}$	24.974 meters	81.9 feet	
		Height above Ground $z_{crit}+h_s$	49.358 meters	161.9 feet	
				Solve for $x=(z-z_v)$ simultaneously in both eqs. (i.e., $Va$ and $a$ )	
				for $V=V_{crit}$ using the cubic equation $ax^3+bx^2+cx+d=0$ , where	
				$a=1$ , $c=0$ , and $b=-0.12F_o/(V_{crit}^3 \cdot 0.16^3)=-2.64351$	
				and $d=[0.12F_o(6.25D-z_v)^2-(Va)_0^2]/(V_{crit}^3 \cdot 0.16^3)=-13227.21$	
		Interpolated Height of critical vertical velocity in Jet Phase:		<a href="http://www.1728.org/cubic.htm">http://www.1728.org/cubic.htm</a>	
		Find Height above Stack $z_{crit}$	#N/A meters	#N/A feet	
		Height above Ground $z_{crit}+h_s$	#N/A meters	#N/A feet	
				gives the real solution $x = z-z_v = 24.5644$	
				or $z$ (m/above stack) = 24.974	
				$z$ (ft/above ground) = 161.9	
<b>Table of Plume Top-Hat Diameters (2a) and Plume-Averaged Vertical Velocities starting at end of jet phase:</b>					
Height (feet)	(meters)	Plume SingleStk	Plume	Temp(K)	
above ground	above stack	Radius(m)	VertVel(m/s)		
<b>Stack, Rel.Ht = 80.0</b>					
	0.00	1.832	11.51		
100.0	6.10	2.198	10.36		Jet Phase Eqs: 20 ft Intervals
120.0	12.19	2.565	9.21		Linearly interpolated from Stack Rel.Ht to Top of Jet
140.0	18.29	2.931	8.06		Spillane Equations:
<b>Top of Single jet = 155.1</b>					
160.0	24.38	3.298	6.91	306.75	$V_{plume}=\{(Va)_0^3+0.12F_o[(z-z_v)^2-(6.25D-z_v)^2]^{1/3}\}/a$
180.0	30.48	3.664	5.76	306.68	$a = 0.16(z-z_v)$
200.0	36.58	5.787	3.74	306.56	$\theta_p=\theta_a(1+(1-(\theta_s/\theta_a))^{1/2}(V_{exit}D^2/(4V_{plume}^2+a^2\lambda^2)))$
220.0	42.67	6.762	3.28	304.89	CEC Staff Equation:
240.0	48.77	7.737	2.95	304.45	$V_{mp}=0.25V_{sp}$
260.0	54.86	8.713	2.69	304.11	Brigg's Equation:
280.0	60.96	9.688	2.49	303.86	$V_{Briggs}=(2/3) \times 1.6^{(2/3)} \times F_{mp}^{(1/2)} \times U^{(1/2)} \times z^{(1/2)}$
300.0	67.06	10.663	2.32	303.65	where $F_{mp} = nF_{sp}$
320.0	73.15	11.639	2.19	303.48	
350.0	82.30	13.102	2.03	303.34	
400.0	97.54	15.540	1.84	303.17	50 ft Intervals
450.0	112.78	17.979	1.70	302.97	Max<5.3 m/s
500.0	128.02	20.417	1.59	302.82	
550.0	143.26	22.855	1.51	302.72	
600.0	158.50	25.294	1.44	302.64	
650.0	173.74	27.732	1.38	302.57	
700.0	188.98	30.171	1.34	302.53	
800.0	219.46	35.047	1.26	302.49	
900.0	249.94	39.924	1.19	302.43	100 ft Intervals
1000.0	280.42	44.801	1.14	302.39	
1100.0	310.90	49.678	1.10	302.36	
1200.0	341.38	54.555	1.06	302.33	
1300.0	371.86	59.431	1.03	302.32	
1400.0	402.34	64.308	1.00	302.30	
1500.0	432.82	69.185	0.98	302.29	
2000.0	585.22	93.569	0.88	302.28	
2500.0	737.62	117.953	0.81	302.25	500 ft Intervals
3000.0	890.02	142.337	0.76	302.24	
3500.0	1042.42	166.721	0.72	302.23	
4000.0	1194.82	191.105	0.69	302.23	
4500.0	1347.22	215.489	0.66	302.22	
5000.0	1499.62	239.873	0.64	302.22	





MERGED (along length) Plume Average Vertical Velocities for Stacks Chillers using CEC Staff Methodology - Summer Max*					
"Aviation Safety and Buoyant Plumes," Peter Best, et. al.					
"The Evaluation of Maximum Updraft Speeds for Calm Conditions at Various Heights in the Merged Plume from Two Gas-Turbine Power Station at Oaky, Queensland, Australia," Dr. K.T. Spillane					
Ambient Conditions:			Constants: Assume neutral conditions (dθ/dz=0 or θ <sub>s</sub> =θ <sub>a</sub> )		
Ambient Potential Temp θ <sub>a</sub>	302.21 Kelvins	84.3 °F	0.3048 meters/feet		
Plume Exit Conditions:			Gravity g	9.81 m/s <sup>2</sup>	
Stack Height h <sub>s</sub>	24.38 meters	80 feet-inches	λ	1.11	
Individual Stack Diameter D	3.6639445 meters	144.2 inches	λ <sub>0</sub>	-1.0	
Stack Velocity V <sub>exit</sub>	11.51 m/s	37.76 ft/sec	4Vol/(60πD <sup>2</sup> )		
Individual Volumetric Flow	121.36 cu.m/sec	257.143 ACFM	πV <sub>exit</sub> D <sup>2</sup> /4		
Stack Potential Temp θ <sub>s</sub>	313.32 Kelvins	104.3 °F	Sect.2¶1		
Initial Stack Buoyancy Flux F <sub>0</sub>	13.43 m <sup>4</sup> /s <sup>3</sup>	20.0 ΔT(F)	gV <sub>exit</sub> D <sup>2</sup> (1-θ <sub>s</sub> /θ <sub>a</sub> ) <sup>4</sup> = Vol.Flow(g/m <sup>3</sup> )(1-θ <sub>s</sub> /θ <sub>a</sub> )		
Plume Buoyancy Flux F	N/A m <sup>4</sup> /s <sup>3</sup>		λ <sup>2</sup> gV <sub>a</sub> <sup>2</sup> (1-θ <sub>s</sub> /θ <sub>a</sub> ) for a, V <sub>a</sub> , θ <sub>s</sub> at plume height (see below)		
Total Number of Stacks n	42				
Average Adjacent Stack Separation d	13.44 meters	44.1 feet	Calcs based on multiple plume treatment in Peter Best Paper: plume velocities increased by N <sup>0.25</sup> at the height where plumes fully merged (interp. below ht, single merged stack above ht)		
Number of Stacks along Orientation N	6				
Conditions at End (Top) of Jet Phase:					
Height above Stack z <sub>jet</sub>	22.900 meters*	75.1 feet*	z <sub>jet</sub> = 6.25D, meters*=meters above stack top		Sect.3¶1
Height above Ground z <sub>jet</sub> +h <sub>s</sub>	47.284 meters	155.1 feet			
Vertical Velocity V <sub>jet</sub>	5.755 m/s	18.88 ft/sec	V <sub>jet</sub> = 0.5V <sub>exit</sub> = V <sub>exit</sub> /2		*
Plume Top-Hat Diameter 2a <sub>jet</sub>	7.328 meters	24.0 feet	2a <sub>jet</sub> = 2D		Conservation of momentum *
Spillane Methodology - Analytical Solutions for Calm Conditions for Plume Heights above Jet and Merging Phases					
Single Plume-averaged Vertical Velocity V given by Analytical Solution in Paper where Product Va given by equations below:					
Single Plume Values: Plume Top-Hat Radius a		Used in Plume Merging Only		a = 0.16(z-z <sub>v</sub> ), or linear increase with height	
Virtual Source Height z <sub>v</sub>		4.410 meters*		z <sub>v</sub> = 6.25D[1-(θ <sub>s</sub> /θ <sub>a</sub> ) <sup>1/2</sup> ], meters*=meters above stack top	
Height above Ground z <sub>v</sub> +h <sub>s</sub>		24.794 meters		81.3 feet	
Single Plume Values: Vertical Velocity V		Used in Plume Merging Only		((Va) <sup>3</sup> + 0.12F <sub>0</sub> [(z-z <sub>v</sub> ) <sup>2</sup> - (6.25D-z <sub>v</sub> ) <sup>2</sup> ] <sup>1/3</sup> ) / a	
Product (Va) <sub>s</sub>		20.709 m <sup>2</sup> /s		V <sub>exit</sub> (D/2)(θ <sub>s</sub> /θ <sub>a</sub> ) <sup>1/2</sup>	
Sect.2/Eq.6		Sect.2/Eq.6		Sect.2.1(6)	
Plume Merging - Based on Single Plume Calculations where:					
Begin Merging Plume Top-Hat Diameter 2a <sub>touch</sub>		13.440 meters		44.1 feet	
Height above Stack z <sub>touch</sub>		42.410 meters*		139.1 feet*	
Height above Ground z <sub>touch</sub> +h <sub>s</sub>		66.794 meters		219.1 feet	
Vertical Velocity V <sub>touch</sub>		3.300 m/s		10.8 ft/sec	
Total Merging Plume Top-Hat Diameter 2a <sub>full</sub>		67.200 meters		220.5 feet	
Height above Stack z <sub>full</sub>		210.410 meters*		690.3 feet*	
Height above Ground z <sub>full</sub> +h <sub>s</sub>		234.794 meters		770.3 feet	
Vertical Velocity V <sub>full</sub>		1.278 m/s		4.2 ft/sec	
Product (V <sup>3</sup> a) <sub>full</sub>		70 m <sup>4</sup> /s <sup>3</sup>			
Sect.3¶3		Sect.3¶3		Sect.3¶3	
Conditions at End (Top) of Merging Phase - Define new values for V <sub>full</sub> and a <sub>full</sub> in Merged Plume calculations (based on TOTAL number of stacks):					
Merged Plume Values: Plume Diameter 2a		Solutions in Table Below		2a = 2 x (a <sub>m</sub> + 0.16(z-z <sub>full</sub> )), or linear increase with height	
Revised Merged Plume Radius a <sub>m</sub>		85.537 meters		280.6 feet	
Revised Merged Plume Velocity V <sub>m</sub>		3.253 m/s		10.67 ft/sec	
Revised Virtual Source Height z <sub>v,full</sub>		210.410 meters*		690.3 feet*	
Revised Vertical Velocity V		Solutions in Tables Below		Height above stack where Total Merging Occurs (shown above)	
Multiple Plume Calculations		Solve for plume-averaged vertical velocity at height		540.0 feet	
Solve for Height of CASC critical vertical velocity V <sub>crit</sub>		5.30 m/s		Critical VV < Top of Jet	
Table of MERGED Plume-Averaged Vertical Velocities starting at Touching Height:		Height (feet)		Plume Vert.	
		above ground		above stack Radius(m)	
		Vel(m/s)			
Begin Merging (touch) = 219.1		42.40		6.720	
		220.0		42.67	
		240.0		48.77	
		260.0		54.86	
		280.0		60.96	
		300.0		67.06	
		320.0		73.15	
		340.0		79.25	
		360.0		85.34	
		380.0		91.44	
		400.0		97.54	
		450.0		112.78	
		500.0		128.02	
		550.0		143.26	
		600.0		158.50	
		700.0		188.98	
End Merging (full/mp) = 770.3		210.40		85.536	
		800.0		219.46	
		900.0		249.94	
		1000.0		280.42	
		1100.0		310.90	
		1200.0		341.38	
		1300.0		371.86	
		1400.0		402.34	
		1500.0		432.82	
		2000.0		585.22	
		2500.0		737.62	
		3000.0		890.02	
		3500.0		1042.42	
		4000.0		1194.82	
		4500.0		1347.22	



MERGED (along width) Plume Average Vertical Velocities for Stacks Chillers using CEC Staff Methodology - Summer Max*					
*Aviation Safety and Buoyant Plumes,* Peter Best, et. al.					
*The Evaluation of Maximum Updraft Speeds for Calm Conditions at Various Heights in the Merged Plume from Two Gas-Turbine Power Station at Oakey, Queensland, Australia,* Dr. K.T. Spillane					
Ambient Conditions:			Constants: Assume neutral conditions (dB/dz=0 or $\theta_a=\theta_b$ )		
Ambient Potential Temp $\theta_a$	302.21 Kelvins	84.3 °F	0.3048 meters/feet		
<b>Plume Exit Conditions:</b>					
Stack Height $h_s$	24.38 meters	80 feet-inches	Gravity g	9.81 m/s <sup>2</sup>	
Individual Stack Diameter D	3.663945 meters	144.2 inches	$\lambda$	1.11	
Stack Velocity $V_{exit}$	11.51 m/s	37.76 ft/sec	$\lambda_b$	~1.0	
Individual Volumetric Flow	121.36 cu.m/sec	257,143 ACFM	$4V_{exit}/(60mD^2)$	Sect.2/¶1	
Stack Potential Temp $\theta_s$	313.32 Kelvins	104.3 °F	$\pi V_{exit}D^2/4$	Sect.2/¶1	
Initial Stack Buoyancy Flux $F_0$	13.43 m <sup>3</sup> /s <sup>3</sup>	20.0 ΔT(F)	$gV_{exit}D^2(1-\theta_s/\theta_a)/4 = Vol.Flow(g/m)(1-\theta_s/\theta_a)$	Sect.2/¶1	
Plume Buoyancy Flux F	N/A m <sup>3</sup> /s <sup>3</sup>		$\lambda^2 g Va^2(1-\theta_s/\theta_p)$ for a, V, $\theta_p$ at plume height (see below)		
Total Number of Stacks n	42				
Average Adjacent Stack Separation d	8.25 meters	27.1 feet	Calcs based on multiple plume treatment in Peter Best Paper:		
Number of Stacks along Orientation N	8		plume velocities increased by $N^{0.25}$ at the height where plumes fully merged (interp. below ht, single merged stack above ht)		
<b>Conditions at End (Top) of Jet Phase:</b>					
Height above Stack $z_{jet}$	22.900 meters*	75.1 feet*	$z_{jet} = 6.25D$ , meters*=meters above stack top	Sect.3/¶1	
Height above Ground $z_{jet}+h_s$	47.284 meters	155.1 feet		*	
Vertical Velocity $V_{jet}$	5.755 m/s	18.88 ft/sec	$V_{jet} = 0.5V_{exit} = V_{exit}/2$	*	
Plume Top-Hat Diameter $2a_{jet}$	7.328 meters	24.0 feet	$2a_{jet} = 2D$	Conservation of momentum *	
<b>Spillane Methodology - Analytical Solutions for Calm Conditions for Plume Heights above Jet and Merging Phases</b>					
Single Plume-averaged Vertical Velocity V given by Analytical Solution in Paper where Product Va given by equations below:					
Single Plume Values: Plume Top-Hat Radius a			Used in Plume Merging Only		
Virtual Source Height $z_v$	0.410 meters*	1.3 feet*	$a = 0.16(z-z_v)$ , or linear increase with height	Sect.2/Eq.6	
Height above Ground $z_v+h_s$	24.794 meters	81.3 feet	$z_v = 6.25D[1-(\theta_s/\theta_a)]^{1/2}$ , meters*=meters above stack top	Sect.2/Eq.6	
Single Plume Values: Vertical Velocity V			Used in Plume Merging Only		
Product (Va) <sub>0</sub>	20.709 m <sup>3</sup> /s		$\{(Va)_0^3 + 0.12F_0 [(z-z_v)^2 - (6.25D-z_v)^2]\}^{1/3} / a$	Sect.2.1(6)	
Plume Merging - Based on Single Plume Calculations where:			Sect.3/¶3		
Begin Merging Plume Top-Hat Diameter $2a_{touch}$	8.250 meters	27.1 feet	$2a_{touch}=d$ , (or $a_{touch}=d/2$ )		
Height above Stack $z_{touch}$	26.191 meters*	85.9 feet*	$z_{touch} = z_v + d/(2*0.16)$ , meters*=meters above stack top		
Height above Ground $z_{touch}+h_s$	50.575 meters	165.9 feet			
Vertical Velocity $V_{touch}$	5.068 m/s	16.6 ft/sec	$V_{touch} = \{(Va)_0^3 + 0.12F_0 [(z-z_v)^2 - (6.25D-z_v)^2]\}^{1/3} / a$		
Total Merging Plume Top-Hat Diameter $2a_{full}$	57.750 meters	189.5 feet	$2a_{full}=2d(N-1)^2$ , (or $a_{full}=d(N-1)^2$ ) FOR 2 STACKS, $2a_{full}=2d$		
Height above Stack $z_{full}$	180.878 meters*	593.4 feet*	$z_{full} = z_v + 2d/(2*0.16)$ , meters*=meters above stack top		
Height above Ground $z_{full}+h_s$	205.262 meters	673.4 feet			
Vertical Velocity $V_{full}$	1.360 m/s	4.5 ft/sec	$V_{full} = \{(Va)_0^3 + 0.12F_0 [(z_{full}-z_v)^2 - (6.25D-z_v)^2]\}^{1/3} / a_{full}$		
Product (V <sup>3</sup> a) <sub>full</sub>	73 m <sup>4</sup> /s <sup>3</sup>				
<b>Conditions at End (Top) of Merging Phase - Define new values for <math>V_{full}</math> and <math>a_{full}</math> in Merged Plume calculations (based on TOTAL number of stacks):</b>					
Merged Plume Values: Plume Diameter $2a$			Solutions in Table Below		
Revised Merged Plume Radius $a_m$	73.508 meters	241.2 feet	$2a = 2x (a_m + 0.16(z-z_{full}))$ , or linear increase with height		
Revised Merged Plume Velocity $V_m$	3.462 m/s	11.36 ft/sec	where $a_m = n^{0.25}a_{full}$ where Total Merging Occurs		
Revised Virtual Source Height $z_{full}$	180.878 meters*	593.4 feet*	and $V_m = n^{0.25}V_{full}$ where Total Merging Occurs		
Revised Vertical Velocity V			Height above stack where Total Merging Occurs (shown above)		
Solutions in Tables Below			$V = [n(V^3a)_{full}]^{1/3}$ for heights above total merging elevation		
Multiple Plume Calculations			$V = V_{touch} + (V_m - V_{touch})^2 (z - z_{touch}) / (z_{full} - z_{touch})$		
Solve for plume-averaged vertical velocity at height			for heights below total merging elevation		
Height above Stack z	540.0 feet	164.592 meters above ground (z+h <sub>s</sub> )	LESS THAN TOP OF MERGING PHASE-INTERPOLATE		
Plume Top-Hat Radius a	#N/A meters	#N/A feet	$a = a_m + 0.16(z - z_{full})$ if $z > z_{full}$		
Vertical Velocity V	3.885 m/s	12.74 ft/sec	$V = [n(V^3a)_{full}]^{1/3}$ if $z > z_{full}$		
Solve for Height of CASC critical vertical velocity $V_{crit}$			Critical VV < Top of Jet		
Find Height above Stack $z_{crit}$	JET meters	JET feet	BEFORE TOUCHING		
Height above Ground $z_{crit}+h_s$	JET meters	JET feet	$z_{crit} = z_{full} + \{[n(V^3a)_{full}/(V_{crit})^3] - a_m\} / 0.16$ if $V_{crit} < V_m$		
Table of MERGED Plume-Averaged Vertical Velocities starting at Touching Height:			Single Plume Eqns (see Single Plume spreadsheet)		
Height (feet)	(meters)	Plume Radius(m)	Vert. Vel(m/s)	$V_{plume} = \{(Va)_0^3 + 0.12F_0 [(z-z_v)^2 - (6.25D-z_v)^2]\}^{1/3} / a$	
Begin Merging (touch) = 165.9	26.18	4.125	5.07	$a = 0.16(z-z_v)$	
180.0	30.48	#N/A	5.02	$\theta_s = \theta_a(1 + (1 - \theta_s/\theta_a)(V_{exit}D^2/(4V_{plume}a^2a^2)))$	
200.0	36.58	#N/A	4.96	Interpolated Layer Eqns	
220.0	42.67	#N/A	4.90	$V = V_{touch} + (V_m - V_{touch})^2 (z - z_{touch}) / (z_{full} - z_{touch})$	
240.0	48.77	#N/A	4.83		
260.0	54.86	#N/A	4.77		
280.0	60.96	#N/A	4.71		
300.0	67.06	#N/A	4.64	50 ft Intervals	
350.0	82.30	#N/A	4.49		
400.0	97.54	#N/A	4.33		
450.0	112.78	#N/A	4.17		
500.0	128.02	#N/A	4.01		
550.0	143.26	#N/A	3.85		
600.0	158.50	#N/A	3.69		
650.0	173.74	#N/A	3.54		
End Merging (full/mp) = 673.4	180.87	73.508	3.46		
700.0	188.98	74.804	3.38	100 ft Intervals	
800.0	219.46	79.680	3.06		
900.0	249.94	84.557	2.75		
1000.0	280.42	89.434	2.43		
1100.0	310.90	94.311	2.11		
1200.0	341.38	99.188	3.46	Merged Plume Eqns	
1200.0	341.38	99.188	3.13	$V = [n(V^3a)_{full}]^{1/3}$	
1300.0	371.86	104.064	3.08	$a = a_m + 0.16(z - z_{full})$	
1500.0	432.82	113.818	2.99		
2000.0	585.22	138.202	2.81		
2500.0	737.62	162.586	2.66	500 ft Intervals	
3000.0	890.02	186.970	2.54		
3500.0	1042.42	211.354	2.43		
4000.0	1194.82	235.738	2.35		
4500.0	1347.22	260.122	2.27		
5000.0	1499.62	284.506	2.21		

