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Vertical Plume Velocity Assessment

Lafayette Backup Generating Facility

Santa Clara, California

Submitted to
California Energy Commission

Submitted by



Prepared by
Atmospheric Dynamics, Inc.



ATMOSPHERIC DYNAMICS, INC
Meteorological & Air Quality Modeling

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Introduction

This report presents the evaluation of the Lafayette Backup Generating Facility (LBGF) source generated plumes from the 46 Cummins diesel engines and 88 rooftop chillers on the effects on airport/aircraft operations. The Normal Y. Mineta San Jose International Airport is located approximately 0.38 miles east southeast of the LBGF. This report is based upon an analysis prepared by Atmospheric Dynamics, Inc. in accordance with the California Energy Commission (CEC) application requirements for a Small Power Plant Exemption (SPPE) pursuant to the power plant siting regulations. This analysis is but one part of a larger analysis, which seeks an SPPE Decision from the CEC.

Based on the stack parameter data, an analysis of the potential plume characteristics from the routine operation the diesel engines and rooftop chillers on vertical winds was prepared and compared to the California Energy Commission (CEC) significance criteria of 5.3 meters per second (m/s) for the average vertical plume velocities as described below.

Atmospheric Dynamics, Inc. (ADI) prepared a screening level plume vertical velocity assessment which are based on the calm wind Spillane methodology outlined in the *“Aviation Safety and Buoyant Plumes”* paper (Peter Best, et. al., presented at the Clean Air Conference, Newcastle, New South Wales, Australia, 2003). This methodology is also recognized as a screening tool for aviation safety set out by the Australian Civil Aviation Safety Authority (CASA) and presented in *“AC 139-5(1) Plume Rise Assessments (CASA, 2012)”*.

The aim of this screening assessment is to conservatively determine the potential for turbulence generated by the diesel engines and rooftop chillers waste heat exhaust plumes. Part 139.370 of the Australian Civil Aviation Safety Regulations (1998, 2004) provides that CASA may determine that plume velocities in excess of 4.3 m/s is or will be a potential hazard to aircraft operations. The *Manual of Aviation Meteorology* (Australian Bureau of Meteorology 2003) defines severe turbulence as a vertical wind gust velocity in excess of 10.6 m/s. The assumed critical vertical velocity used as a CEC significance threshold is 5.3 meters per second* (m/s) but it should be noted that the basis of the original CASA derived threshold of 4.3 m/s has been lost in antiquity and that CASA no longer relies on the 1998 and 2004 regulations that established this critical threshold other than to note that a more rigorous analysis, which includes site specific meteorology, should be used if the 4.3 m/s and 10.6 m/s screening thresholds are exceeded. The screening method uses absolute worst-case assumptions of calm winds and neutral atmospheric conditions for the entire vertical extent of the plume to determine these worst-case impacts. It should be noted that these results are extremely conservative in that these worst-case conditions typically only occur during a few hours each year.

The Spillane methodology is generally applied to a limited number of plume source geometry's (turbines, power plant boilers, etc.) with the stacks arranged linearly (in a single straight-line) and separated by distances that typically exceed the individual stack diameters. For the diesel engines, this assumption was maintained. Only one engine stack was modeled consistent with the normal operational testing schedule of the emergency generator engines. For the chiller assessment, a conservative assumption was made in order to use the Spillane methodology on an atypical chiller plume configuration, which is made up of 88 chillers arranged on a two-dimensional surface. Here, the methodology, as described below, assumed that all sixteen chiller cells for each chiller were merged into a single stack with an effective diameter based on the combined area of all sixteen chiller cells. In other words, a single stack was assumed to initially

*For the Puente Power Project (Docket#15-AFC-01, TN#213674, 9/15/2016), “CEC staff ... concluded that an average velocity of 5.3 m/s is the appropriate velocity ... [for a plume velocity threshold].” The CEC staff “Plume Background Threshold” attached to the docketed document concludes with “...[CEC] staff will use 10.6 m/s peak vertical plume velocity as the new threshold. The altitude at which a plume would have a peak vertical velocity of 10.6 m/s would be the same altitude at which a plume would have an average vertical velocity of half that, 5.3 m/s.”



describe the release parameters of the combined chiller cells in each of the 88 individual chillers. The effective plume diameter is appropriate for each individual chiller based on the close proximity and arrangement of the sixteen chiller cells.

Screening Methodology and Vertical Plume Velocity Calculations

The Spillane methodology is based on worst-case calm wind neutral stability conditions to assess the average plume vertical velocity as a function of height. The methodology is based on well-verified laboratory and theoretical treatments of the rise and spread of a buoyant jet, both into a still ambient environment and into a light crosswind. This treatment covers in detail the initial dynamics of the plume as it exits the stack and the entrainment of ambient air into the plume as it rises directly above the stack. In addition to providing clarifications and algebraic solutions to the Spillane methodology, the 2003 Peter Best paper provides additional methodologies that also consider the enhancement of vertical velocities that may occur if the plumes from multiple identical stacks merge and form a higher buoyancy combined plume (referred to here as the enhanced Spillane methodology).

The vertical plume assessment will involve several stages of development. For individual plumes, the stages are:

- (a) In the first stage very close to the stack exit, the high plume momentum will result in a short section in which the conditions at the center of the plume are relatively unaffected by ambient and plume buoyancy conditions. This jet phase extends from the stack exit to approximately a distance of 6.25 D above the stack (where D is the stack diameter) in calm conditions. At the end of this stage, the plume-averaged vertical velocity has decreased to half of the stack exit velocity, with a corresponding increase, or doubling, in effective plume diameter.
- (b) In the second stage, the plume responds to differences between ambient and plume buoyancy conditions, with much cooler and less turbulent ambient air being entrained into the plume from the outside regions of the plume towards the plume centerline. The momentum and buoyancy of the plume significantly influences plume rise and subsequently the dilution of the stack exhaust to decrease plume vertical velocities. This dilution is very sensitive to ambient wind speed, so the calm wind conditions considered here are extremely conservative.
- (c) In the third stage of plume development, plume rise is due entirely to the buoyancy of the plume and continues from some distance until there is an equalization of turbulence conditions within and outside the plume. This final rise is often only achieved at considerable heights/distances from the stack where the effective average vertical velocity is then close to zero. Since there is very little turbulence and near-zero vertical velocities, this stage of plume development is usually not considered for this type of analysis.

In the second stage of development, the analytical solution of the governing equations under these conditions is given by:

$$a = 0.16(z - z_v)$$

$$V = \{ (Va) \sigma^3 + 0.12Fo [(z - z_v)^2 - (6.25D - z_v)^2] \}^{1/3} / a$$



Where the subscript 'o' refers to values of the parameters at the stack outlet and the variables are:

a	plume radius (m)
V	average vertical velocity (m/s)
z	height above stack top (m)
z_v	virtual source height (m)
D	stack diameter (m)
F_o	buoyancy flux evaluated at the stack outlet (m^4s^{-3})

These are the two primary equations governing the growth of a single plume in the second stage of development under neutral calm wind conditions. Additional equations governing the first stage of single plume development as well as the interaction of multiple plumes in the second stage of development are discussed in detail in the Best paper.

For multiple stacks in the enhanced Spillane methodology, the equations governing the second stage are calculated from the point when the plumes begin to merge until they are fully merged. The plume merging begins at the height where the plume diameters equal the stack separations and the plumes are fully merged at the height where the plume diameters are equal to $2d(N-1)/2$ for three or more stacks or $2d$ for two stacks. At the fully merged height, the merged plume diameter and velocity is enhanced by the fourth root of the number of stacks. Above the fully merged plume height, the enhanced plume diameter and plume velocities follow the regular equations given for the second stage. Below the fully merged plume height for the merging phase, plume velocities are linearly interpolated by height from the single plume velocity at the height where the plumes begin to merge to the enhanced plume velocity at the fully merged plume height.

Vertical Plume Velocity Calculations for the Diesel Engines

The LBGF is comprised of 44 individual large and one (1) small diesel emergency generator stacks. The small diesel emergency generator was not assessed as it would have smaller plume vertical velocities. Generator stack parameter data (plume exit velocity, plume exit temperature and stack exit diameter) were provided by Cummins. Only one (1) engine will be tested during any one hour. While the engines will be tested at minimum loads, the 100 percent load case was utilized for the worst-case plume analysis. For the engine analysis, two ambient conditions were considered: 41.0°F, the minimum monthly mean of daily minimum temperatures, and 84.3°F, the maximum monthly mean of daily maximum temperatures for the San Jose Airport (*"Climatology of the United States No. 81 – Monthly Station Normals of Temperature, Precipitation, and Heating and Cooling Degree Days 1971-2000 – California"*, February 2002, and *"Climatology of the United States No 20 – Monthly Station Climate Summaries, 1971-2000 – California"*, February 2004). These data is summarized in Table 1.



Table 1 Cummins Diesel Stack Characteristics for Vertical Plume Velocity Analysis			
	Case #	1	2
Ambient Temperature (°F)*		41.0	41.0
Stack Diameter (m)		0.7112	0.7112
Exhaust Velocity (m/s)*		31.20	31.20
Exhaust Temperature (K)*		912.0	912.0
Stack Release Height (m)		22.86	22.86
Stack Buoyancy Flux (m ⁴ /s ³)		24.58	23.35
*Stack data provided by Cummins at 100% load			

Screening level vertical plume velocity assessments were made for two ambient temperatures with calm winds and neutral atmospheric conditions for the cases presented in Table 1 which are based on 100 percent load. The results based on the two ambient conditions are presented in Table 2 and the output from the calculation spreadsheet provided in Attachment A.

The initial jet phase extends to a height of about 90 feet above grade level (ft-agl) for both cases. After the jet phase, plume temperature buoyancy characteristics modeled in the Spillane methodology cause a uniform decrease in plume-averaged vertical velocities, with the critical plume-averaged vertical velocity of 5.3 m/s occurring at about 113 ft-agl for both cases

Table 2 Diesel Engine Vertical Plume Velocity Analysis Results for Reference Height			
	Case #	1	2
Ambient Temperature (°F)		41.0	84.3
Single Plume Results:			
Plume-Averaged Vertical Velocity at 200 feet-agl (m/s)		2.77	2.73
Height of 5.3 m/s Plume-Averaged Vertical Velocity (feet-agl)		112.8	112.9

These screening results indicate that mechanical and thermal turbulence levels due to the flow from the diesel engine always remain in the light turbulence category and below the significance level of 5.3 m/s at all heights above about 113 ft-agl. Even light wind speeds can dramatically decrease the predicted plume-averaged vertical velocities, so the above results are very conservative indications of adverse conditions. The important factor for a given location is the appropriateness of available information for estimating true wind and temperature profiles throughout a typical year. Theoretical calculations, as shown in the tables above, are likely to overestimate the expected vertical velocities, for the following reasons:

- The wind profile is assumed constant with height with no occurrence of wind-shear when realistically, there is a considerable variation with height, especially in light winds;
- Worst-case scenarios are based on very light-wind, near-neutral atmospheric conditions with maximum loading.

Vertical Plume Velocity Calculations for the Rooftop Chillers

The 88 rooftop chillers are each comprised of 20 individual cells, with a cell fan diameter of 34 inches. The 88 chillers are generally arranged 24 along the longer building length (averaging 15 feet between adjacent chillers) by three along the shorter building width (averaging 15 feet between adjacent chillers). It should be noted that the chillers are arranged differently on the two-story part of the data center (8x2). Based on the groupings of chillers, the single and merged



plumes were based on the 24 (3x8) chiller arrangement merging plumes along the length (3 merged stacks) and width (8 merged stacks). Chiller stack parameter data (exit velocity and temperature) were provided by the applicant. An effective stack diameter for all 20 cells was utilized for each chiller. The chillers will utilize variable speed fans and the number of fans that are operational are dependent upon ambient temperature and plant load. However, to be conservative, all chillers/cells were assumed to be operating at full load. These data are summarized in Table 3 for the same ambient temperatures used for the engine analysis.

Table 3 Chiller Stack Characteristics for Vertical Plume Velocity Analysis			
	Case #	1	2
Ambient Temperature (°F)*		41.0	84.3
Effective Stack Diameter (m)**		3.86	3.86
Exhaust Velocity (m/s)*		8.06	8.06
Exhaust Temperature (K)*		289.26	313.32
Stack Release Height (m)		23.81	23.81
Stack Buoyancy Flux (m ⁴ /s ³)		11.33	10.45
*Chiller stack data provided by the applicant			
** Calculated value based on the cell diameter of 34 inches multiplied by the square of the number of operating cells, or $D_{\text{eff}} = 34 \sqrt{20}$			

The Spillane methodology was originally developed to treat multiple individual stacks that are arranged along a linear x or y direction, but not both directions at once, with stack separations much greater than the stack diameters, typical of boilers/turbines at large power plants. As noted above, the 88 chillers are generally arranged in a 3 x 8 pattern. Therefore, the enhanced Spillane methodology was based on calculating the total merging height for the largest linear direction of chiller placements (which is eight chillers spaced 24.6 feet apart along the longer length of the building). The largest grouping of 48 (3x16) chillers were considered in the calculation of vertical velocity plume enhancement (both at and above the totally merged height, and for the interpolation down to the plume touching height). Again, the effective single stack diameter of each chiller was based on the combined 20 cells.

Screening level vertical plume velocity assessments were made for the same ambient temperatures with calm winds and neutral atmospheric conditions as was done for the emergency generator engines. The results are presented in Table 4 and the output from the calculation spreadsheets are provided in Attachment A.

The initial jet phase extends to a height of about 157.3 ft-agl for both cases. The critical plume-averaged vertical velocity of 5.3 m/s occurs in the jet phase at about 132.4 ft-agl for both cases. The plumes touch (begin to merge) at about 246 ft-agl and are fully merged at about 1,233 ft-agl for both cases. Under the enhanced Spillane methodology, the merged plume-averaged vertical velocities never approach 5.3 m/s (either above the totally merged height or when interpolated down to the touching height).



Table 4 Chiller Vertical Plume Velocity Analysis Results for Reference Height		
Case #	1	2
Ambient Temperature (°F)	41.0	84.3
Single Plume Results:		
Height of 5.3 m/s Plume-Averaged Vertical Velocity (Within the Jet Phase, feet-agl)	132.4	132.4
Merged Plume Results:		
Plume-Averaged Vertical Velocity at 1,000 feet-agl (m/s)	3.50	3.42

From these results and for each ambient condition, the vertical plume velocities are less than the threshold value of 5.3 m/s for all heights above about 132 ft-agl and above for the chillers. The heights at which plume-averaged vertical velocities exceed 5.3 m/s only occur during the jet phase for both cases. These cases also represent worst-case conditions of calm winds at all levels of a neutral atmosphere.

These screening results indicate that mechanical and thermal turbulence levels due to the flow from the chillers always remain in the light turbulence category and below the significance level of 5.3 m/s at all heights above about 132 ft-agl. Even light wind speeds can dramatically decrease the predicted plume-averaged vertical velocities so the above results are very conservative indications of adverse conditions. The important factor for a given location is the appropriateness of available information for estimating true wind and temperature profiles throughout a typical year. Theoretical calculations, as shown in the tables above, are likely to overestimate the expected vertical velocities, for the following reasons:

- The wind profile is assumed constant with height with no occurrence of wind-shear when realistically, there is a considerable variation with height, especially in light winds;
- Worst-case scenarios are based on very light-wind, near-neutral atmospheric conditions with maximum loading.



Attachment A
Spillane Method Plume Velocity Calculations



SINGLE Plume Average Vertical Velocities for Lafayette Large Emer.Gen Engine, 100% Load, and Maximum Stack Height - Winter Min*					
"A Aviation Safety and Buoyant Plumes," Peter Best, et. al.					
"The Evaluation of Maximum Updraft Speeds for Calm Conditions at Various Heights in the Plume from a Gas-Turbine Power Station at Oakey, Queensland, Australia," Dr. K.T. Spillane					
Ambient Conditions:			Constants: Assume neutral conditions (dθ/dz=0 or θ _a =θ _s)		
Ambient Potential Temp θ _a	278.15 Kelvins	41.0 °F		0.3048 meters/feet	
Plume Exit Conditions:			Gravity g	9.81 m/s ²	
Maximum Stack Height h _s	22.86 meters	75 feet-inches	λ	1.11	
Stack Diameter D	0.7112 meters	28 inches	λ ₀	-1.0	
Stack Velocity V _{exit}	31.20 m/s	102.37 ft/sec			
Volumetric Flow	12.39 cu.m/sec	26,264 ACFM	πV _{exit} D ² /4		Sect.2/¶1
Stack Potential Temp θ _s	762.04 Kelvins	912 °F			
Initial Stack Buoyancy Flux F ₀	24.5763 m ³ /s ³		gV _{exit} D ² (1-θ _a /θ _s)/4 = Vol.Flow(g/π)(1-θ _a /θ _s)		Sect.2/¶1
Plume Buoyancy Flux F	N/A m ⁴ /s ³		λ ² gVa ² (1-θ _a /θ _p) for a,V,θ _p at plume height (see below)		
No.of Stacks N	1		1.000 Multiple Stack Multiplication Factor (N ^{0.25})		
Conditions at End (Top) of Jet Phase:					
Height above Stack z _{jet}	4.445 meters*	14.6 feet*	z _{jet} = 6.25D, meters*=meters above stack top		Sect.3/¶1
Height above Ground z _{jet} +h _s	27.305 meters	89.6 feet			*
Vertical Velocity V _{jet}	15.600 m/s	51.18 ft/sec	V _{jet} = 0.5V _{exit} = V _{exit} /2		*
Plume Top-Hat Diameter 2a _{jet}	1.422 meters	4.7 feet	2a _{jet} = 2D	Conservation of momentum	*
Spillane Methodology - Analytical Solutions for Calm Conditions for Plume Heights above Jet Phase					
Single Plume-averaged Vertical Velocity V given by Analytical Solution in Paper where Product Va given by equations below:					
Plume Top-Hat Radius a	Solutions in Table Below		0.16(z-z _v), or linear increase with height		Sect.2/Eq.6
Virtual Source Height z _v	1.760 meters*	5.8 feet*	6.25D[1-(θ _a /θ _s) ^{1/2}], meters*=meters above stack top		Sect.2/Eq.6
Height above Ground z _v +h _s	24.620 meters	80.8 feet	where (θ _a /θ _s) ^{1/2} = (θ _a /θ _s) ^{1/2} = 0.6042		
Vertical Velocity V	Solutions in Table Below		{(Va) ₀ ³ + 0.12F ₀ [(z-z _v) ² - (6.25D-z _v) ²] ^(1/3) / a		Sect.2.1(6)
Product (Va) ₀	6.703 m ² /s		V _{exit} D/2(θ _a /θ _s) ^{1/2}		
Solve for plume-averaged vertical velocity at height 200.0 feet 60.96 meters above ground (z'+h _s)					
Gives the following Height above Stack z'	38.100 meters*	125.0 feet*			
Plume Top-Hat Diameter 2a'	11.629 meters	38.2 feet	2a'=2*0.16(z'-z _v)		Sect.2/Eq.6
Vertical Velocity V	2.769 m/s	9.09 ft/sec	V={(Va) ₀ ³ +0.12F ₀ [(z'-z _v) ² -(6.25D-z _v) ²] ^(1/3) }/(2a'/2)		Sect.2/Eq.6
Solve for Height of CASC critical vertical velocity V _{crit} 5.30 m/s plume-averaged vertical velocity Critical VV > Top of Jet (Spillane)					
Find Height above Stack z _{crit}	11.519 meters	37.8 feet	Solve for x=(z-z _v) simultaneously in both eqs. (i.e., Va and a)		
Height above Ground z _{crit} +h _s	34.379 meters	112.8 feet	for V=4.3 m/s using the cubic equation ax ³ +bx ² +cx+d=0, where		
Interpolated Height of critical vertical velocity in Jet Phase:				a=1, c=0, and b=(-0.12F ₀)/(4.3 ³ 0.16 ³)=	-4.8363
Find Height above Stack z _{crit}	#/N/A meters	#/N/A feet	and d=[0.12F ₀ (6.25D-z _v) ² -(Va) ₀ ³]/(4.3 ³ 0.16 ³)=		-459.00
Height above Ground z _{crit} +h _s	#/N/A meters	#/N/A feet	http://www.1728.org/cubic.htm		
				gives the real solution x = z-z _v =	9.7599
				or z(m/above stack) =	11.519
				z(ft/above ground) =	112.8
Table of Plume Top-Hat Diameters (2a) and Plume-Averaged Vertical Velocities starting at end of jet phase:					
Height (feet)	(meters)	Plume	SingleStk	Plume	
above ground	above stack	Radius(m)	VertVel(m/s)	Temp(K)	
Stack.Rel.Ht = 75.0					
	0.00	0.356	31.20		
80.0	1.52	0.477	25.86		Jet Phase Eqs: 5 foot Intervals
85.0	3.05	0.599	20.52		Linearly interpolated from Stack Rel.Ht to Top of Jet
Top of jet = 89.6					
	4.45	0.711	15.60		Spillane Equations:
90.0	4.57	0.450	14.93	465.22	V _{plume} ={(Va) ₀ ³ +0.12F ₀ [(z-z _v) ² -(6.25D-z _v) ²] ^(1/3) }/a
100.0	7.62	0.938	7.73	361.34	a = 0.16(z-z _v)
110.0	10.67	1.425	5.62	327.69	θ _s =θ _a (1+(1-θ _a /θ _s))*(V _{exit} D ² /(4V _{plume} *a ² *λ ²))
Spillane 5.3 m/s Height = 112.8					
120.0	13.72	1.913	4.64	311.42	
130.0	16.76	2.401	4.09	302.17	
140.0	19.81	2.888	3.72	296.37	Max<5.30 m/s
150.0	22.86	3.376	3.46	292.49	
160.0	25.91	3.864	3.26	289.77	
170.0	28.96	4.351	3.10	287.78	
220.0	44.20	6.790	2.61	282.84	50 foot Intervals
270.0	59.44	9.228	2.34	280.99	
320.0	74.68	11.667	2.16	280.08	
370.0	89.92	14.105	2.02	279.56	
420.0	105.16	16.543	1.92	279.23	
470.0	120.40	18.982	1.83	279.01	
520.0	135.64	21.420	1.76	278.85	
620.0	166.12	26.297	1.64	278.65	100 foot Intervals
720.0	196.60	31.174	1.55	278.53	
820.0	227.08	36.051	1.47	278.45	
920.0	257.56	40.927	1.41	278.39	
1020.0	288.04	45.804	1.36	278.35	
1120.0	318.52	50.681	1.32	278.32	
1220.0	349.00	55.558	1.28	278.29	
1320.0	379.48	60.435	1.24	278.27	
1420.0	409.96	65.311	1.21	278.26	
1520.0	440.44	70.188	1.18	278.25	
1620.0	470.92	75.065	1.15	278.24	
1720.0	501.40	79.942	1.13	278.23	
1820.0	531.88	84.819	1.11	278.22	
1920.0	562.36	89.695	1.09	278.21	
2020.0	592.84	94.572	1.07	278.21	

*Winter Min = Monthly Mean of Minimum Daily Temperatures for 1971-2000 (Lowest in December)
 NOAA Sources: Climatology of the United States No.81 "Monthly Station Normals of Temperatures, Precipitation, and Heating and Cooling Degree Days, 1971-2000 California" and Climatology of the United States No. 20 "Monthly Station Climate Summaries, 1971-2000 California"



SINGLE Plume Average Vertical Velocities for Single LBGF Large Emer.Gen Engine, 100% Load, and Maximum Stack Height - Summer Max*						
"Aviation Safety and Buoyant Plumes," Peter Best, et. al.						
"The Evaluation of Maximum Updraft Speeds for Calm Conditions at Various Heights in the Plume from a Gas-Turbine Power Station at Oakey, Queensland, Australia," Dr. K.T. Spillane						
Ambient Conditions:			Constants: Assume neutral conditions (dθ/dz=0 or θ _a =θ _s)			
Ambient Potential Temp θ _a	302.21	Kelvins	84.3	°F		0.3048 meters/feet
Plume Exit Conditions:			Gravity g	9.81	m/s ²	
Maximum Stack Height h _s	22.86	meters	75	feet-inches	λ	1.11
Stack Diameter D	0.7112	meters	28	inches	λ ₀	~1.0
Stack Velocity V _{exit}	31.20	m/s	102.37	ft/sec		
Volumetric Flow	12.39	cu.m/sec	26,264	ACFM	πV _{exit} D ² /4	Sect.2/¶1
Stack Potential Temp θ _s	762.04	Kelvins	912	°F		
Initial Stack Buoyancy Flux F ₀	23.3543	m ³ /s ³			gV _{exit} D ² (1-θ _s /θ _a)/4 = Vol.Flow(g/π)(1-θ _s /θ _a)	Sect.2/¶1
Plume Buoyancy Flux F	N/A	m ³ /s ³			λ ² gVa ² (1-θ _s /θ _a) for a,V,θ _s at plume height (see below)	
No.of Stacks N	1		1.000	Multiple Stack Multiplication Factor (N ^{0.25})		
Conditions at End (Top) of Jet Phase:						
Height above Stack z _{jet}	4.445	meters*	14.6	feet*	z _{jet} = 6.25D, meters*=meters above stack top	Sect.3/¶1
Height above Ground z _{jet} +h _s	27.305	meters	89.6	feet		"
Vertical Velocity V _{jet}	15.600	m/s	51.18	ft/sec	V _{jet} = 0.5V _{exit} = V _{exit} /2	"
Plume Top-Hat Diameter 2a _{jet}	1.422	meters	4.7	feet	2a _{jet} = 2D	Conservation of momentum
Spillane Methodology - Analytical Solutions for Calm Conditions for Plume Heights above Jet Phase						
Single Plume-averaged Vertical Velocity V given by Analytical Solution in Paper where Product Va given by equations below:						
Plume Top-Hat Radius a	Solutions in Table Below			0.16(z-z _v), or linear increase with height		Sect.2/Eq.6
Virtual Source Height z _v	1.646	meters*	5.4	feet*	6.25D[1-(θ _s /θ _a) ^{1/2}], meters*=meters above stack top	Sect.2/Eq.6
Height above Ground z _v +h _s	24.506	meters	80.4	feet	where (θ _s /θ _a) ^{1/2} = (θ _s /θ _a) ^{1/2} = 0.6297	
Vertical Velocity V	Solutions in Table Below			{(Va) ₀ ³ + 0.12F ₀ [(z-z _v) ² - (6.25D-z _v) ²] ^{1/3} / a		Sect.2.1(6)
Product (Va) ₀	6.987	m ² /s			V _{exit} D/2(θ _s /θ _a) ^{1/2}	
Solve for plume-averaged vertical velocity at height 200.0 feet						
60.96	meters above ground (z'+h _s)					
Gives the following Height above Stack z'	38.100	meters*	125.0	feet*		
Plume Top-Hat Diameter 2a'	11.665	meters	38.3	feet	2a' = 2*0.16(z'-z _v)	Sect.2/Eq.6
Vertical Velocity V	2.731	m/s	8.96	ft/sec	V = {(Va) ₀ ³ + 0.12F ₀ [(z-z _v) ² - (6.25D-z _v) ²] ^{1/3} / (2a'/2)	Sect.2/Eq.6
Solve for Height of CASC critical vertical velocity V _{crit} 5.30 m/s plume-averaged vertical velocity						
Critical VV > Top of Jet (Spillane)						
Find Height above Stack z _{crit}	11.563	meters	37.9	feet	Solve for x=(z-z _v) simultaneously in both eqs. (i.e., Va and a)	
Height above Ground z _{crit} +h _s	34.423	meters	112.9	feet	for V=4.3 m/s using the cubic equation ax ³ +bx ² +cx+d=0, where	
						a=1, c=0, and b=-(0.12F ₀)/(4.3 ³ 0.16 ³)=-4.5958
						and d=[0.12F ₀ (6.25D-z _v) ² -(Va) ₀ ³]/(4.3 ³ 0.16 ³)=-523.34
Interpolated Height of critical vertical velocity in Jet Phase:						
Find Height above Stack z _{crit}	#N/A	meters	#N/A	feet	http://www.1728.org/cubic.htm	
Height above Ground z _{crit} +h _s	#N/A	meters	#N/A	feet	gives the real solution x = z-z _v = 9.9171	
						or z(m/above stack) = 11.563
						z(ft/above ground) = 112.9
Table of Plume Top-Hat Diameters (2a) and Plume-Averaged Vertical Velocities starting at end of jet phase:						
Height (feet)	(meters)	Plume Radius(m)	SingleStk VertVel(m/s)	Plume Temp(K)		
above ground	above stack					
Stack Rel.Ht = 75.0						
0.00	0.356	31.20				
80.0	1.52	0.477	25.86	Jet Phase Eqs: 5 foot Intervals		
85.0	3.05	0.599	20.52	Linearly interpolated from Stack Rel.Ht to Top of Jet		
Top of jet = 89.6						
4.45	0.711	15.60	Spillane Equations:			
90.0	4.57	0.468	14.95	480.36	V _{plume} = {(Va) ₀ ³ + 0.12F ₀ [(z-z _v) ² - (6.25D-z _v) ²] ^{1/3} / a	
100.0	7.62	0.956	7.83	383.84	a = 0.16(z-z _v) 10 foot Intervals	
110.0	10.67	1.444	5.67	351.66	θ _s = θ _a [1 + (1 - (θ _s /θ _a)) * (V _{exit} D ² / (4V _{plume} ² a ² λ ²))]	
Spillane 5.3 m/s Height = 112.9						
11.56	1.587	5.30	345.97			
120.0	13.72	1.931	4.66	335.83		
130.0	16.76	2.419	4.08	326.68		
140.0	19.81	2.907	3.70	320.89	Max < 5.30 m/s	
150.0	22.86	3.394	3.43	316.98		
160.0	25.91	3.882	3.23	314.21		
170.0	28.96	4.370	3.07	312.18		
220.0	44.20	6.808	2.58	307.10	50 foot Intervals	
270.0	59.44	9.246	2.30	305.17		
320.0	74.68	11.685	2.12	304.22		
370.0	89.92	14.123	1.99	303.68		
420.0	105.16	16.562	1.88	303.34		
470.0	120.40	19.000	1.80	303.11		
520.0	135.64	21.438	1.73	302.95		
620.0	166.12	26.315	1.61	302.73	100 foot Intervals	
720.0	196.60	31.192	1.52	302.60		
820.0	227.08	36.069	1.45	302.52		
920.0	257.56	40.946	1.39	302.46		
1020.0	288.04	45.822	1.34	302.42		
1120.0	318.52	50.699	1.29	302.39		
1220.0	349.00	55.576	1.25	302.36		
1320.0	379.48	60.453	1.22	302.34		
1420.0	409.96	65.330	1.19	302.33		
1520.0	440.44	70.206	1.16	302.31		
1620.0	470.92	75.083	1.13	302.30		
1720.0	501.40	79.960	1.11	302.29		
1820.0	531.88	84.837	1.09	302.28		
1920.0	562.36	89.714	1.07	302.28		
2020.0	592.84	94.590	1.05	302.27		

*Summer Max = Monthly Mean of Maximum Daily Temperatures for 1971-2000 (Highest in July)
 NOAA Sources: Climatology of the United States No.81 "Monthly Station Normals of Temperatures, Precipitation, and Heating and Cooling Degree Days, 1971-2000 California" and Climatology of the United States No. 20 "Monthly Station Climate Summaries, 1971-2000 California"



SINGLE/Approximated Plume Average Vertical Velocities for LBGF Chillers using CEC Staff Methodology - Winter Min*					
Based on 48 chillers w/ 20 cells/chiller. Calc' eff.diam for each chiller with each cell at 34" ID (220,110 ACFM total for each chiller).		"Aviation Safety and Buoyant Plumes," Peter Best, et. al. "The Evaluation of Maximum Updraft Speeds for Calm Conditions at Various Heights in the Plume from a Gas-Turbine Power Station at Oakey, Queensland, Australia," Dr. K.T. Spillane			
Ambient Conditions:		Constants: Assume neutral conditions (dθ/dz=0 or θ _a =θ ₀)			
Ambient Potential Temp θ _a	278.15 Kelvins	41.0 °F		0.3048 meters/feet	
Plume Exit Conditions:				Gravity g	9.81 m/s ²
Stack Height h _s	23.81 meters	78 2/12 feet-inches		λ	1.11
Individual Chiller Stack Diameter D	3.8621 meters	152.1 inches		λ ₀	-1.0
Stack Velocity V _{exit}	8.06 m/s	26.45 ft/sec		4Vol/(60πD ²)	
Individual Chiller Volumetric Flow	94.44 cu.m/sec	200,110 ACFM		πV _{exit} D ² /4	Sect.2/¶1
Stack Potential Temp θ _s	289.26 Kelvins	61.0 °F			
Initial Stack Buoyancy Flux F ₀	11.3279 m ⁴ /s ³	20.0 ΔT(°F)		gV _{exit} D ² (1-θ _s /θ _a)/4 = Vol.Flow(g/m)(1-θ _s /θ _a)	Sect.2/¶1
Plume Buoyancy Flux F	N/A m ⁴ /s ³			λ ² gVa ² (1-θ _s /θ _p) for a,V,θ _p at plume height (see below)	
Number of Chillers n	48		2.632	Multiple Stack Multiplication Factor (n ^{0.25})	
Conditions at End (Top) of Jet Phase:					
Height above Stack z _{jet}	24.138 meters*	79.2 feet*		z _{jet} = 6.25D, meters*=meters above stack top	Sect.3/¶1
Height above Ground z _{jet} +h _s	47.952 meters	157.3 feet			"
Vertical Velocity V _{jet}	4.031 m/s	13.22 ft/sec		V _{jet} = 0.5V _{exit} = V _{exit} /2	"
Plume Top-Hat Diameter 2a _{jet}	7.724 meters	25.3 feet		2a _{jet} = 2D	Conservation of momentum
Spillane Methodology - Analytical Solutions for Calm Conditions for Plume Heights above Jet Phase					
Single Plume-averaged Vertical Velocity V given by Analytical Solution in Paper where Product Va given by equations below:					
Plume Top-Hat Radius a	Solutions in Table Below		0.16(z-z _v), or linear increase with height		Sect.2/Eq.6
Virtual Source Height z _v	0.468 meters*	1.5 feet*	6.25D[1-(θ _s /θ _a) ^{1/2}], meters*=meters above stack top		Sect.2/Eq.6
Height above Ground z _v +h _s	24.282 meters	79.7 feet	where (θ _s /θ _a) ^{1/2} = (θ _s /θ _a) ^{1/2} = 0.9806		
Vertical Velocity V	Solutions in Table Below		{(Va) ₀ ³ + 0.12F ₀ [(z-z _v) ² - (6.25D-z _v) ²] ^(1/3) / a		Sect.2.1(6)
Product (Va) ₀	15.265 m ² /s		V _{exit} D/2(θ _s /θ _a) ^{1/2}		
Single Chiller Results:					
Solve for plume-averaged vertical velocity at height		940.0 feet	286.512 meters above ground (z'+h _s)		
Gives the following Height above Stack z'	262.698 meters*	861.9 feet*			
Plume Top-Hat Diameter 2a'	83.914 meters	275.3 feet	2a'=2*0.16(z'-z _v)		Sect.2/Eq.6
Vertical Velocity V	1.092 m/s	3.58 ft/sec	V={[(Va) ₀ ³ +0.12F ₀ [(z-z _v) ² -(6.25D-z _v) ²] ^(1/3)]/(2a'/2)}		Sect.2/Eq.6
Solve for Height of CASC critical vertical velocity V _{crit}		5.30 m/s plume-averaged vertical velocity	Critical VV < Top of Jet		
Find Height above Stack z _{crit}	#N/A meters	#N/A feet	Solve for x=(z-z _v) simultaneously in both eqs. (i.e., Va and a)		
Height above Ground z _{crit} +h _s	#N/A meters	#N/A feet	for V=V _{crit} using the cubic equation ax ³ +bx ² +cx+d=0, where		
a=1, c=0, and b=-[0.12F ₀]/(V _{crit} ³ 0.16 ³)=-2.22917					
and d=[0.12F ₀ (6.25D-z _v) ² -(Va) ₀ ³]/(V _{crit} ³ 0.16 ³)=-4584.19					
Interpolated Height of critical vertical velocity in Jet Phase:					
Find Height above Stack z _{crit}	16.537 meters	54.3 feet	http://www.1728.org/cubic.htm		
Height above Ground z _{crit} +h _s	40.352 meters	132.4 feet	gives the real solution x = z-z _v =		17.3892
or z(m/above stack) = 17.857					
z(ft/above ground) = 136.7					
Table of Plume Top-Hat Diameters (2a) and Plume-Averaged Vertical Velocities starting at end of jet phase:					
Height (feet)	(meters)	Plume Radius(m)	SingleStk VertVel(m/s)	Plume Temp(K)	
above ground	above stack				
Stack.Rel.Ht = 78.1	0.00	1.931	8.06		
80.0	0.57	1.977	7.97		Jet Phase Eqs: 20 ft Intervals
100.0	6.67	2.464	6.95		Linearly interpolated from Stack Rel.Ht to Top of Jet
120.0	12.76	2.952	5.93		Spillane Equations:
Single Jet 5.3 m/s Height = 132.4	16.54	3.254	5.30		
140.0	18.86	3.440	4.91		V _{plume} ={[(Va) ₀ ³ +0.12F ₀ [(z-z _v) ² -(6.25D-z _v) ²] ^(1/3) / a
Top of Single jet = 157.3	24.14	3.862	4.03		a = 0.16(z-z _v)
160.0	24.95	3.918	3.92	282.49	θ _p =θ _s (1-(1-(θ _s /θ _a)) ² *(V _{exit} D ² /(4V _{plume} *a ² *λ ²)))
180.0	31.05	4.893	3.26	282.49	CEC Staff Equation:
200.0	37.15	5.868	2.84	281.49	V _{mp} =n ^{0.25} V _{sp}
220.0	43.24	6.844	2.54	280.82	Brigg's Equation:
240.0	49.34	7.819	2.33	280.34	V _{Briggs} = (2/3) x 1.6 ^(0.2) x F _{mp} ^(1/2) x u ^(1/2) x z ^(1/2)
260.0	55.43	8.795	2.16	279.98	where F _{mp} = nF _{sp}
280.0	61.53	9.770	2.04	279.71	
300.0	67.63	10.745	1.93	279.49	
350.0	82.87	13.184	1.74	279.32	50 ft Intervals
400.0	98.11	15.622	1.60	279.01	Max<5.3 m/s
450.0	113.35	18.060	1.51	278.82	
500.0	128.59	20.499	1.43	278.68	
550.0	143.83	22.937	1.37	278.58	
600.0	159.07	25.376	1.31	278.51	
650.0	174.31	27.814	1.27	278.46	
700.0	189.55	30.252	1.23	278.42	
800.0	220.03	35.129	1.16	278.38	
900.0	250.51	40.006	1.11	278.33	100 ft Intervals
1000.0	280.99	44.883	1.07	278.30	
1100.0	311.47	49.760	1.03	278.27	
1200.0	341.95	54.636	1.00	278.25	
1300.0	372.43	59.513	0.97	278.24	
1400.0	402.91	64.390	0.94	278.23	
1500.0	433.39	69.267	0.92	278.22	
2000.0	585.79	93.651	0.83	278.21	
2500.0	738.19	118.035	0.77	278.19	500 ft Intervals
3000.0	890.59	142.419	0.72	278.17	
3500.0	1042.99	166.803	0.68	278.17	
4000.0	1195.39	191.187	0.65	278.16	
4500.0	1347.79	215.571	0.63	278.16	
*Winter Min = Monthly Mean of Minimum Daily Temperatures for 1971-2000 (Lowest in Dec)					
NOAA Sources: Climatology of the United					



MERGED (along width) Plume Average Vertical Velocities for Lafayette Chillers using CEC Staff Methodology - Winter Min*					
"Aviation Safety and Buoyant Plumes," Peter Best, et. al.					
"The Evaluation of Maximum Updraft Speeds for Calm Conditions at Various Heights in the Merged Plume from Two Gas-Turbine Power Station at Oakey, Queensland, Australia," Dr. K.T. Spillane					
Ambient Conditions:			Constants: Assume neutral conditions (dθ/dz=0 or θ _a =θ _s)		
Ambient Potential Temp θ _a	278.15 Kelvins	41.0 °F		0.3048 meters/feet	
Plume Exit Conditions:			Gravity g	9.81 m/s ²	
Stack Height h _s	23.81 meters	78 2/12 feet-inches	λ	1.11	
Individual Stack Diameter D	3.86213661 meters	152.1 inches	λ ₀	-1.0	
Stack Velocity V _{exit}	8.06 m/s	26.45 ft/sec	4Vol/(60πD ²)		
Individual Volumetric Flow	94.44 cu.m/sec	200,110 ACFM	πV _{exit} D ² /4		Sect.2/¶11
Stack Potential Temp θ _s	289.26 Kelvins	61.0 °F			
Initial Stack Buoyancy Flux F ₀	11.33 m ³ /s ³	20.0 ΔT(°F)	gV _{exit} D ² (1-θ _a /θ _s)/4 = Vol.Flow(g/π)(1-θ _a /θ _s)		Sect.2/¶11
Plume Buoyancy Flux F	N/A m ³ /s ³		λ ² gVa ² (1-θ _a /θ _s) for a,V,θ _s at plume height (see below)		
Total Number of Stacks n	48				
Average Adjacent Stack Separation d	7.50 meters	24.6 feet	Calcs based on multiple plume treatment in Peter Best Paper: plume velocities increased by N ^{0.25} at the height where plumes fully merged (interp. below ht, single merged stack above ht)		
Number of Stacks along Orientation N	16				
Conditions at End (Top) of Jet Phase:					
Height above Stack z _{jet}	24.138 meters*	79.2 feet*	Z _{jet} = 6.25D, meters*=meters above stack top		Sect.3/¶11
Height above Ground z _{jet} +h _s	47.952 meters	157.3 feet			
Vertical Velocity V _{jet}	4.031 m/s	13.22 ft/sec	V _{jet} = 0.5V _{exit} = V _{exit} /2		
Plume Top-Hat Diameter 2a _{jet}	7.724 meters	25.3 feet	2a _{jet} = 2D	Conservation of momentum	
Spillane Methodology - Analytical Solutions for Calm Conditions for Plume Heights above Jet and Merging Phases					
Single Plume-averaged Vertical Velocity V given by Analytical Solution in Paper where			Product Va given by equations below:		
Single Plume Values: Plume Top-Hat Radius a			Used in Plume Merging Only		
Virtual Source Height z _v	0.468 meters*	1.5 feet*	a = 0.16(z-z _v), or linear increase with height		Sect.2/Eq.6
Height above Ground z _v +h _s	24.282 meters	79.7 feet	z _v = 6.25D[1-(θ _a /θ _s) ^{1/2}], meters*=meters above stack top		Sect.2/Eq.6
Single Plume Values: Vertical Velocity V			Used in Plume Merging Only		
Product (Va) ₀	15.265 m ² /s		{(Va) ₀ ³ + 0.12F ₀ [(z-z _v) ² - (6.25D-z _v) ²] ^{1/3} / a		Sect.2.1(6)
			V _{exit} (D/2)(θ _a /θ _s) ^{1/2}		
Plume Merging - Based on Single Plume Calculations where:					
Begin Merging Plume Top-Hat Diameter 2a _{touch}	7.500 meters	24.6 feet	2a _{touch} =d, (or a _{touch} =d/2)		Sect.3/¶13
Height above Stack z _{touch}	23.906 meters*	78.4 feet*	Z _{touch} = z _v +d/(2*0.16), meters*=meters above stack top		
Height above Ground z _{touch} +h _s	47.720 meters	156.6 feet			
Vertical Velocity V _{touch}	4.065 m/s	13.3 ft/sec	V _{touch} = {(Va) ₀ ³ + 0.12F ₀ [(z-z _v) ² - (6.25D-z _v) ²] ^{1/3} / a		
Total Merging Plume Top-Hat Diameter 2a _{full}	112.500 meters	369.1 feet	2a _{full} =2d(N-1)/2, (or a _{full} =d(N-1)/2) FOR 2 STACKS, 2a _{full} =2d		
Height above Stack z _{full}	352.031 meters*	1155.0 feet*	Z _{full} = z _v +2d/(2*0.16), meters*=meters above stack top		
Height above Ground z _{full} +h _s	375.845 meters	1233.1 feet			
Vertical Velocity V _{full}	0.986 m/s	3.2 ft/sec	V _{full} = {(Va) ₀ ³ + 0.12F ₀ [(z _{full} -z _v) ² - (6.25D-z _v) ²] ^{1/3} / a _{full}		
Product (V ² a) _{full}	54 m ⁴ /s ³				
Conditions at End (Top) of Merging Phase - Define new values for V _{full} and a _{full} in Merged Plume calculations (based on TOTAL number of stacks):					
Merged Plume Values: Plume Diameter 2a			Solutions in Table Below		
Revised Merged Plume Radius a _m	148.058 meters	485.8 feet	2a = 2 x (a _m + 0.16(z-z _{full})), or linear increase with height		
Revised Merged Plume Velocity V _m	2.596 m/s	8.52 ft/sec	where a _m = n ^{0.25} a _{full} where Total Merging Occurs		
Revised Virtual Source Height z _{v,full}	352.031 meters*	1155.0 feet*	and V _m = n ^{0.25} V _{full} where Total Merging Occurs		
Revised Vertical Velocity V			Height above stack where Total Merging Occurs (shown above)		
Multiple Plume Calculations			Solutions in Tables Below		
Solve for plume-averaged vertical velocity at height			940.0 feet		
Gives the following Height above Stack z	262.698 meters*	861.9 feet*	286.512 meters above ground (z+h _s)		
Plume Top-Hat Radius a	#N/A meters	#N/A feet	LESS THAN TOP OF MERGING PHASE-INTERPOLATE		
Vertical Velocity V	2.996 m/s	9.83 ft/sec	a=a _m +0.16(z-z _{full}) if z>Z _{full}		
Solve for Height of CASC critical vertical velocity V _{crit}			5.30 m/s		
Find Height above Stack z _{crit}	JET meters	JET feet	V=[n(V ³ a) _{full} /a] ^{1/3} if z>Z _{full}		
Height above Ground z _{crit} +h _s	JET meters	JET feet	V _{crit} =Z _{touch} +(V _m -V _{touch})*(z'-Z _{touch})/(Z _{full} -Z _{touch}) if z _{touch} <z<Z _{full}		
Table of MERGED Plume-Averaged Vertical Velocities starting at Touching Height:			Single Plume Eqns (see Single Plume spreadsheet)		
Height (feet)	(meters)	Plume Radius(m)	Vel(m/s)		
above ground					
above stack					
Begin Merging (touch) = 156.6	23.92	3.750	4.06		
160.0	24.95	#N/A	4.06		
180.0	31.05	#N/A	4.03		
200.0	37.15	#N/A	4.01		
220.0	43.24	#N/A	3.98		
240.0	49.34	#N/A	3.95		
260.0	55.43	#N/A	3.92		
300.0	67.63	#N/A	3.87		
350.0	82.87	#N/A	3.80	50 ft Intervals	
400.0	98.11	#N/A	3.73		
450.0	113.35	#N/A	3.66		
500.0	128.59	#N/A	3.60		
550.0	143.83	#N/A	3.53		
600.0	159.07	#N/A	3.46		
650.0	174.31	#N/A	3.39		
700.0	189.55	#N/A	3.32		
800.0	220.03	#N/A	3.19		
900.0	250.51	#N/A	3.05		
1000.0	280.99	#N/A	2.91		
1100.0	311.47	#N/A	2.78		
1200.0	341.95	#N/A	2.64		
End Merging (full/mp) = 1233.1	352.03	148.058	2.60		
1300.0	372.43	151.322	2.58		
1400.0	402.91	156.198	2.55		
1500.0	433.39	161.075	2.52		
2000.0	585.79	185.459	2.41		
2500.0	738.19	209.843	2.31		
3000.0	890.59	234.227	2.23		
3500.0	1042.99	258.611	2.16		
4000.0	1195.39	282.995	2.09		
4500.0	1347.79	307.379	2.04		
5000.0	1500.19	331.763	1.98	500 ft Intervals	



SINGLE/Approximated Plume Average Vertical Velocities for Lafayette Chillers using CEC Staff Methodology - Summer Max*						
Based on 88 chillers w/ 20 cells/chiller. Calc' eff.diam for each chiller with each cell at 34" ID (220,110 ACFM total for each chiller).		"Aviation Safety and Buoyant Plumes," Peter Best, et. al. "The Evaluation of Maximum Updraft Speeds for Calm Conditions at Various Heights in the Plume from a Gas-Turbine Power Station at Oakey, Queensland, Australia," Dr. K.T. Spillane				
Ambient Conditions:						
Ambient Potential Temp θ_a	302.21 Kelvins	84.3 °F	Constants: Assume neutral conditions (d ₀ /dz=0 or $\theta_a=\theta_b$)			
Plume Exit Conditions:						
Stack Height h_s	23.81 meters	78 2/12 feet-inches	Gravity g	9.81 m/s ²		
Individual Chiller Stack Diameter D	3.8621 meters	152.1 inches	λ	1.11		
Stack Velocity V_{exit}	8.06 m/s	26.45 ft/sec	λ_o	-1.0		
Individual Chiller Volumetric Flow	94.44 cu.m/sec	200,110 ACFM	$4Vol/(60\pi D^2)$			
Stack Potential Temp θ_s	313.32 Kelvins	104.3 °F	$\pi V_{exit} D^2/4$	Sect.2/¶1		
Initial Stack Buoyancy Flux F_o	10.4540 m ⁴ /s ³	20.0 ΔT(°F)	$gV_{exit} D^2(1-\theta_s/\theta_a)/4 = Vol.Flow(g/\pi)(1-\theta_s/\theta_a)$	Sect.2/¶1		
Plume Buoyancy Flux F	N/A m ⁴ /s ³		$\lambda^2 g Va^2(1-\theta_s/\theta_a)$ for a,V, θ_p at plume height (see below)			
Number of Chillers n	48		2.632 Multiple Stack Multiplication Factor ($n^{0.25}$)			
Conditions at End (Top) of Jet Phase:						
Height above Stack z_{jet}	24.138 meters*	79.2 feet*	$z_{jet} = 6.25D$, meters*=meters above stack top	Sect.3/¶1		
Height above Ground $z_{jet}+h_s$	47.952 meters	157.3 feet		"		
Vertical Velocity V_{jet}	4.031 m/s	13.22 ft/sec	$V_{jet} = 0.5V_{exit} = V_{exit}/2$	"		
Plume Top-Hat Diameter $2a_{jet}$	7.724 meters	25.3 feet	$2a_{jet} = 2D$	Conservation of momentum		
Spillane Methodology - Analytical Solutions for Calm Conditions for Plume Heights above Jet Phase						
Single Plume-averaged Vertical Velocity V given by Analytical Solution in Paper where Product Va given by equations below:						
Plume Top-Hat Radius a	Solutions in Table Below		0.16(z-z _v), or linear increase with height		Sect.2/Eq.6	
Virtual Source Height z _v	0.432 meters*	1.4 feet*	6.25D[1-(θ_p/θ_s) ^{1/2}], meters*=meters above stack top		Sect.2/Eq.6	
Height above Ground z _v +h _s	24.246 meters	79.5 feet	where (θ_p/θ_s) ^{1/2} = (θ_p/θ_a) ^{1/2} = 0.9821			
Vertical Velocity V	Solutions in Table Below		$\{[(Va)_o^3 + 0.12F_o [(z-z_v)^2 - (6.25D-z_v)^2]]^{(1/3)} / a$		Sect.2.1(6)	
Product (Va) _o	15.289 m ² /s		$V_{exit} D/2(\theta_p/\theta_s)^{1/2}$			
Single Chiller Results:						
Solve for plume-averaged vertical velocity at height	1,000.0 feet		304.8 meters above ground (z'+h _s)			
Gives the following Height above Stack z'	280.986 meters*	921.9 feet*				
Plume Top-Hat Diameter 2a'	89.777 meters	294.5 feet	2a'=2*0.16(z'-z _v)		Sect.2/Eq.6	
Vertical Velocity V	1.040 m/s	3.41 ft/sec	$V = \{[(Va)_o^3 + 0.12F_o [(z-z_v)^2 - (6.25D-z_v)^2]]^{(1/3)} / (2a'/2)$		Sect.2/Eq.6	
Solve for Height of CASC critical vertical velocity V_{crit} = 5.30 m/s plume-averaged vertical velocity Critical VV < Top of Jet						
Find Height above Stack z _{crit}	#N/A meters	#N/A feet	Solve for x=(z-z _v) simultaneously in both eqs. (i.e., Va and a)			
Height above Ground z _{crit} +h _s	#N/A meters	#N/A feet	for V=V _{crit} using the cubic equation ax ³ +bx ² +cx+d=0, where			
			a=1, c=0, and b=-0.12F _o /(V _{crit} ³ 0.16 ³)=		-2.05720	
			and d=[0.12F _o (6.25D-z _v) ² -(Va) _o ³]/(V _{crit} ³ 0.16 ³)=		-4704.55	
			http://www.1728.org/cubic.htm			
Interpolated Height of critical vertical velocity in Jet Phase:						
Find Height above Stack z _{crit}	16.537 meters	54.3 feet				
Height above Ground z _{crit} +h _s	40.352 meters	132.4 feet	gives the real solution x = z-zv =		17.4707	
			or z(m/above stack) =		17.902	
			z(ft/above ground) =		136.9	
Table of Plume Top-Hat Diameters (2a) and Plume-Averaged Vertical Velocities starting at end of jet phase:						
Height (feet)	(meters)	Plume Radius(m)	SingleStk VertVel(m/s)	Plume Temp(K)		
above ground	above stack					
Stack.Rel.Ht = 78.1	0.00	1.931	8.06			
80.0	0.57	1.977	7.97		Jet Phase Eqs: 20 ft Intervals	
100.0	6.67	2.464	6.95		Linearly interpolated from Stack Rel.Ht to Top of Jet	
120.0	12.76	2.952	5.93		Spillane Equations:	
Single Jet 5.3 m/s Height = 132.4	16.54	3.254	5.30			
140.0	18.86	3.440	4.91		$V_{plume} = \{[(Va)_o^3 + 0.12F_o [(z-z_v)^2 - (6.25D-z_v)^2]]^{1/3} / a$	
Top of Single jet = 157.3	24.14	3.862	4.03		a = 0.16(z-z _v)	
160.0	24.95	3.924	3.91	306.56	$\theta_p = \theta_s (1 + (1 - (\theta_p/\theta_s)) * (V_{exit} D^2 / (4V_{plume} a^2 \lambda^2)))$	
180.0	31.05	4.899	3.25	306.55	CEC Staff Equation:	
200.0	37.15	5.874	2.82	305.56	$V_{mp} = n^{0.25} V_{sp}$	
220.0	43.24	6.850	2.52	304.89	Brigg's Equation:	
240.0	49.34	7.825	2.31	304.42	$V_{avg} = (2/3) * 1.6^{(3/2)} * F_{mp}^{(1/2)} * u^{(1/2)} * z^{(1/2)}$	
260.0	55.43	8.800	2.14	304.06	where $F_{mp} = nF_{sp}$	
280.0	61.53	9.776	2.01	303.79		
300.0	67.63	10.751	1.90	303.57		
350.0	82.87	13.189	1.71	303.40	50 ft Intervals	
400.0	98.11	15.628	1.57	303.09	Max<5.3 m/s	
450.0	113.35	18.066	1.47	302.89		
500.0	128.59	20.505	1.40	302.75		
550.0	143.83	22.943	1.33	302.66		
600.0	159.07	25.381	1.28	302.58		
650.0	174.31	27.820	1.24	302.53		
700.0	189.55	30.258	1.20	302.48		
800.0	220.03	35.135	1.13	302.45	100 ft Intervals	
900.0	250.51	40.012	1.08	302.40		
1000.0	280.99	44.889	1.04	302.36		
1100.0	311.47	49.765	1.00	302.33		
1200.0	341.95	54.642	0.97	302.32		
1300.0	372.43	59.519	0.94	302.30		
1400.0	402.91	64.396	0.92	302.29		
1500.0	433.39	69.273	0.89	302.28		
2000.0	585.79	93.657	0.81	302.27	500 ft Intervals	
2500.0	738.19	118.041	0.75	302.25		
3000.0	890.59	142.425	0.70	302.24		
3500.0	1042.99	166.809	0.67	302.23		
4000.0	1195.39	191.193	0.64	302.22		
4500.0	1347.79	215.577	0.61	302.22		

*Winter Min = Monthly Mean of Minimum Daily Temperatures for 1971-2000 (Lowest in Dec)
NOAA Sources: Climatology of the United



MERGED (along length) Plume Average Vertical Velocities for Lafayette Chillers using CEC Staff Methodology - Summer Max*					
"Aviation Safety and Buoyant Plumes," Peter Best, et. al.					
"The Evaluation of Maximum Updraft Speeds for Calm Conditions at Various Heights in the Merged Plume from Two Gas-Turbine Power Station at Oakey, Queensland, Australia," Dr. K.T. Spillane					
Ambient Conditions:		Ambient Potential Temp θ_a		Constants: Assume neutral conditions (d ₀ /dz=0 or $\theta_a=\theta_{a0}$)	
		302.21 Kelvins	84.3 °F	0.3048 meters/feet	
Plume Exit Conditions:		Stack Height h_s		Gravity g	
		23.81 meters	78 2/12 feet-inches	9.81 m/s ²	
		Individual Stack Diameter D		λ	
		3.86213661 meters	152.1 inches	1.11	
		Stack Velocity V_{exit}		λ_{co}	
		8.06 m/s	26.45 ft/sec	-1.0	
		Individual Volumetric Flow		$4Vol/(60\pi D^2)$	
		94.44 cu.m/sec	200,110 ACFM	$\pi V_{exit} D^2/4$	
		Stack Potential Temp θ_s		Sect.2/¶1	
		313.32 Kelvins	104.3 °F		
		Initial Stack Buoyancy Flux F_o		$gV_{exit} D^2(1-\theta_s/\theta_a)/4 = Vol.Flow(g/\pi)(1-\theta_s/\theta_a)$	
		10.45 m ² /s ³	20.0 ΔT(°F)	Sect.2/¶1	
		Plume Buoyancy Flux F		$\lambda^2 g Va^2(1-\theta_p/\theta_a)$ for a, V, θ_p at plume height (see below)	
		N/A m ⁴ /s ³			
		Total Number of Stacks n			
		48			
		Average Adjacent Stack Separation d			
		16.31 meters	53.5 feet		
		Number of Stacks along Orientation N			
		3			
Conditions at End (Top) of Jet Phase:					
		Height above Stack z_{jet}		$z_{jet} = 6.25D$, meters*=meters above stack top	
		24.138 meters*	79.2 feet*	Sect.3/¶1	
		Height above Ground $z_{jet}+h_s$		157.3 feet	
		47.952 meters	157.3 feet	*	
		Vertical Velocity V_{jet}		$V_{jet} = 0.5V_{exit} = V_{exit}/2$	
		4.031 m/s	13.22 ft/sec	*	
		Plume Top-Hat Diameter $2a_{jet}$		$2a_{jet} = 2D$ Conservation of momentum	
		7.724 meters	25.3 feet	*	
Spillane Methodology - Analytical Solutions for Calm Conditions for Plume Heights above Jet and Merging Phases					
Single Plume-averaged Vertical Velocity V given by Analytical Solution in Paper where Product Va given by equations below:					
Single Plume Values:		Plume Top-Hat Radius a		Used in Plume Merging Only	
		Virtual Source Height z_v		a = 0.16(z-z _v), or linear increase with height	
		Height above Ground z_v+h_s		$z_v = 6.25D[1-(\theta_s/\theta_a)^{1/2}]$, meters*=meters above stack top	
		Vertical Velocity V		where $(\theta_s/\theta_a)^{1/2} = (\theta_a/\theta_s)^{1/2} = 0.9821$	
		Product (Va) _a		$\{[(Va)_a^3 + 0.12F_o [(z-z_v)^2 - (6.25D-z_v)^2]]^{1/3}\} / a$	
		15.289 m ² /s		Sect.2/Eq.6	
				Sect.2/Eq.6	
				Sect.2.1(6)	
				Sect.3/¶3	
Plume Merging - Based on Single Plume Calculations where:					
Begin Merging		Plume Top-Hat Diameter $2a_{touch}$		$2a_{touch}=d$, (or $a_{touch}=d/2$)	
		Height above Stack z_{touch}		$z_{touch} = z_v+d/(2*0.16)$, meters*=meters above stack top	
		Height above Ground $z_{touch}+h_s$		246.8 feet	
		Vertical Velocity V_{touch}		$V_{touch} = \{[(Va)_a^3 + 0.12F_o [(z-z_v)^2 - (6.25D-z_v)^2]]^{1/3}\} / a$	
		2.244 m/s		7.4 ft/sec	
Total Merging		Plume Top-Hat Diameter $2a_{full}$		FOR 2 STACKS, $2a_{full}=2d$	
		Height above Stack z_{full}		$z_{full} = z_v+2d/(2*0.16)$, meters*=meters above stack top	
		Height above Ground $z_{full}+h_s$		414.0 feet	
		Vertical Velocity V_{full}		$V_{full} = \{[(Va)_a^3 + 0.12F_o [(z_{full}-z_v)^2 - (6.25D-z_v)^2]]^{1/3}\} / a_{full}$	
		1.542 m/s		5.1 ft/sec	
		Product $(V^2a)_{full}$		60 m ⁴ /s ³	
Conditions at End (Top) of Merging Phase - Define new values for V_{full} and a_{full} in Merged Plume calculations (based on TOTAL number of stacks):					
Merged Plume Values:		Plume Diameter 2a		Solutions in Table Below	
		Revised Merged Plume Radius a_m		where $a_m = n^{0.25}a_{full}$ where Total Merging Occurs	
		42.930 meters		140.8 feet	
		Revised Merged Plume Velocity V_m		and $V_m = n^{0.25}V_{full}$ where Total Merging Occurs	
		4.058 m/s		13.32 ft/sec	
		Revised Virtual Source Height z_{full}		Height above stack where Total Merging Occurs (shown above)	
		102.369 meters*		335.9 feet*	
		Revised Vertical Velocity V		Solutions in Tables Below	
				V = $(n(V^2a)_{full}/a)^{1/3}$ for heights above total merging elevation	
				V = $V_{touch} + (V_m - V_{touch}) * (z - z_{touch}) / (z_{full} - z_{touch})$ for heights below total merging elevation	
Multiple Plume Calculations					
Solve for plume-averaged vertical velocity at height		1,000.0 feet		304.8 meters above ground (z+h _s)	
		Gives the following Height above Stack z		REGULAR EQNS	
		280.986 meters*		921.9 feet*	
		Plume Top-Hat Radius a		a = $a_m + 0.16(z - z_{full})$ if $z > z_{full}$	
		71.509 meters		234.6 feet	
		Vertical Velocity V		V = $(n(V^2a)_{full}/a)^{1/3}$ if $z > z_{full}$	
		3.424 m/s		11.23 ft/sec	
				V = $V_{touch} + (V_m - V_{touch}) * (z - z_{touch}) / (z_{full} - z_{touch})$ if $z_{touch} < z < z_{full}$	
				V = single plume values if $z < z_{touch}$	
Solve for Height of CASC critical vertical velocity V_{crit}		5.30 m/s		BEFORE TOUCHING Critical VV < Top of Jet	
		Find Height above Stack z_{crit}		JET meters	
		JET meters		JET feet	
		Height above Ground $z_{crit}+h_s$		JET feet	
				$z_{crit} = z_{full} + \{[n(V^2a)_{full}/(V_{crit})^3] - a_m\} / 0.16$ if $V_{crit} < V_m$	
				$z_{crit} = z_{touch} + (z_{full} - z_{touch}) * (V_{crit} - V_{touch}) / (V_m - V_{touch})$ if $V_{crit} > V_m$	
Table of MERGED Plume-Averaged Vertical Velocities starting at Touching Height:					
		Height (feet)		Single Plume Eqns (see Single Plume spreadsheet)	
		(meters)		Vert.	
		above ground		above stack	
		above stack		Radius(m)	
		Vel(m/s)			
Begin Merging (touch) = 246.8		51.41		8.155	
		260.0		55.43	
		280.0		61.53	
		300.0		67.63	
		320.0		73.72	
		340.0		79.82	
		360.0		85.91	
		380.0		92.01	
		400.0		98.11	
End Merging (full/mp) = 414.0		102.37		42.930	
		450.0		113.35	
		500.0		128.59	
		550.0		143.83	
		600.0		159.07	
		650.0		174.31	
		700.0		189.55	
		800.0		220.03	
		900.0		250.51	
		1000.0		280.99	
		1100.0		311.47	
		1200.0		341.95	
		1300.0		372.43	
		1400.0		402.91	
		1500.0		433.39	
		2000.0		585.79	
		2500.0		738.19	
		3000.0		890.59	
		3500.0		1042.99	
		4000.0		1195.39	
		4500.0		1347.79	
		5000.0		1500.19	



MERGED (along width) Plume Average Vertical Velocities for Lafayette Chillers using CEC Staff Methodology - Summer Max*				
"Aviation Safety and Buoyant Plumes," Peter Best, et. al.				
"The Evaluation of Maximum Updraft Speeds for Calm Conditions at Various Heights in the Merged Plume from Two Gas-Turbine Power Station at Oakey, Queensland, Australia," Dr. K.T. Spillane				
Ambient Conditions:		Constants: Assume neutral conditions (dθ/dz=0 or θ _s =θ _a)		
Ambient Potential Temp θ _a	302.21 Kelvins	84.3 °F	0.3048 meters/feet	
Plume Exit Conditions:		Gravity g 9.81 m/s ²		
Stack Height h _s	23.81 meters	78 2/12 feet-inches	λ	1.11
Individual Stack Diameter D	3.86213661 meters	152.1 inches	λ _o	-1.0
Stack Velocity V _{exit}	8.06 m/s	26.45 ft/sec	4Vol/(60mD ²)	
Individual Volumetric Flow	94.44 cu.m/sec	200,110 ACFM	πV _{exit} D ² /4	
Stack Potential Temp θ _s	313.32 Kelvins	104.3 °F		
Initial Stack Buoyancy Flux F _o	10.45 m ³ /s ³	20.0 ΔT(°F)	gV _{exit} D ² (1-θ _s /θ _a)/4 = Vol.Flow(g/π)(1-θ _s /θ _a)	
Plume Buoyancy Flux F	N/A	m ³ /s ³	λ ³ gVa ² (1-θ _s /θ _p) for a,V,θ _p at plume height (see below)	
Total Number of Stacks n	48			
Average Adjacent Stack Separation d	7.50 meters	24.6 feet	Calcs based on multiple plume treatment in Peter Best Paper: plume velocities increased by N^{0.25} at the height where plumes fully merged (interp. below ht, single merged stack above ht)	
Number of Stacks along Orientation N	16			
Conditions at End (Top) of Jet Phase:				
Height above Stack Z _{jet}	24.138 meters*	79.2 feet*	Z _{jet} = 6.25D, meters*=meters above stack top	Sect.3/¶1
Height above Ground Z _{jet} +h _s	47.952 meters	157.3 feet		"
Vertical Velocity V _{jet}	4.031 m/s	13.22 ft/sec	V _{jet} = 0.5V _{exit} = V _{exit} /2	"
Plume Top-Hat Diameter 2a _{jet}	7.724 meters	25.3 feet	2a _{jet} = 2D	Conservation of momentum
Spillane Methodology - Analytical Solutions for Calm Conditions for Plume Heights above Jet and Merging Phases				
Single Plume-averaged Vertical Velocity V given by Analytical Solution in Paper where Product Va given by equations below:				
Single Plume Values: Plume Top-Hat Radius a		Used in Plume Merging Only		a = 0.16(z-z _v), or linear increase with height
Virtual Source Height z _v	0.432 meters*	1.4 feet*	Z _v = 6.25D[1-(θ _s /θ _a) ^{1/2}], meters*=meters above stack top	Sect.2/Eq.6
Height above Ground z _v +h _s	24.246 meters	79.5 feet	where (θ _s /θ _a) ^{1/2} = (θ _s /θ _a) ^{1/2} = 0.9821	Sect.2/Eq.6
Single Plume Values: Vertical Velocity V		Used in Plume Merging Only		{(Va) _s ³ + 0.12F _o [(z-z _v) ² - (6.25D-z _v) ²]} ^{1/3} / a
Product (Va) _s	15.289 m ² /s		V _{exit} (D/2)(θ _s /θ _a) ^{1/2}	Sect.2.1(6)
Plume Merging - Based on Single Plume Calculations where:				
Sect.3/¶3				
Begin Merging Plume Top-Hat Diameter 2a _{touch}		7.500 meters	24.6 feet	2a _{touch} =d, (or a _{touch} =d/2)
Height above Stack Z _{touch}	23.869 meters*	78.3 feet*	Z _{touch} = z _v +d/(2*0.16), meters*=meters above stack top	
Height above Ground Z _{touch} +h _s	47.683 meters	156.4 feet		
Vertical Velocity V _{touch}	4.071 m/s	13.4 ft/sec	V _{touch} = {(Va) _s ³ + 0.12F _o [(z-z _v) ² - (6.25D-z _v) ²]} ^{1/3} / a	
Total Merging Plume Top-Hat Diameter 2a _{full}		112.500 meters	369.1 feet	2a _{full} =2d(N-1)/2, (or a _{full} =d(N-1)/2) FOR 2 STACKS, 2a_{full}=2d
Height above Stack Z _{full}	351.994 meters*	1154.8 feet*	Z _{full} = z _v +2d/(2*0.16), meters*=meters above stack top	
Height above Ground Z _{full} +h _s	375.808 meters	1233.0 feet		
Vertical Velocity V _{full}	0.961 m/s	3.2 ft/sec	V _{full} = {(Va) _s ³ + 0.12F _o [(z _{full} -z _v) ² - (6.25D-z _v) ²]} ^{1/3} / a _{full}	
Product (V ³ a) _{full}	50 m ² /s ³			
Conditions at End (Top) of Merging Phase - Define new values for V_{full} and a_{full} in Merged Plume calculations (based on TOTAL number of stacks):				
Merged Plume Values: Plume Diameter 2a		Solutions in Table Below		2a = 2 x (a _m + 0.16(z-z _{full})), or linear increase with height
Revised Merged Plume Radius a _m	148.058 meters	485.8 feet	where a _m = n ^{0.25} a _{full} where Total Merging Occurs	
Revised Merged Plume Velocity V _m	2.529 m/s	8.30 ft/sec	and V _m = n ^{0.25} V _{full} where Total Merging Occurs	
Revised Virtual Source Height Z _{full}	351.994 meters*	1154.8 feet*	Height above stack where Total Merging Occurs (shown above)	
Revised Vertical Velocity V			V = (n(V ³ a) _{full}) ^{1/3} for heights above total merging elevation	
Multiple Plume Calculations				
Solve for plume-averaged vertical velocity at height		1,000.0 feet	304.8 meters above ground (z+h _s)	
Gives the following Height above Stack z	280.986 meters*	921.9 feet*	LESS THAN TOP OF MERGING PHASE-INTERPOLATE	
Plume Top-Hat Radius a	#N/A meters	#N/A feet	a = a _m + 0.16(z-z _{full}) if z > Z _{full}	
Vertical Velocity V	2.863 m/s	9.39 ft/sec	V = (n(V ³ a) _{full}) ^{1/3} if z > Z _{full}	
Solve for Height of CASC critical vertical velocity V_{crit}				
Find Height above Stack Z _{crit}	JET meters	JET feet	BEFORE TOUCHING	Critical VV < Top of Jet
Height above Ground z _{crit} +h _s	JET meters	JET feet	Z _{crit} = Z _{full} + [(n(V ³ a) _{full} /(V _{crit}) ³ - a _m)/0.16] if V _{crit} < V _m	
Table of MERGED Plume-Averaged Vertical Velocities starting at Touching Height:				
Single Plume Eqns (see Single Plume spreadsheet)				
Height (feet)	(meters)	Plume	Vert.	
above ground	above stack	Radius(m)	Vel(m/s)	
Begin Merging (touch) = 156.4				
160.0	23.86	3.750	4.07	
180.0	24.95	#N/A	4.07	
200.0	31.05	#N/A	4.04	
220.0	37.15	#N/A	4.01	
240.0	43.24	#N/A	3.98	
260.0	49.34	#N/A	3.95	
280.0	55.43	#N/A	3.92	
300.0	61.53	#N/A	3.87	
350.0	82.87	#N/A	3.79	50 ft Intervals
400.0	98.11	#N/A	3.72	
450.0	113.35	#N/A	3.65	
500.0	128.59	#N/A	3.58	
550.0	143.83	#N/A	3.51	
600.0	159.07	#N/A	3.44	
650.0	174.31	#N/A	3.36	
700.0	189.55	#N/A	3.29	
750.0	204.79	#N/A	3.22	
800.0	220.03	#N/A	3.15	
850.0	235.27	#N/A	3.08	100 ft Intervals
900.0	250.51	#N/A	3.01	
950.0	265.75	#N/A	2.93	
1000.0	280.99	#N/A	2.86	
1100.0	311.47	#N/A	2.72	
1200.0	341.95	#N/A	2.58	
End Merging (full/mp) = 1233.0				
1300.0	372.43	151.327	2.51	
1500.0	433.39	161.081	2.46	
2000.0	585.79	185.465	2.35	
2500.0	738.19	209.849	2.25	
3000.0	890.59	234.233	2.17	
3500.0	1042.99	258.617	2.10	
4000.0	1195.39	283.001	2.04	
4500.0	1347.79	307.385	1.98	
Merged Plume Eqns				
V = (n(V ³ a) _{full}) ^{1/3}				
a = a _m + 0.16(z-z _{full})				500 ft Intervals

